

### HYDRAULICS

HTIW

### WORKING TABIFS

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# E S BELLASIS, MINST CE FRECUENT FIGURER IN THE IRRIGATION BRANCH OF THE FIELD WORNS DEPARTMENT OF INDIA

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LONDON
1903



#### PREFACE

A NEW Treatise on Hydraulies is required for more than one reason It is required in order to include the very consider able advances which have been made of late years in nearly all branches of the science advances due to such investigations as those made by Mons Bazin on Weirs, by Mr Kennedy of the Indian Public Works Department, on the Power of Streams to carry Suspended Matter, and by engineers in America on Pipes and Apertures It is also required in order to develop and expand the branch of Hydraulics which relates to Flow in Open Channels In this branch there has always been an excessive number of matters regarding which information has been obtainable only in a scattered highly condensed, or otherwise defective form or has been altogether non existent 1 so that although they can easily be reduced to general principles and although they have often a direct practical bearing on his work the engmeer has had to find them out gradually for himself

The above remarks refer chiefly to the laws and principles of Hydraulics. Not less important is the matter of Co efficients. The very large errors (carrying with them waste of time and money when works are designed) in the co efficients given by the older writers are now fully admitted

<sup>&</sup>lt;sup>1</sup> Owing to ties, causes and to tie consequent want of portunity for studying matters and referring them to underlying immerples fallaces are not uncommon. Several are mentioned in the text, and one in particular in chan via art. 9

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by engineers and the advantage of using modern figures is recognised. Much light has been thrown on co efficients by the researches above mentioned and others equally recent

It has further seemed desirable to have a book which besides being a text book should include practical Examples and full Working Tables

In the present volume an attempt is made to deal with the above matters. The book has been compiled from notes which have extended over a long period and embody the results of twenty five years' practical experience and study both of observed facts and of current literature. It contains a very large proportion of new matter especially in chapters n iv vi vn, and in It is hoped that it may be found to meet the requirements both of the student and of the engmeer

In every branch considerable detail is gone into, but the reader who does not require details will have no difficulty in passing over them some being in small print and some forming special articles

For kindly supplying remarks or information on points which seemed doubtful I beg to thank Messis Bazin Stearns hafter and kennedy Professors Unwin Williams and Bovey, and Dr Brightmore

I also thank Messes Rivington for the attention which they have given to the printing and issue of the bool

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#### CHAPTER I

#### INTRODUCTION

### SECTION I -PRELIMINARY REMARKS AND DESIREMANT

- 1 Hydraulies.-Hydraulies is the science in which the flow of water, occurring under the conditions ordinarily met with in Engineering practice, is dealt with Based on the exact sciences of hydrostatics and dynamics, it is itself a practical, not an exact, Its principal laws are founded on theory, but owing to imperfections in theoretical knowledge, the algebraic formula employed to embody these laws are somewhat imperfect and con tain elements which are empirical, that is, derived from observation and not from theory The science of Hydraulics is concerned with the discussion of laws, principles, and formule, of such observed phenomena as are connected with them, and of their practical The quantities dealt with are generally velocities application and discharges, but sometimes they are pressures or energies is frequently necessary in Hydraulics to refer to particular works or machines, but this is done to afford practical illustrations of the application of the laws and principles Descriptions of works or machines form part of Hydraulic Engineering and not of Hydraulies, and the same remark applies to statistical information on subjects such as Ramfall Some description of Hydraulic Fieldwork is included in this work for reasons given below (chap ii art 25) The laws governing the power of a stream to move solids by rolling or carrying them are intimately connected with the laws of flow and are naturally included
  - 2 Pluids, Streams, and Channels—A 'fluid' is a substance which offers no resistance to distortion or change of form Fluids are divided into 'compressible fluids' or 'gases,' such as arr, and 'incompressible fluids' or 'hiquids,' such as water Perfect fluids are not met with, all being more or less 'viscous,' that is, offering some resistance, though it may be very small, to change of form A 'stream' is a mass of fluid having a general movement of

translation It is generally bounded laterally by solid substances which form its 'channel' If the channel completely encloses the stream, and is in contact with it all round, as in a pipe running full, it is called a 'closed channel', but if the upper surface of the stream is 'free,' as in a river or in a pipe running partly full, it is an 'open channel' An 'eddy' is a portion of fluid whose particles have movements which are irregular and generally more or less rotatory, it may be either stationary or moving with respect to other objects The 'axis' of a stream or channel is a line centrally

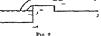


situated and parallel to the direction of flow an open channel its exact position need not be fixed but in a pipe it is supposed to pass through the centre of gravity of each cross section

An 'orifice' or 'short tube' (Fig 1) is a short closed channel expanding abruptly, or at least very rapidly, at both its upstream and downstream ends A short open channel similarly circumstanced

(Fig 2) is called a 'weir,' provided the expansions are wholly or partly in a vertical direction. When they are wholly lateral it is called a 'contracted channel'. All these short channels will collectively be

termed 'apertures,' and 'channel' will be used for channels of con siderable length



The stream issuing from an ori

fice or pipe is called a 'jet,' that
falling from a weir a 'sheet' Except in the case of a jet issuing
under water a stream bounded by other fluid of the same kind is called a 'current'

3 Velocity and Discharge -The direction of the flow of a stream is in general parallel to the axis, but it is not always so at each individual point. If at any point the flow is not parallel to the axis the velocity at that point may be resolved into two com ponents, one of which is parallel to the axis and the other at right angles to it The component parallel to the axis is termed the 'forward velocity' A 'cross section' of a stream is a section at right angles to the axis The velocities at all points in the cross section of a stream are not equal. A curve whose alscissas represent distances along a line in the plane of the cross section and whose ordinates represent forward velocities is called a 'velocity curve' The 'discharge' of a stream at any cross section is the volume of water passing the cross section in the

unit of time. The 'mean velocity' at any cross section is the mean of the different forward velocities. It is the discharge of the stream divided by the area of the cross section. Thus

$$\Gamma = \frac{Q}{4}$$
 or  $Q = A\Gamma$  (1)

This is the first elementary formula of Hydraulies - Fxcept when velocities at individual points are under consideration, the term 'velocity' is generally used instead of 'mean velocity'.

As long as the conditions under which flow takes place at any given cross-section of a stream remain constant, the velocity and discharge are constant, that is, they are the same in succeeding equal intervals of time. In this case the flow is said to be 'steady ' As soon as the conditions change, the velocity and dis charge usually change, and the flow is then said to be unsteady Owing to the introduction or abstraction of water by subsidiars channels, leakage, or evaporation, the discharges at successive cross sections of a stream may be unequal, but the flow may still be steady Flow is unsteady only when the discharge varies with the time, and not when it merely varies with the place Hydraulies, flow is always assumed to be steady unless the contrary is expressly stated. For instance, in the statement that a rise of surface level gives an increase in velocity, it must be understood that this refers to the period after the surface has risen, and not to that while it is rising In any length of stream in which the flow is steady, and in which no water is lost or gained, the discharges at all cross-sections are equal, or

$$0=A,V,=A,V,=\text{etc.}$$
 (2)

where  $A_1$ ,  $A_2$ , etc, are the areas of the cross sections, and  $V_1$ ,  $V_2$ , etc, the mean velocities. In other words, the mean velocity at any cross section is inversely as the sectional area.

#### SECTION II -PHENOMENA OBSERVED IN FLOWING WATER

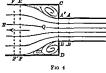
4 Irregular Character of Motion —In flowing water the free surface oscillates, especially in large and rapid streams. The oscillation is probably greater near the sides than at the centre. The motion of the water is also irregular. Except under peculiar conditions the fluid particles do not move in parallel lines, or 'stream lines' but their paths continually cross each other, and the velocity and direction of motion at any point vary every instant. The stream is, in fact, a mass of small eddies. The

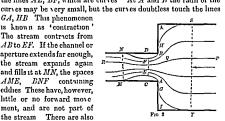
irregularities of motion increase with the roughness of the channel and with the velocity of the stream. They are especially great in open channels. Eddies produced at the bed are constantly rising to the surface. Floats dropped in at one point in quick succession move neither along the same paths nor with the same velocities. In experiments made by Iraneis, whitewash discharged into a stream four inches above the bed came to the surface in a length which was equal to ten to thirty times the depth, and was less, the rougher the channel. The eddies are strongest where they originate, namely, at the border of the stream. To compensate for the upward eddies there must, of course, be down ward currents, but they are diffused and hardly noticeable. The resistance to flow caused by all these irregular movements is enor mously greater than that which would exist in stream line motion.

Although the velocity and water level at any point fluctuate every moment as above described, the average values obtained in successive periods of time of longer duration are more or less constant The velocities obtained at any point in successive seconds will, perhaps, vary by 20 per cent, those obtained in successive minutes will vary much less, and those in successive periods of five minutes each probably scarcely at all The same is true of the direction of the flow. For the water level the averages of several observations obtained in periods of a minute each will probably agree very closely A velocity curve obtained from a few observations is generally irregular, but one obtained from a large number is regular If the flow is not steady, the average velocities and water levels obtained in successive long periods of time may, of course, vary, but they will exhibit a regular change When velocity and water level are spoken of, the average values and not the momentary values are meant, and this remark applies to the foregoing definition of steady flow The discharge at any cross section, if considered in its momentary aspect, is probably never steady The irregularity of the motion of water renders the theoretical investigation of flow extremely difficult, and no complete theory has yet been propounded 5 Contraction and Expansion -I vcept under an infinite force,

a body cannot, without either coming to rest or describing a curve, change its direction of motion. Acting in obedience to this law, water cannot turn shirp round a corner. Wherever any sharp salient angle 1 or 1 (Fig. 3) occurs in a channel, or at the entrance of an aperture the water travelling along the lines GA, III. cannot turn su idenly and follow the lines AC, IID. It follows

the lines AE, BF, which are curves At A and B the radii of the is known as 'contraction' The stream contracts from AB to EF. If the channel or aperture extends far enough, the stream expands again and fills it at MN, the spaces AME, BNF containing eddies These have, however, little or no forward move ment, and are not part of the stream There are also





eddies at K, L In a case of abrupt enlargement (Fig 4) the stream expands gradually, and there are eddies in the corners Similar phenomena occur at abrupt bends, bifurcations. and junctions For a closed channel or an orifice, Fig 3 represents any longitudinal section For an open channel or a weir, it represents a plan

or a horizontal section, and its lower part—from PQR downwards

—a vertical section And similarly with Fig 4 Sometimes still or 'dead' water may replace part of an eddy The term eddy will be used to include it

#### SECTION III - USEFUL FIGURES

6 Weights and Measures—The following table 1 gives the weight of distilled water for various temperatures. The weights of clear river and spring water are practically the same as the above For all ordinary practical purposes the weight of fresh water may be taken to be 62 4 lbs per cubic foot when clear, and 62 5 lbs or 1000 ounces when containing sediment is compressed by about one twenty thousandth part of its bulk by a pressure of one atmosphere. Sea water weighs about 64 lbs per cubic foot Water usually contains a small quantity of air in solution

<sup>1 5</sup>mith a Hydraulica chap. 1

Temperature (Fabrenheit)	Pounds per Cub c Foot.	Tu nperat ire (Fahrenhe t)	Pounds per Cubic Foot	Te   erature (Fahrenbe t)	Pounds per Cubic Foot
32°	62 42	95°	62 06	160°	61 01
35°	62 42	100°	62 00	165°	60 90
39 3°	62 424	105°	61 93	170°	60 80
45°	62 42	110°	61 86	175°	60 69
50°	62 41	115°	61 79	180°	60 59
55	62 39	120°	61 72	185°	60 48
60°	62 37	125°	61 64	190°	60 36
65°	62 34	130	61 55	195°	60 25
70°	62 30	135°	61 47	20 <b>6</b> °	60 14
75°	62 26	140°	61 39	205°	60 02
80°	62 22	145°	61 30	210°	59 89
85°	62 17	150°	61 20	212°	59 84
90°	62 12	155°	61 11		

An Imperial gallon of water contrains  $\frac{1}{6400}$  cubic feet, and weighs almost exactly 10 lbs. A United States gallon is five sixths of an Imperial gallon. A metre is 3 2809 feet, a cubic metre 35 317 cubic feet, a kilogram 2 2005 pounds avoirdupois, and a litre 61 027 cubic inches or 2201 gallons. A cubic metre of water weighs 1000 kilograms. The metric system being that chiefly employed on the continent of Europe, these figures may be useful in the conversion of figures given in reports of foreign experiments or in estigations. A French inch is 02707 of a metre or 0888 of an English foot.

The units employed in this work are the foot, the second, and the pound. Thus velocities and discharges are in feet or cubic feet per second, weights in pounds per cubic foot.

To Gravity and Air Pressure—The force of gravity, denoted by g, is generally assumed to be 32.2, that is, it is supposed to increase the velocity of a falling body by 32.2 feet per second, and  $\sqrt{2g}$ , a quantity very frequently occurring in hydrulies, is then 8.025. These figures are suitable for Great British and Canada, but the force of gravity varies with the locality, increasing with the littitude and decreasing with the height above see level. At the Equator at the sea level g is 32.09, and at the Pole at the sea level it is 32.26. The mean values of g and  $\sqrt{2g}$  for ordinary elevations and for latitudes up to  $70^\circ$  are 32.16 and 8.02 respectively. These are suitable for the United States, India, and Australia, and are adopted in this work. They, however, differ by only 12. per cent and 06 per cent respectively from the values given above, and ordinarily this difference is of no account what ever An increase of elevation of 5000 feet decreases a by only 16 and  $\sqrt{2g}$  by 002.

The pressure of the atmosphere near the scaledel is about 147 lbs. per squire inch, and is equivalent to about 30 inches of mercury or 34 fect of water. According to the 'Laglish system' of computation by 'atmospheres,' one atmosphere is equivalent to 29 905 inches of mercury in London at a temperature of 32.' Fahrenheit. The French asstem gives a pressure which is greater in the ratio of 1 to 2997. For elevations above the scaledel the atmospheric pressure decrease. Up to a height of 6000 feet the reduction for every thousand feet is about 51b per square inch, or 1 inch of mercury, or 113 feet of water. Above 6000 feet the reduction is less rapid, amounting to 19 lbs per square inch in rising from 6000 to 11,000 feet.

#### SECTION IV -- HISTORY AND REMARKS

8 Historical Summary—A historical sketch of Hydraulies given in the Encyclogedia Intiannia omprises the names of Cistelli, Torricelli, Pascal, Mirotte, Newton, Pitot, Bernouelli, D'Alembert, Dubuat, Bossut, Pronj, Eytelwein, Mallet, Vici, Hachette, and Bidone To these may be added Michelotti, D'Aubuisson, Castel, and Bodne

Coming to specific branches of Hydraulies and recent periods, flow in pipes has been mide the subject of experiment and investing the Newsbach, Coulomb, Venturn, Couplet, Dircy, Lampe, Hagen, Poiseuille, Reynolds, Smith, and Steuris, and flow through apertures by Poncelet, Lesburs, Weisbuch, Reinne, Blickwell, Boileau, Ellis, Bornemann, Thompson, Francis, Tunin, Fteley and Stearns, Herschel, Steckel, Fanning, and Smith All the chief experiments on pipes and apertures have been discussed and sum marised by Fanning's and Smith, both of whom have compiled tables of co-efficients for pipes and apertures Smith's discussions show great care, and his figures and conclusions will be largely utilised in this work, but since the publication of his and Fanning's works further important experiments have been made on weirs by Razin, and on weirs and pipes by various American engineers?

- 1 Encyclopædia Britannica 9th Edition Article 'Hydromechanics'
- " Lowell Hydraulic Experiments
- 3 Transactions of the American Society of Civil Engineers, vol xii
- 4 Hydraulics

Détersoir

- I reatise on Water Supply Engineering
  6 Annales des Poits et Chaussées Ath Series, Tomes 16 and 19 and 7th Series, Tomes 2, 7 12, and 15 A résumé is given in L'Écoulement en
  - 7 Transactions of the American Society of Civil Engineers, vols xix.,

Regarding flow in open channels, extensive observations and investigations have been made by Durey and Bizin<sup>1</sup> on small channels, by Humphreys and Abbott<sup>2</sup> on the Mississippi, and by Cumungham<sup>3</sup> on large canals. Many observations have also been made by German engineers and some by Revy<sup>4</sup> on the great South American rivers. In this branch of Hydraulies the Swiss engineers Ganguillet and Kutter have analysed most of the chief experiments, sincluding some made by themselves, and arrived at a series of coefficients for mean velocity. Their writings have been translated and commented on by Jackson, who has framed tables of coefficients based on their researches. Finally Bizin has reviewed the whole subject and arrived at some fresh coefficients. Investigations have been made by Francis on rod floats, by Stearns on current-meters, and by Kennedy on the silt-transporting power of streams.

9 Remarks—The different branches of Hydraulics are shown by the headings of chapters in to x of this work. In the following chapter the whole subject is considered in a general manner. This enables us to dispose once for all of many points which would otherwise have had to be mentioned in more than one of the subsequent chapters. Moreover, the different branches are not always divided by such hard and fast lines as might appear, there are many points common to two branches, and the preliminary consideration of the various branches of the subject in connection with one another instead of separately will be advantageous.

1 Pecherches Hydrauliques

" Peport on the Plysics and Hydraulics of the Mississippi I vier

3 I oorkee Hydraulic Experiments

4 Hydraulies of Great Rivers

b A General Formula for the Uniform Flow of Water in Rivers and other Channels Translated by Hering and Trautwine

and other Channels Translated by Hering and Trautwine

<sup>6</sup> The New Formula for Mean Velocity in Piers and Canals
Translated by Jackson

7 Canal and Culvert Tables

ftude d'une Nouvelle Formule pour Canaux Découterts

Dowell Hydraulic Experiments

10 Transactions of the American Society of Civil Engineers, vil xii

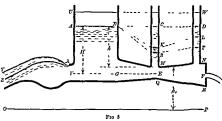
11 Menutes of Proceedings, Institution of Civil Ir gineers vol cxix

#### CHAPTER II

#### GENERAL PRINCIPLES AND FORMULÆ

#### SECTION I -FIRST PRINCIPLES

1 Bernouilli's Theorem —Let Fig 5 represent a body of still water, the openings at f and  $\iota$  being supposed to be closed The



water in the tubes at  $C_iD$  stands at the same level as AB. The 'head' or 'hydrostatie head' over any point is its depth below the plune AB. This plane is sometimes called the 'plane of charge'. The pressure is as the head. If P is the pressure per square foot at the depth  $H_i$  and W the weight of one cubic foot of water, then P = WH or  $H = \frac{P}{W}$ . The head H is said to be that 'due to' the pressure P

Livery particle of water in the reservoir possesses the same degree of potential energy. Comparing a particle at the depth II with one at the surface, the one possesses energy in virtue of its pressure, the other in virtue of its clevation.

Let an orifice be opened at F so that water flows along the pape  $GFF_s$  and let the reservoir be large, so that the water in it has no velocity and the surface AB is unaltered. The pressure in the water flowing in the pape is reduced, and the water levels in the

tubes fall to K, L The heights KM, LN are as the pressures at M and N, and they are called the 'hy draulte heads' or 'pressure heads'. The tubes are called 'pressure columns' and the line BKL the line of 'hy draulte gradient'. Let p be the pressure at M, and  $l_p$  the pressure head. Then  $h_p = \frac{p}{\sqrt{n}} \sum_{N} L$  be the velocity in the pipe at

M and let  $h_v = \frac{V^*}{2q}$  Then  $h_v$  is the 'velocity head'. It is the height through which a body falls under the influence of gravity in an unresisting medium in acquiring the velocity V, or the height to which it could be made to rise by parting with its velocity. Let it be supposed that there are no resistances to the motion of the water, so that no energy is consumed in overcoming them. Then by the law of the conservation of energy the total energy of any moving particle of water remains as before. Whatever is lost as pressure is gained as velocity. The head ch lost in pressure is the velocity head  $h_v$ . Thus

 $h=h_p+h_v$  (3) or the pressure head added to the velocity head is the hidrostitic head. This equation, due to Bernoulli, 1 is the basis of all theoretical hydraulic formulæ. It obviously applies to any point in the pipe

It has been seen that the pressure at M is as the height A M

Assume that the velocities at all points in the cross section MO are equal. Let  $H_p$  and  $H_v$  be the pressure head and velocity head at I, then  $H=H_1+H_v$ ,  $h=h_p+h_v$ . But since the velocities are equal,  $H_v=h_v$ , therefore  $H_p-h_1=H_v$ , or the change in pressure in passing from M to I is the sime answer was no flow. The pressure head at I is KF, and

the pressure at any point in the cross section is as its depth below K. Let OP be a datum line and let  $I_k$  be the 'head of elevation' of any point M above OP. Then  $k+h_k$  is constant for all points in the

system, and therefore

 $h_n + h_r + h_s = K$  (4)

where A is constant. This is Bernouillis theorem more fully stated. The total energy possessed by a particle of water is the sum of the energies due to its pressure velocity, and elevation.

If instead of a pipe we consider an open channel VF, the results obtained will be the same as before. If pressure columns were used the water in them would not rise above the surface VI. At each point in the surface the pressure head is zero and the velocity.

1 The simple method of proof just given is not Berrouilles but is taken from Merriman's Hydraules chap in

head is equal to the hydrostatic head. If the velocities at all points in a cross section are assumed to be equal, the law of change of pressure with depth is the same as before

Since the area  $\hat{NR}$  is greater than MQ, the velocity is less and the pressure greater. Thus from K to L there is a rise in the hydraulic gradient. Similarly, in the open stream there is a rise where the sectional area is increasing

The pressure in a body of flowing water can never be negative, as the continuity of the liquid would be broken

2 Loss of Head from Resistances—Practically a certain amount of head h' is always expended in overcoming resistances, due to the friction of the water on its channel and to the internal move ments of the water, so that the total head diminishes in going along the stream in the direction of the flow. In other words, the pressure head and velocity head do not together equal the hydrostatic head. The difference is the 'head lost'. The actual water-levels would in practice be S. T. and CS. DT would be the total losses of pressure head up to the points M and N. As head is lost, the work which the water is capable of doing in virtue of its clevation, pressure, and velocity is diminished. If h is the head lost by resistance between two cross sections, then

$$h = h - \frac{V_{s}^{1} - V_{1}^{2}}{2a}$$
 (5),

or the head lost is equal to the fall in the surface or line of gradient less the increase in the velocity head. The same is true of the open channel. The surface would be AZ instead of AY.

3 Atmospheric and other Pressures—Generally a body of water is subjected to the atmospheric pressure  $P_a$ . The head due to this pressure is  $\frac{P_a}{H^{s'}}$  and this has to be added in order to obtain the total head over any point. The case is the same as if the water surface at each point were raised from AD to UH' by a

height  $\frac{P}{P}$ . But usually—as in the preceding demonstrations—the relative heads over two or more points are considered, the pressure of the atmosphere affects all parts equally and is left out of consideration. If, however, different portions of the water are subjected to pressures of different intensities caused, sai, hi partly exhausted air, by steam, or by a weighted piston, the water surface of each portion of the system must be considered as being raised by a height  $\frac{P}{P}$ , where P is the intensity of the special pressure.

acting on it

#### SECTION II -FLOW THROUGH APERTURES

4 Definitions —An aperture is said to be 'in a thin wall' when its upstream edge is sharp (Figs. 6 and 7), and the 'wall' or structure containing the aperture is thin, or is



bevelled or stepped, so that the stream after passing the edge springs clear and does not touch it again. An aperture like that shown in Fig. 1 or Fig. 2, page 2, may have its upstream edge sharp, but it does not come within the definition. A rounded or 'bell mouthed' orifice (Fig. 8) is one in which the sides are curved so that



the tangents at c and d are parallel, and the stream after passing CD does not contract. A weir of analogous shape may be formed



1 10 S.

by rounding the angle between the top and the upstream side or 'face,' and by prolonging the side walls upstream

The upstream surface of the wall surrounding in

The upstream surface of the wall surrounding in aperture will be called the 'margin.' The margin is said to be 'clear' when it is free from projections, leakages, or anything which would interfere with the free flow of water along the wall towards the aperture. The clear margin, if not otherwise limited, is bounded by the sides of the reservoir or channel, or by any other aperture existing in the same wall. When an aperture has sharp edges an increase in the clear margin, up to a certain limit, increases the degree of contraction. When this limit has been reached the contraction is said to be 'complete'.

An aperture with sharp edges is 'normal' when the margin is plane and the axis of the aperture is perpendicular to the plane. Any other aperture is normal when its sides and approaches are symmetrical with regard to any plane (in the case of a werr any vertical plane) through the axis. For a

werr any vertical plane) through the axis. For a weir it is a further condition that the 'crest' or highest portion must be strught and horizontal from one side wall to the other, and, in the case of a weir in a thin wall, that the wall must be

<sup>1</sup> For this reason the expression 'sharp edgel,' used by some recent writers in preference to the old one of 'in a thin wall' is not suitable.

vertical Every aperture is assumed to be normal unless the contrary is expressly stated

5 Flow through Orifices —Let H be the height of the free surface (Fig. 9) above the centre of gravity of the small orifice C, D, or E, and let V be the velocity of the issuing jet. Both the jet and the free surface AB are supposed to be subject to the atmospheric pressure  $P_*$ . The total head over the orifice is  $H + \frac{P_*}{H_*}$ , and the pressure in and upon the issuing jet is  $P_*$ .

Then from equation 3 (page 10), supposing no head to be lost in overcoming resistances,

 $H + \frac{P_{\bullet}}{W} = \frac{P_{\bullet}}{W} + \frac{V^{s}}{2g},$  or  $V = \sqrt{2g}H . \qquad (6)$ 

or  $V = \sqrt{2gH}$ . (6)

All formulæ for flow from apertures are modifications of this The velocity  $\sqrt{2gH}$  is called the 'theoretical velocity' It is the same as would be acquired by a body falling from rest in a vacuum through a height H. If the jet issues vertically upwards it will, in the absence of all resistance except gravity, rise to the level of AB. The velocity depends only on H and not on the direction in which the jet issues. If AGR is a parabola with axis vertical and parameter 2g, the theoretical velocities of jets issuing at F, M, N are as the ordinates FG, MK, NR. Practically owing to resistances caused by friction and internal movements of the water, the velocity of efflux is less than the theoretical velocity, and is given by the formula

 $V=c_o\sqrt{2gH}$  (7),

where  $c_v$  is a 'co-efficient of velocity' whose mean value for the two kinds of orifices under consideration is about 97

Instead of assuming the water in the reservoir to have no appreciable motion, let it be supposed that it is moving with a velocity v directly towards the orifice. This velocity is called 'velocity of approach' and the discharge through the orifice is increased. The energy possessed by the water can, theoretically, raise it to a height  $\frac{v}{v}$  or h. This is called the head due to the

velocity of approach, and it must be added to the hydrostatic head Practically, for reasons which will be given below, a head nh has to be added, n being 10 or less. The formula thus becomes

 $V = c_v \sqrt{2g(H+nh)}$  (8)

If the fluid moved without resistance, a velocity v in any direction, and not only toward the orifice, could be utilised in increasing the

14

head and the discharge, but practically the only useful component of the velocity is that parallel to the axis of the orifice

In the case of an orifice in a thin wall (Fig 6), the jet attains a minimum cross section at AB, whose distance from the edge of the orifice is about half the diameter of the orifice, or half the least diameter if the orifice is of elongated form. This minimum section is called the 'vena contracta'. The ratio of its sectional area a to the area a of the orifice is called the 'co-efficient of contrac tion,' and is denoted by  $c_c$  thus  $a = c_c a$  The mean value of  $c_c$  is about 63 A vena contracta occurs with any kind of orifice having sharp edges, and cois probably about the same For a bell mouth c = 10

The discharge of an orifice is

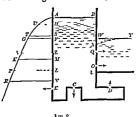
 $Q=a v=a c_s c_n \sqrt{2gH}$ 

Then c 15 the 'co efficient of discharge' and  $Q = ac \sqrt{2aH}$ 

Or when there is velocity of approach

 $Q = ac \sqrt{2g(H+nh)}$ . The value of c for ornices in thin walls averages about 61, and for bell mouthed orifices 97 It does not usually vary much with the head Generally the values of con co and c are not very greatly affected by the shape and size of an orifice nor by the amount of head Generally c is better known than c, or c, and it is also of far more importance

When an orifice has a head of water on both sides it is sud to be 'submerged' or 'drowned,' and H in the formula is the differ



ence between the two heads Thus for any orr fice Q or O (Fig 9), the head as BW It has no thing to do with the actual depth of the orifice below AB If in orifice is partly submerged it must be divided into two parts and only the lower part treated as submer\_ed If the water level at I' is higher than at A, as it mis be when AUI is a stream

whose size is not very great relatively to that of the orifice, the head is I \ and not I H'1 It is the pressure at A and not at Y that affects the discharge from the orifice The rise from X to Y is owing to the stream being in 'variable flow' (art 10)

When an ortice is in a horizontal plane, or when it is submerged, formula 7 to 10 apply, no matter what the size of the orifice may be When an orifice is in a vertical or inclined plane the theoretical velocity of each horizontal layer of water is  $\sqrt{2gH}$ , where H is the head over that layer. When the vertical height between the head, the mean velocity in the orifice is small compared to the head, the mean velocity in the orifice is practically that at its centre of gravity. If an orifice extends from M to N (Fig. 9), its contrebeng L, it is clear that, the curve KR being nearly straight, LP is practically the mean of all ordinates from M to N. But with an orither HZ, whose centre is F, the protuberance of the curve UV causes the mean ordinate to fall short of that at F, and a correction has to be applied depending on the shape of the orifice and the ratio of its depth to the head over its centre.

6 Flow over Weirs —Unless the contrary is stated, it will be assumed that all wers have vertical side walls, such forming in practice the vast majority. The remarks just made regarding the protuberance of the curve apply a fortion to a weir Let  $M(\mathrm{Fig}, 9)$  be the level of the crest of a weir. Let M=H and  $MS=\frac{4H}{9}$ . The mean of all the velocities from M to M is represented by  $ST^1$ . Thus the theoretical velocity V is  $\sqrt{2g\frac{4H}{9}}$  or  $\frac{2}{3}\sqrt{2gH}$ . The practical formula is

 $Q = \frac{2}{3} \operatorname{cl} \sqrt{2g} H^{\frac{1}{2}}$  (11)

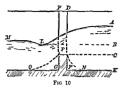
where I is the length of the crest, II the head on the crest, and e is a co-efficient of discharge whose value for sharp-edged wers averages about 62, and for others viries greatly according to the form of the wer. With increase of head the co-efficient increases in some cases and decreases in others. It is not usual to give a separate formula for finding e or to divide e into e, and e, but roughly these are about the same for sharp-edged wers as for sharp-edged orifices. If there is velocity of approach the formula is

$$Q = \frac{2}{3} cl \sqrt{-g} (Il + nh)^{\frac{1}{2}}$$
 (12)

where n is 10 or more, and h, as for orifices is  $\frac{r^2}{-1}$ , r being the velocity of approach

1 Fr proof see chap, m art. 19

When the water on the downstream side of the weir or 'tail water' rises above its crest (Fig 10), the weir is said to be 'sub-



merged' or 'drowned' instead of being 'free' The discharge of AB 1° found by the ordinary weir formulæ, equations 11 and 12 The discharge of BC is considered as being that of a submerged ornice BC under a head AB, and is found by equation 9 or 10

The same procedure is a

dopted when a sudden full occurs in the surface of a stream owing, not to a weir, but to a lateral contraction of the channel The length l in equation 11 or 12 and the area a in equation 9 or 10 are measured downstream of DE where the contraction occurs. The question whether the stream expands again at FG or continues contracted for an indefinite distance may affect the coefficient to be used, but does not affect the formule. When the fall AB is small compared to BC in the case of a weir, or to BK in the case of a contracted channel, equation 9 or 10 alone is often used. The tail water level, which should theoretically be measured at L (see romarks regarding submerged orifices in the preceding article) is measured at M. The co-efficients for most such cases are imperfectly known, and refinements as to details are unnecessary. See also article 19

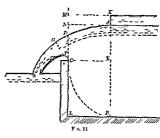
7 Concerning both Orifices and Weirs—With all kinds of opertures small heads are troublesome, not only because of the difficulty in measuring them exactly, but because complications occur, and the co efficients are not properly known

At a werr the water surface always begins to fall at a point A (Fig 11) situated a short distance upstream of the weir Mence, whitever the crest and end contractions may be, there is always surface contraction. The angular spaces between the will and the bed and sides of the channel are occupied by eddies. The full in the surface begins where the eddies begin. From this point the section of the stream proper or forward moving water diminishes, its velocity and momentum increase, and the increased surface fall is necessary to give the increased momentum (art 10). A similar fall occurs upstream of an orifice, though it may only be perceptible when the orifice is near the surface.

The section where the eddies begin will be termed the 'approach

section' It is here that the head should be measured and the velocity of approach observed or calculated, but when, as often happens

with a wer, and generally withan ornice, the sur face upstream of A is nearly level, the head may be observed either at A or up stream of it. It must not be observed down stream of A in some of the older observations on weirs the head

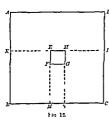


was measured from D to C instead of from A to E, but the coefficients thus obtained are more variable, and it is very difficult in practice to observe the water level at D with accuracy. The section for velocity of approach may be shifted either way from AB provided its area is not appreciably altered

The velocity of approach +, is the discharge, Q, of the aperture divided by the area, A, of the approach section If water enters a reservoir in such a manner as to cause a defined local current towards the aperture, the sectional area of the current may be estimated or observed, and this area not that of the whole cross section of the reservoir, used for determining the velocity of approach If the axis of an aperture is oblique to the direction of the approaching water the component of the velocity of the latter parallel to the axis of the aperture may be taken to be the velocity of approach Equations 8, 10 and 12 cannot be solved directly because, until Q or V is known v and h are unknown It is impossible to find v by direct observation in the case of a pro posed structure or unless the water is actually flowing and even then it is not a convenient process. The usual procedure is to estimate a value for a calculate h, solve equation 10 or 12 divide by A, and thus find a corrected value for i If this differs much from the value first assumed at can be substituted and Q calculated afresh Velocity of approach has very little effect when the area of the approach section is about fifteen times that of the smallest

section of the stream issuing from the aperture, that is for a sharp edged aperture inne or ten times the area of the aperture, and for a bell mouthed orifice fifteen times the area of the orifice. In a weir the height of the aperture is to be considered AE, not DC

In order that the contraction may be complete the margin must be clear for a distance from the aperture extending in all directions to about three times the least dimension of the aperture further extension has no effect. If the ratio of the width of the clear margin to the least dimension of the aperture is reduced to 2 67 and 2 0, the discharge is increased by only about 16 and 50 per cent respectively, so that practically a ratio of 2 75 is sufficient and will be so regarded In a weir the length of crest is usually the greater dimension and the least dimension is then the head AL and not DC Another condition essential for complete crest con traction is that hir shall have free access to the space under the issuing stream. In an aperture in a thin wall with complete con traction air usually has free access unless the tail water rises very nearly to the crest or lower edge when its surging may shut out In a weir with no end contractions the width of the channel, both upstream and downstream of the weir, is very likely, the same as the length of the crest, and air will be excluded unless openings in the sides of the downstream channel are provided to admit it Any want of free admission of air causes the sheet of water to be pressed down by the air above it, the contraction is reduced and various complications may occur. It is also neces sary for complete contraction that the edges be perfectly sharp Any rounding increases the discharge



In Figs 12 and 13 II CD is the loundary of the minimum clear margin necessiry to give full contraction, supposing FIGII to be an orifee, KI CL the boundary supposing it to be a weir, and FILAG supposing it to be a weir with no end contractions. In Fig. 13 LII = IF x 20. The ratios of the areas within these boundaries to those of the apertures are 42 25, 24 38, and 3 75 in Fig. 12 and 8 29, 4 78, and 13 75 in Fig. 13. It is thus clear that of the two

conditions namely, sufficiency of the marginal area to give full

contriction and sufficiency of the area of the approach section to give a negligible velocity of approach, one does not necessarily imply the other. The two matters must be kept distinct. An iclongated aperture, especially a weir, is most likely to have a high velocity of approach and a square aperture, especially an orifice, to have incomplete contraction. Even when the area of the approach



section is very large, it may allow of incomplete contraction in a portion of an aperture if unsymmetrically situated

The co-efficients for apertures in thin walls are known with more exactness than for others, but they are best known for orifices when the contraction is complete, and for weirs either when it is complete on all three sides or complete at the creat and absent at the sides. The co-efficient n for velocity of approach is not very accurately known. Hence very high velocities of approach are objectionable where Q has to be accurately computed from assumed co-efficients, but when r is not very high, that is, when the area A is more than three times that of the smallest section of the issuing stream, Q depends very little on n

The fall in the surface upstream of an aperture, the rise CF due to crest contraction in a sharp-edged wer, and the effect of velocity of approach greatly complicate the theoretical discussion of wer formula

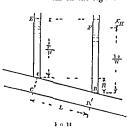
#### SECTION III -FLOW IN CHANNELS

8 Definitions—The 'border,' or 'wet border, L, of a stream is the perimeter of its cross section, omitting in the case of an open stream, the surface width The 'hydraulic mean depth,' is the sectional area A divided by the border Thus  $R=\frac{A}{B}$ . The flow of a stream is 'uniform' when the mean velocities at successive cross sections are equal, that is, when the areas of the cross sections are equal, that is, when the areas of the cross sections are equal.

uniform when all its cross-sections are of equal area. The flow in such a channel must be uniform when it is flowing full. An open channel is uniform when it has a constant bed slope and a uniform cross section. The flow in such a channel is uniform when the water surface is parallel to the bed, but otherwise it is variable. The 'inclination' or 'surface slope' of an open stream is the 'fall' or difference between the water levels at any two points divided by the horizontal distance between them. The 'irrual slope' or 'virtual inclination' of a pipe is the difference between the levels of two points in the hydraulic gradient divided by the horizontal distance between them.

9 Uniform Flow in Channels—When a stream flows over a solid surface the frictional resistance is independent of the pressure, and approximately proportional to the area of the surface, and to the square of the velocity. Thus if f is the resistance for an area of one square foot at a velocity of one foot per second the resistance for an area A and a velocity I' is nearly fAV'. The value of f increases with the roughness of the surface

In the case of a uniform stream open or closed, ACDB (I ig 14) the second term on the right in equation 5 (p 11) vanishes and



the loss of head h in a length L is equal to the full in the surface or in the hydraulic gradient. In an open stream the pressures on the ends AC, LD of the mass of water are equal and the accelerating force is that component of its weight which acts parallel to its axis or WAL h On the assumption that the resistance is entirely due to friction letween the stream

and its channel, the resistance is approximately flll's Since the motion is uniform this is equal to the accelerating force or

$$I^{n} = \frac{II}{J} \quad I^{f} \quad I^{h}$$

But  $\frac{A}{B} = K$  and  $\frac{I}{I} = S$  the surface slope of the stream

$$\frac{\mathcal{W}}{f} = C^{z}$$
 Then  $h = \frac{F^{2}L}{C^{2}L}$  (13),  
or  $\mathcal{V} = C\sqrt{RS}$  (14)

the discharge is

where C is a co-efficient. In the case of a uniform pipe the pressures on the ends have to be taken into consideration, but the resulting equation is the same, S being the hydraulic gradient EF For if  $P_1$  and  $P_2$  are the pressures at A and B, the resultant pressure on the mass ACDB, resolved parallel to its axis, is  $A(P_1-P_2)$  or  $WA\left(\frac{P_1}{P}-\frac{P_2}{W}\right)$  or WA(h-h). The component of the weight parallel to the axis is as before WAh. These two together are WAh. Equation 14 is the usual formula for uniform flow in Streams. It is known as the 'Chezy' formula. Obviously the coefficient C is greater the smoother the channel. The formula for

$$Q = AC \sqrt{LS}$$
 (15)

The theoretical proof just given takes no account of the resist ances due to the internal motions of the fluid, nor of the facts that the velocities at all the different points in the cross section differ from one another, that the mean velocity V of the whole is greater than the mean velocity v of the portions in contact with the border, and that the frictional resistance may not be exactly as V2, nor even as v2 Practically, it is found that the co-efficient C depends not only on the nature of the channel, but on R and S The co-efficient increases with R, that is, generally with the size of the stream It depends also to some extent on S, and perhaps on other factors which will be mentioned It increases with S in pipes of the sizes met with in practice, and in open streams of small hydraulic radius The value of C varies generally between 40 and 120 for earthen channels, and between 80 and 160 for clean pipes The chief difficulty with all kinds of channels consists in forming a correct estimate of the value of C The difficulty is the greater because the roughness of a particular channel may be altered by deposits or other changes

Let an open stream of rectangular cross section have a depth of water D, width W, and velocity V. Let W be great relatively to D, then R is practically equal to D and the fall in a length L is  $\frac{V^*L}{U^*D}$ . Let other reaches of the same stream have equal lengths, but widths 2W', 3W', etc., the longitudinal slopes being flatter, so that D is the same in all. The velocities will be

 $\frac{V}{2}$ ,  $\frac{V}{3}$ , etc, and the losses of head will be  $\frac{FL}{4C^*D^*}$   $\frac{V^*L}{9C^*D^*}$  etc. The total loss of head in two reaches of widths W and 3W is  $\frac{V}{C^*D^*}(1+\frac{1}{n})$ . The loss of head in two reaches, each of width 2W, will be  $\frac{V^*L}{C^*D^*}(\frac{1}{n}+\frac{1}{n})$ . Thus, the loss of head in a reach of

length 2L and width 2W is less than half the loss in an equal length of the same mean width, but in which the width is W for half the length and 3W for the other half. If the streams compared have circular or semicircular sections the difference is still greater. Thus, in conveying a given discharge to a given distance, the advantage as regards fall is on the side of uniformity in velocity.

10 Variable Flow in Channels —When the flow is variable the loss of head from resistances is the same as in a uniform stream, that is  $\frac{V}{C}\frac{L}{L}$ , provided the change of section is gradual and the lengt! L short, so that the velocity and hydraulic radius change only a little, say by 10 per cent, V and R being their mean values. Then, from equation 5 (p. 11) the fall in the surface or hydraulic gradient in the length L is

$$h = \frac{V^2L}{UL} - \frac{V_1^2 - V_2^2}{2g}$$
 (16)

where  $V_1$  and  $V_2$  are the velocities at the beginning and end of the length L. The equation may be written

$$V = C \sqrt{I_h} \sqrt{\frac{h + h_v}{L}}$$
 (17)

where  $h_s = \frac{V_1^2 - V_2^2}{2g}$  This is the equation for variable flow in

streams It is the same is equation 14 (since  $S = \frac{h}{L}$ ) with the addition of the quantity  $h_n$ , which is introduced because of the change in the istima of the water. The quantity  $V_i^{\pm}$  is the square of the means of all the different velocities in the cross section. It ought strictly to be the mean of the squares. In a cross which was worked out, it was found to be 3.3 per cent in excess. But a nearly equal error occurs with  $V_i$ . The quantity  $h_i$  thus represents the change of its time without appreciable error.

If the section of the stream is decreasing,  $V_1$  is less than  $V_2$ , h, is negative, and V is less than it would be in a uniform stream with

the same values of R and S Or, V being the same, the fall h in the surface, or in the hydraulic gradient, is greater than in a uniform stream. This is because work is being 'stored' in the water as its velocity increases. If the section is increasing  $V_1$  is greater than  $V_1$ ,  $h_s$  is positive, and V is greater than in a uniform stream, or V being the same, h is less. Work is being 'restored' by the water. There may even be a rise in the surface or line of hydraulic gradient instead of a fall

Consider any stream AE (Fig 15) in which the sectional areas A and E are equal and the velocities therefore equal, and let the area D be not more

than 10 per cent greater than C Make C and C each equal to C Evidently the quantities h.



F10 15

to the lengths AC, CE will be equal, but of opposite signs, and the total fall in the surface in AC+CE will be the same as if the flow were uniform and the section of the stream were an average between the sections at A and C. The same is true of the length CC and of CC. It does not matter whether the fluctuations in section are due to changes in the width or in the depth, or both. The formula  $V=C\sqrt{RS}$  therefore applies to a variable stream AE if the velocities at both ends of it are equal and the fluctuations moderate, but evidently it does not apply any the better to a short length of such a stream in which the velocities at the ends are not equal. Evidently in such a stream S varies from point to point. It is greater as S is less. S in the formula must be deduced from the total fall.

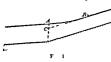
Now let the fluctuations be so great that the revelues must be subdivided before the equation can be applied to them Make F equal to G. The fall in CF+GC is the same as in a uniform stream of section H. The fall in FB+BG is the same as in a uniform stream of section K. The total fall in CG is the same as the sum of the falls in two uniform streams of sections H and K. This total fall is (art 9) greater than that in a uniform stream, having a section equal to the mean of H and K. It will also be seen in section V that if there are any abrupt changes the falls at the contractions are by no means counterbalanced by the rises at the expansions. Thus a variable stream is less efficient than a uniform stream of the same mean section, or in other words, it must have a greater total fall in order to carry the same discharge

This and the result arrived at in article 9 are analogous to other mechanical law Uniformity in speed is best, slight fluctuations are unimportant, but great, and especially abrupt, fluctuations give reduced efficiency

It is clear that the formula  $V=C\sqrt{LS}$  applies to the case last considered if a suitable value is given to  $\widehat{C}$  and S is the slope deduced from the total fall. It even applies approximately to a stream in which the two end velocities are not equal, provided the length is considerable, so that he is small relatively to he It applies to such a case still more nearly if the value assigned to C is such as to take account of the change in the end velocity, C being greater than for uniform flow if V increases and less if it decreases It may not always be easy to say how much C should be altered in such a case, but it may still be highly convenient to use the formula in generalising regarding such a stream, for instance in comparing the discharges for two different water levels or stages of supply in an open stream Thus the formula for uniform flow applies either exactly or nearly to a vast number of cases met with in practice in which more or less approximate uniformity of flow exists 11 Concerning both Uniform and Variable Flow -Pipes are

nearly always of approximately uniform section, and the flow in them nearly uniform, but the sections are seldom exactly equal Open channels are sometimes nearly uniform and, if there is no disturbing cause, the flow is nearly uniform. But in both cases much confusion and error have been caused by applying the formula for uniform flow to variable streams of short lengths or, supposing the short length to be uniform, by carrying the slope or hydraulic gradient observations into variable reaches

Owing to a change, for instance a change of slope, or of section, or a weir, in a uniform open stream, the water may be theired up.

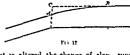


(Fig 16) or drawn down (Fig 17) for a great distance, AI, upstream of the point of change. In these cases the surface slope AI differs from the bed slop and the flow is variable leading up is allo known as

although the channel is uniform. Heading up is allo known as affiliar, or thack water. In all such cases the water surface 11, which would, if the upstream reach had continued without any change, have followed the line 16, has to accommodate itself to

the downstream level at A, and assumes a curve such that the surface-slope changes in the opposite manner to the sectional area. Downstream of

A the flow is uniform. In uniform closed chan nels the section of the stream cannot vary, and if from any cause the



gradient level at any point is altered, the change of slope runs back to the commencement of the pipe

In the absence of any disturbing cause, that is when the flow is uniform throughout, it is obvious from equations 14 and 15 that in an open stream an increase of discharge is accompanied by a riso of water level and the error. The same is the case in a nariable stream. In uniform flow in an open stream, the dimensions and slope of the channel being known, the discharge can be found if the water level is given and the trers. The surface slope is the same as the bed slope. In variable flow the surface slope into the very different from the bed slope, and it is necessary to know the water levels at two points in order to find the discharge, or to know the discharge and the water level at one point in order to find the water level at the other point.

A large stream, whether in an open or closed channel, has an

advantage over a small one both in sectional area and in velocity

For as A increases R usually increases, and with it C If the slopes are equal Q is much greater for the larger stream Q is the same for both, S is much less, that is the loss of head is less, for the larger stream. This applies to variable as well as to uniform streams A fire hose of diameter D is fitted at its end with a tapering 'nozzle' whose least diameter d is perhaps  $rac{D}{3}$  , so that the velocity of the issuing jet is nine times the velocity in the hose. If the hose were made of diameter d the loss of head in it would be greatly increased, and more pressure would le required to drive the water through it. The size is limited by convenience in handling If part of the hose stretches under pressure, so that the flow is variable, there is a gain all the same Again, let Fig 16 represent an irrigation distributary with dis charge Q, the bed slope downstream of A being the same as upstream, so that BC is the water level To supply water to high ground near A a dam may be made, raising the surface to I A, and enabling a discharge q to be drawn off at A, whereas a small

branch made for this purpose from B, with a slope such as BA,

might discharge hardly any water

The theoretical proof (art 1) regarding the variation of

ressure with depth depended on the assumption that the velo etities at all points in a cross section were equal. Though they are not equal, it is found in practice that the law holds good

12 Relative Velocities in Cross section -The velocity at any point in a straight uniform stream flowing in a channel is, generally speaking, greater the further the point is removed from the border The border retards the motion of the water next to it, and the retardation is thus communicated to the rest of the stream In a pipe of square or circular section the velocity is greatest at the axis, and thence decreases gradually to the border. In an open channel the form of cross section varies greatly in different streams, and the distribution of the velocities varies with it The distribution of velocities in the cross section of a variable stream, provided the section of the channel changes gradually, is practi cally the same as if the flow were uniform. The distribution depends on the form of the section, and is not likely to be appreci ably affected by the fact that the whole velocity is slowly changing In all cases the velocity changes more rapidly near the border (probably very rapidly quite close to the border, but of servations cannot be made there) and less rapidly towards the centre of Thus all velocity curves are convex downstream Nothing in this article relates to the velocities at or near to abrupt changes of any kind 13 Bends -In flow round a bend the distribution of velocities

13 Bends—In flow round a bend the distribution of velocities is modified, the line of greatest velocity being shifted, by reison of the centrifugal force, towards the outer side of the bend, and all the velocities on the outer side being increased while those on the inner side are reduced. The loss of head from resistance in a bend is greater than in the same length of straight channel. The additional resistance is chiefly caused by work done in redistributing the velocities consequent on the transfer of the maximum line from its normal to its new position, and in the fresh redistribution after the bend is passed. This fresh redistribution and the strainteneously, so that the normal distribution is not restored till some distance below the termination of the bend. Besides these resistances it is probable that wherever the distribution is almost all normal, no matter whether any redistribution is in actual progress or not, the resistance is greater, owing to the high velocities near the border on the outer side of the lend

For a given channel and given radius of bend the total resist ance or loss of head caused by the bend is not proportional to its length because, however long it may be, the redistribution has to be effected only twice If the lower half of a bend is reversed in position, thus forming two curves, the loss of head in the whole bend is greater than before, because the redistribution of velocities has now to be effected in the opposite direction, doubling the work of this kind done before No abnormal distribution of velocities occurs upstream of a bend unless, as in the case of an earthen channel, the section of the stream is also abnormal a little upstream of the bend The laws regarding bends, both in pipes and open channels, are imperfectly known Recent experiments on large pipes show that, for a given angle subtended by a bend, a small radius of bend is, down to a certain limit, preferable to a large radius. This is contrary to what has hitherto been believed Flow round a lend may be either uniform or variable. If the section of the stream is the same as in the straight reaches, the slope of the surface or gradient must be greater, and there will be heading up in the unstream reach

# SECTION IV -- CONCERNING BOTH ALFRTURES AND CHANNELS

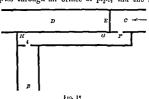
14 Comparisons of different cases -The difference between the case of an aperture and that of a channel depends on the nature of the work done It is a difference of degree and not of kind In flow through a small orifice in the side of a large reservoir a mass of water which is at rest has a velocity impressed on it The motive power is the pressure of the water due to the head, and the work done consists almost entirely in imparting momentum to the water, friction and resistance being unimportant In uniform flow in a channel a mass of water slides, under the influence of gravity, with a constant velocity The motive power is that component of the weight of the water which acts parallel to the surface or line of gradient, and the work done consists in overcoming friction and the resistance caused by internal move ments No fresh momentum is imported. These are the two extreme cases In flow through some kinds of apertures there are considerable resistances and in variable flew in channels much of the work may consist in the imparting of momentum two extreme cases thus merge one into the other ! Most cases of

<sup>2</sup> Fig 10 p 16 may be regarded as a case of variable flow

abrupt changes in channels, dealt with in articles 17 to 21, occupy an intermediate position

Comparing channels or apertures which entirely surround the flowing stream with those which leave the water-surface free, it will be found that the latter are far more elastic than the former In the case of the pipe GEF (Fig 5, p 9) and the orifice C (Fig 9, p 14), if it is desired to double the discharge, it is necessary to quadruple the head or the hydraulic gradient. In either case a very great rise in the water level AB is required But for a weir, since Q is roughly as  $H^{\frac{3}{2}}$ , in order to double Q it is only necessary to increase H by some 60 per cent. For an open channel with vertical sides the discharge-recollecting that C increases with R-is doubled by increasing the depth about 50 per cent The above comparisons do not of course take exact account of variations in the co efficients For an open channel with sloping sides the discharging power may vary very greatly for a quite moderate change of water level When the changes in the conditions governing the flow are slight, so that the co efficient is practically unaltered, the changes in the discharge are as follows a change of 1 per cent in the head over an orifice or in the slope of a channel changes the discharge 5 per cent , a change of I per cent in the head on a weir or in the sectional area of a stream changes the discharge 1 5 per cent

A 'module' is an arrangement by which it is sought to ensure a constant discharge of water from a fluctuating source of supply Generally it is a machine which automatically alters the size or position of an aperture as the water level varies. Some modules are imperfect, and in such cases, having regard to the preceding paragraph, it is clearly best that the water to be delivered should pass through an orifice or pipe, and the surplus over a weir or



irplus over a woir or through an open channel In Footes modulo (Fig. 18) a gate E, regulated at intervals by hand, causes the water level in the canal at C to be nearly constant, and higher than at D. By an orifice I water flows into the

tank I I, and on to the branch AI, the surplus passing over a

weir GH. The regulation is better the longer the weir, but it would be improved by a parranging the gate I that the water would flow ever it instead of under it.

I send the water in a casal is steely, an outlet consisting of an order of facels is estill in the filter god, give a constant distribute if the branch channel is liable to be altered. If it is enlarged, its water level falls, and thus the bead at the outlet is increased. The limit is hot revoked until there is a free full

15 Special Conditions affecting Flow —The condition of water, as for instance its temperature or the art and of suspended matter which it contains, by an some cases an effect on the flow. A rise in the temperature of water probably causes an increase in the discharge, while an increase in the suspended matter causes, for flow in channels, a decrease 1 it its seems that apprecial bechanges in the discharge are caused only by great changes in the conditions and scarcely even then unless the channels or apertures are small and the velocities also low.

For velocities under six inches per second the frictional resist ance of water flowing over a solid is not as  $I^{r_0}$ . For velocities of one such per second and less it is nearly as I' At very low relocates the nature of flow in pipes is essentially different from that at ordinary relocates. For any given pipe there is a certain 'entical velocity' For velocities lower than this the motion is in parallel filaments, I' sarres nearly as S and as I' and increases with the temperature of the water. With pipes whose diameter was 03 inch or less, I, when below the critical velocity, was found to be trebled as the temperature rose from 0° to 45 Centigrade With larger pipes some increase occurs. When the velocity in a pipe rises to the critical amount, a very rapid or even sudden change occurs, the motion becoming first sinuous and then eddring Reynolds, who made investigations with very small pipes, concluded that the critical velocity was higher the smaller the pipe. Thrupp 1 states that with pipes having a hydriulic radius of two inches and more the critical velocity increases with the hydraulic radius, and that there is a similar law for open streams, but no details of his observations have been published. It is not known how flow through apertures is affected, if at all Experiments made by Shaw 2 with very small bodies of water—he used films whose thickness did not exceed  $\frac{1}{4}$ 0 of an inch—tend to show that the water immediately adjoining the

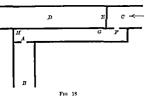
L gineering vol. lxxii p 834 and Min Proc Inst C L, vol exlvii Linguisering vol 1xiv p 00 vol 1xv p 444 vol 1xvii p 28

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E gineering vol. lxxii p 834 and Min Proc Inst C L vol. cxlvii
 Eng neering, vol. lxiv p 90 vol. lxv p 444 vol. lxvii p 28

30 HYDRAULICS

channel moves in parallel lines, and that in going further away from the border sinuous or eddying motion takes place suddenly

16 Remarks -The solution of a numerical question in Hydraulies by means of formulæ may be either direct or indirect When the conditions are given and the discharge, say, is to be found, it is only necessary to look out the proper co efficient and apply the formula But frequently the problem is inverted and consists in finding a suitable set of conditions to give a particular result This is especially the case when channels or structures have to be designed In many cases a direct solution cannot be obtained by inverting the formula, either because its form is unsuitable—an instance of this has been given in article 7-or because the co efficients are not known until the conditions are determined It is often necessary to obtain an indirect solution by assuming a certain set of conditions, calculating the discharge or other quantity sought, and, if it is not what is desired, making alterations in the assumed conditions and calculating afresh order to facilitate calculations which would otherwise become very tedious, numerous working tables are given By their use work is vastly reduced

Both in apertures and channels the coefficients in the formulæ vary more or less as above stated. Various attempts have been made to modify the formulæ (putting for instance  $H^n$ ,  $R^n$ ,  $S^n$ , instead of  $H^1$ ,  $R^n$ ,  $S^n$ ) in such a way as to make the co-efficient constant. Such formulæ either have a restricted range or clse the functions of H, R, and S involved are very inconvenient. It is far better to adhere to the simple induces in common use and to uccept the variations in the co-efficients.

Although for discharge computation one should avoid complex conditions such as incomplete contraction, small heads, high velocity of approach or variability of flow, jet in practice an engineer is frequently compelled to accept such conditions, and some attention will be given to methods of dealing with them

In many of the more complicated cases (such as some considered in the following section and in chap this) it may be difficult to arrive at any exact results by calculation but it may still be most useful to recognise the existence of the phenomena referred to and to take note of their general effects

### SECTION V -- ABRUPT AND OTHER CHANGES IN A CHANNEL

17 Abrupt Changes—Any change in a channel whether of sectional area or direct in, and whether or not there is a bifur cition or junction, which is so sudden as to cause contraction or eddies is called an alrupt change. At an abrupt change the first term on the right in equation 5 (p. 11) is omitted. It would be small because of the small length of stream considered, and owing to the stream being bounded partly by eddies and changing rapilly in form, it would be difficult to assign values to the quantities I and C. The second term only is used. Thus the formula are analogous to, or identical with, those for aper tures. In fact alrupt changes include submerged weirs and (in certain respects which will be specially noted) other apertures.

At a rule t changes there are special losses of head, owing to work being expended on eddies. The length and violence of the dedies at an enlargement are much greater than at a corresponding contraction (Figs. 3 and 4, p. 5) and the loss of head is consequently much greater. At a contraction the pressure at K, L is slightly greater, and in the case of an open stream the water level slightly higher than in the flowing stream. These remarks a ply also to orifices and weirs with which there is velocity of approach. At an expansion the conditions are the reverse. The loss of head at an abrupt change of any kind is most important when the velocity is high, it can seldom be calculated with exactness, and often can only be roughly estimated.

18 Abrupt Enlargement.—At an abrupt cultigreement (Fig. 1) the loss of head due to the enlargement can be found theoretically by assuming that the intensity of pressure on AC, PD is the same as at AE. If EF,  $A_n$  be the velocity and sectional area at AI,  $P_1$  the pressure on its centre of gravity, and  $V_1$ ,  $A_1$ ,  $P_2$  similar quantities at EF. The force  $A_1(P_2-P_1)$  causes the velocity to be reduced from  $P_1$  to  $P_2$ . In a short time,  $t_i$  the fluid AEFE comes to ABFE. Since the momentum of ABFE is unchanged the change of momentum in the whole mass is the difference between that of ABEA and that of EFFF, and that is

If 
$$Qt\left(\frac{V_1}{g} - \frac{V_2}{g}\right)$$

where  $H^*$  is the weight of a cubic foot of water and Q is the discharge per second. This change of momentum is equal to the impulse  $A_1(P_1-P_1)$  I, therefore

or 
$$\begin{split} A & (P_1 - P_1) = \frac{IVA_1V_2(V_1 - V_2)}{g} \\ \frac{P - P_1}{IV} \approx \frac{V_2(V_1 - V_2)}{g} \end{split}$$

But  $\frac{P_1-P}{m}$  is the fall h in the surface or line of gradient, there

fore from equation 5 (p 11)  $h + \frac{P_2 - P_1}{W} = \frac{V_1 - V_2^2}{2g},$ 

subtracting the preceding equation from this
$$h = \frac{V_1^* - V_2^* - 2V_1V_2 + 2V}{2g} = \frac{(V_1 - V_2)^*}{2g}$$
(18)

or the loss of head is the head due to the relative velocity of the two streams In order to simplify the calculation it has been assumed that the stream flows horizontally, that is that the centres of gravity of the sections AL, EF are at one level but the loss of head due to the enlargement is the same in any case The pressure in the eddy has been found to be really less than in the jet, so that the assumption made is incorrect, and the formula has been found in practice to give incorrect results for small pressures and velocities, but for other cases it is fairly accurate

Equation 18 is of the same form as the equation giving the loss by shock, in a case of impact of inelastic solid bodies, and the loss of head due to an abrupt enlargement is often called 'loss by shock though there is not really any shock, the stream always expanding Lradually

If there were no loss of head in the length AE there would be a use of  $\frac{V_1 - V_2^*}{2\sigma}$  in the surface or hydraulic gradient

pipe the loss of head  $\frac{(V_1-V_2)^2}{a}$  is always much less than  $V_1^2 - V_2^2$ , and there is actually a rise whose amount is approximately  $\frac{V_2(V_1 - V_2)}{g}$  (18A)

This proof is usually given only for a pipe but it clearly applies to an open stream if there is no rise in the surface. If there is a rise the pressure on the wave QI, supposing Fig 4 to be a vertical section, is not P but Pa (the atmospheric pressure) and the loss of head is greater thin  $\frac{(I_1-I_1)^2}{2g}$  Moreover, the section usually changes not only in size but in form and the redistribution of

the velocities absorbs more work. The rise in the water level is thus generally slight, and it cannot usually be calculated accurately

When an enlargement is immediately succeeded by a contraction so as to cause a deep recess the water in the recess has little or no forward motion, and the flow is practically the same as if the recess did not exist

19 Abrupt Contraction —At an abrupt contraction in a pipe (Fig 3) it is necessary, if exact results are required, to calculate the sectional area at the vena contracta EF and find the velocity  $V_1$  at that section Then,  $V_1$  being the velocity at ST, the fall in the hydraulic gradient, due to increase in the velocity head from ST to EF, is  $\frac{V_1^* - V_1^*}{2g}$ , but some head is lost owing to friction and to the eddies at K, L The expansion of the stream from EF to MN causes loss of head, which may be calculated as explained in the preceding article. The case of an open stream is analogous, but the whole fall due to loss of head and increase of

is used

A particular case of abrupt contraction occurs when a stream issues from a reservoir. There is a fall in the surface or hydraulic gradient. Most likely the velocity of approach is negligible. If so the fall, in the case of a pipe can be calculated without finding the area kF (chap v art. 1), and, if not the above procedure can

velocity head is considered together (art 6) and equation 10 (p 14)

be adopted For an open stream equation 10 is to be used

At a local contraction the channel contracts and expands
again, but not necessarily to the same size For an open channel
equation 10 is used For a pipe there are various empirical formula
for local narrowings, all involving the factor  $\frac{V^2}{2n}$  (chap v art 6)

20 Abrupt Bends, Bifurcations, and Junctions
—An abrupt bend (Fig. 19) is called an 'elbow
The contraction causes a local narrowing of the
stream It has been found in small pipes that, with
an elbow of 90°, the head lost is very nearly 2',

Judging from analogy and from observation it is probable that this is nearly true for any pipe and also for an open stream. For elbows of other angles the relative loss of head is known for small pipes (chap a art 6) and it may be assumed that for other channels it is roughly the same.

At a bifurcation (Figs 20 and 21) the stream entering the

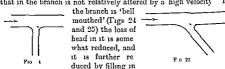
branch may be regarded as flowing round a bend whose outer boundary is shown by the dotted lines In the main channel below the

branch there is an en largement (art 18) Let  $\theta$  be the angle made by the centre lines of

the branch and of the main channel upstream of it When θ is 90° or thereabouts the whole head due to the velocity is lost, and there is a fall in the surface or hydraulic gradient of the branch of about the same amount as there would be if it issued from a reservoir But if V is high the absence of contraction at A does not compensate for the excessive contraction at B, and the fall is increased, or the discharge of the branch diminished When  $\theta$  exceeds 90° the component of V resolved parallel to the axis of the branch may be regarded as velocity of approach, the discharge being increased accordingly. It is not known for what angle the velocity of approach compensites for the greater contraction as compared with that in the case of a reservoir The angle differs with the velocity and probably with

the width of the branch, and is perhaps generally not much greater than 90° the arrangement shown in Figs 22 and 23, the losses of head both in the branch and in the main stream are reduced and

that in the branch is not relatively altered by a high velocity



the portions shown in dotted lines, thus doing away with eddies Figs 20 to 25 represent junctions if the stream is supposed to flow in the directions opposite to those of the arrows The losses of head are very much the same as in the corresponding cases of hifurcations

21 Concerning all Abrupt Changes -The 'limits' of an abrupt

change are those of the peculiar local flow caused by it. The upstream limit is, in Fig. 4, at I B7, in Fig. 3, just as with a wear and certain kinds of orifices (art. 7), at ST. In the other cases it is where the edding or curvature begins. In all cases eddies exist in the stream itself for some distance downstream of an abrupt change. The downstream limit is where these eddies have become reduced. They may not cease altogether for a long distance.

In the reach downstream of an abrupt change the flow, except for eddying and probably disturbance of the relation to one another of the various velocities in the cross section, is normal, and the water surface or hydraulic gradient takes the level suited to the discharge just as if no abrupt change existed. Within the limits of the abrupt change there occurs the fall or rise discussed in the three preceding articles. Thus the level of the surface or hydraulic gradient at the downstream limit of the abrupt change governs that at the upstream limit, and this again affects the slope in the upstream reach in the uniteriam reach in the upstream reach is normal. There is nothing to affect it until the abrupt change actually begins. (Cf. also Bends, art. 13). Thus, at all changes, whether of sectional area or direction of flow, and whether strictly abrupt or not, the effect on the hydraulic gradient or slope is wholly upstream, but eddies and disturbance of the velocity relations are wholly downstream.

It follows that discharge observations in which the mean velocity of the whole stream is to be deduced from observations taken, say, in the centre only, should not be made within a considerable distance downstream of an abrupt change, but may be made a short distance upstream of it

Any alteration which makes a change less abrupt reduces the loss of head. This has been seen in considering bends, elbows, and bifurcations. Regarding changes of section an instance would be the rounding of the edges of the weir in Fig. 10. But in all cases, if the eddies are replaced by solid matter, the flow is very much as before. Though rounding is caused, the size of the aperture is reduced. The friction on the solid is added, but the maintenance of the eddy is subtracted. Wherever eddies are referred to the term may be considered to apply also to a solid of the form of the eddy.

36 HYDRAULICS

### SECTION VI -- MOVEMENT OF SOLIDS BY A STREAM

22 Definitions -- When flowing water transports solid sub stances by carrying them in suspension, they are known as 'silt,' when by rolling them along the channel they are termed 'drift' The weight of silt present in each cubic foot of water is called the 'charge' of silt Silt consists chiefly of clay, mud, and fine sand, drift, of sand, gravel, shingle, and boulders When a stream obtains material by croding its channel, it is said to 'scour' When it deposits material in its channel, it is said to 'silt' Both terms are used irrespective of whether the material is silt or drift The difference between silt and drift is one of degree and not of kind Material of one kind may be rolled and carried alternately

23 General Laws -If a number of bodies have similar shapes, and if D is the diameter of one of them and V the velocity of the water relatively to it, the supporting or rolling force is theoretic cally as V'D2, and the resisting force or weight as D3 If these are just belinced D varies as V. or the diameters of similarly shaped bodies which can just be supported or rolled are as V' and their weights as V. From practical observations, it seems that the diameters do not vary quite so rapidly as they would by the

above law, the weights being more nearly as V.

If a stream has power to scour any particular material from its channel, it has power to transport it, but the converse is not always true If the material is hard and compact the stream may have

for more difficulty in eroding it than in retaining it

It has long been known that the scouring and transporting power of a stream increases with its velocity Recent observations made by Kennedy have shown that its power to carry silt decreases as the depth of water mereases 1 The power is probably derived It is prevented from sinking by the upward components of the eddies If V is the velocity of the stream and D its depth, the force exerted by the eddies generated on one square foot of the hed is greater as the velocity is greater, and is, say, as I'm But, given the average charge of silt, the weight of silt in a vertical column of water whose base is one square foot is as D. Therefore the power of a stream to support silt is as  $V^n$  (say as  $V^n$ ) and inversely as D

The power of water to move drift is probably as I?, and the Min Proc Inst C1 , vol exix

depth does not a "wist. It has constitues because of the increased of the time increased security power, because of the increased pressure but the is not set. The increased pressure due to depth acts or both the transact and downstrian subsect a body. It is moved only by the pressure due to the velocity. It is impossible to construct an equation which shall include both suspended and rolling matter, because the proportions in which they exist an not known.

It is sometimes supposed that the inclination of the bed of a stream when high, facilitates seour, the material rolling more easily down a steep inclined plane. The inclination is neath always too small to have any appreciable direct effect on the rolling force. In fact the bed is generally more or less undulating, and the drift may be moving either uphill or downhill. The inclination of the surface of the stream of course affects its velocity, and this is the only real factor in the case.

A stream of given velocity and depth can only carry a certain charge of silt. When it is carrying this it is said to be fully charged. In this case, if there is any reduction in velocity, or if any additional silt is by any means brought into the stream, a deposit will occur (unless there is also a reduction of dipth) until the charge of silt is reduced again to the full charge for the stream. The denosit may, however, occur slowly, and extend over a considerable length of channel. If a stream is not fully charged, it tends to become so by scouring its heal. A stream fully charged with silt cannot scour silt from its channel, but its power to move drift is, perhaps, unaffected by its being charged with silt.

It is not known how the full charge is affected by the nature of the sit. The specific gravity of fine mind is not much greater than that of water, while that of sand is about 1.5 times as great. If two streams of equal depths and velocities are fully charged, one with particles of mind and the other with equally sized particles of sand, the latter will sink more rapidly and will have to be more frequently thrown up. They will probably be fewer in number, but in what proportion is not known.

In the 'Inundration Carala,' so called because they flow only when the rivers or in flood, fiel from the rivers of Northern India, the site entering a canal usually context of said and until "The sandy portion, or most of it, is deposited in the head reach of the canal, forming a wedge-shaped mass, with a digith of perhaps two or three feet at the head of the canal, dimini him to rive at a point a few miles from the head. Beyond this point the water,

charged with mud and perhaps a little and, usually flows for many miles without any deposit occurring, although there are frequent reductions in the velocity caused by the diminutions in the size of the stream as the distributaries are tallen off, and sometimes also by reductions in the gradient. The absence of further deposits mexplicable till the discovery of Kennedy's law, is due to the fact that the depth of water diminishes as well as the velocity Many of the channels were constructed long upo by the natives, and they seem to have learned from experience to give the channels such widths that the depth of water decreases at the proper rate

It is a common practice to so reduce the velocity of a stream that silting must take place. The object may be either to 'warp up' certain localities by silt deposit or to free the witer from silt, and thus reduce the deposit in places further down When the velocity of a stream is arrested altogether, as it practically is when a stream flows through a large reservoir, the whole of the silt will deposit if it has time to do so, that is, if the reservoir is large enough. Low lying and marshy plots of ground may be sitted up, and rendered healthy and culturable by turning all-bearing stream through them. In order to pravent deposit in the head of a canal the water may be made to pass through a 'silt-trup' or large natural or artificial basin, where the velocity is small, or the supply may be drawn from the upper layers of the river water (art. 24)

Silting and seouring are generally regular or irregular in their action according as the flow is regular or irregular, that is, according as the chunnel is free or not from abrupt changes and eddies In a uniform canal fed from a river the deposit in the head of the canal forms a wedge shaped mass, as above stated, the depth of the deposit decreasing with a fair approach to uniformity. Salient angles are most hable to scour, and deep hollows or recesses to silt. Eddies have a strong scouring power. Immediately downstream of an abrupt change scour is often severe

Most streams vary greatly at different times both in volume and velocity and in the quantity of material brought into them Hence the action is not constant. A stream may silt at one season and scour at another, maintaining a steady average. When this happens, or when the stream never silts or scours, appreciably it is said to be in "permanent regime.

Wases, whether due to wind or other agency, may cause scour, especially of the banks. Their effect on the bed becomes less as

thed other water is reas only a disk role concallegether at a depth of 21 feet, as has been supposed. Salt water posicious appropriate girls.

ap verefpre peats gest.

24 Detributine of filt Charge — 5 received his are strongest reactive held, the charge of siter of specially increase towards the best the teste of increase agree greatly. Three multiparing a lowage stepparity, the charge is probably nearly a great near their stacks as closed on. Sand is bear, and is offerer instead than carried. When carried it is as all in much greater proper trongest the less. Materials with as beat fers, do not generally meeting halves the less of Aprels sheet fers, do not generally meeting halves the less of a special stream may be moung duffe. The ratio of the suit of any and the suitage to that at the bed this varies from a stace to be 1 per body more such the rate of available forms of stace to be 1 per body more institution in any particular stream can only be as grained by observation, or by expendice of similar stream. It is a inviter of great practical importance, as affecting the best bed feed for a branch taking off from the stream. The results of observations show considerable from the stream. The results of observations show considerable discrepancies, even when averaged, and in lividual observations discriptiones, even when averaged, and in firming meet values are; great discriptions. In some raters 10 to 17 feet deep the silt charge has been found to increase at the rate of about 10 per cent, for each foot in depth below the surface. In other, with depths ranging up to 16 feet, the silt charge at about three fourths or four fifths of the full depth has been found to bear to that near the surface a ratio varying from 11 to 2

## SICTION VII -- HYDRACTIC OBSERVATIONS AND COLLECTIONS

25 Hydraulic Observations—It is frequently necessary in Hydraulic Engineering to observe water levels, dimensions of streams, and velocities, and from these to compute discharges. The object of a set of observations may be either simply to ascertain, say, the discharge in a particular instance, or to find and record the co-efficients applicible to the case, so as to enable other discharges under similar conditions to be calculated. Observations of the latter class, when extensive, are usually termed 'Hydraulic Experiments'. A consideration of the instruments and methods adopted in Hydraulic Observations may be strictly a matter of Hydraulic Engineering, but it is necessary to include it in a general manner in a Treatise on Hydraulics, both because

the principles involved in such work are closely connected with the laws of flow, and also in order that proper estimates may be formed of the errors which are possible and of the reliability of the results which have been arrived at by various observers 1

In making observations accurate measurements of lineal dimen sions, depth, and water levels are necessary, as well as accurate The number and duration of the observations should be sufficient to eliminate the effects of the irregular motion of the water, and bring out the true average values of the quantities sought for Owing to imperfections in these matters, or in the instruments used, errors of various kinds may occur These are known as 'observation errors' They may balance one another more or less, but are hable to accumulate in one direction in a remarkable manner Care in observing, as well as sufficiency in the number of observations, are therefore essential points An error in measuring length or time has, of course, a greater relative effect when the amount measured is small. In a channel the fall in the surface or hydraulic gradient is often a small quantity, and thus in slope observations the error is often large. With an aper ture under a small head the error in observing it may be serious It has been shown by Smith 2 that, even in the careful experiments made by Lesbros on orifices, the co efficients were probably affected by such causes as the expansion and contraction of the long iron handles attached to the movable 'gates,' and to the bending, under great pressure, of the plates forming the orifices Besides quantities which can be actually measured there are conditions which can be observed but may be overlooked, such as a slight rounding of a sharp edge, the chinging of some portion of the water to an aperture when it is supposed to be springing clear, or the occurrence of a deposit in a channel Such matters not always very perceptible may have considerable effects on the flow

Again, there are conditions which cannot be ascertained, and assumptions are made regarding them It has, for instance, been assumed that a local surface slope too small to be observed as the same as the observed slope in a great length, or that the diameter of a pipe, measured at only a few places, is constant throughout Lastly, there are some things very difficult to describe, such as the degree of sharpness of an edge, or of roughness of a channel Thus there is often, in accounts of experiments, a defective or erroneous description of the conditions which existed my be termed 'descriptive error' In some cases it has been 1 Details will be given in chap viii " Hadraulies, char in

very great Its effect is similar to that of observation error, and the line between the two cannot easily be drawn

When the quantity whose law of variation is sought depends on several conditions which vary together, it is often difficult to determine the effect of the variation of any one condition alone As far as possible observations should be made with only one condition varying at a time Generally, observations at one site are kept distinct from those at other sites, but if the conditions of different sites are nearly similar, it is legitimate to combine observations at different sites. In such a case, care should be taken that the effect of any slight or accidental dissimilarity in the sites will not affect any one set of values, but will be distributed throughout all It would, for instance, be undesirable to have all the low water observations at one site and the high water observations at another

A series of observations containing a source of error may show results quite consistent with one another, and may be of great use in bringing out certain laws. The well known weir experiments of Francis and of Fteley and Stearns give results which are consistent, and have long been accepted as practically correct, but when they are compared with the later results of Bazin certain discrepancies appear, and it is clear that one or the other set of experiments contains some error.

Detailed accounts of Hydraulic Experiments do not of course, find a place in a textbook References to the chief works on such experiments have already been given (p 7) but special points will

be noticed whenever necessary

26 Co efficients — From the causes above stated the co efficients, or other figures, arrived at by various observers frequently show grave discrepancies. This is especially the case with the older experiments. In the more recent ones the discrepancies have been reduced.

The 'probable errors' of coefficients have in some cases been estimated by those who have investigated them. The meaning of this may be explained by an example which will be made to include all kinds of errors. Let a weir have a crest 1 foot wide, sharp edges, and a head of 1 foot. Suppose the coefficient arrived at is 500, and that it is estimated that the observation error may Probably be 1 per cent either way. Then 1 per cent is the probable error, and the value of the coefficient is as likely to be between 606 and 594 as to be outside of these limits. But there may also have been descriptive errors connected with, say,

the width of the crest or sharpness of the edges and the real probable error may be much greater than 1 per cent Finally, if the co efficient is applied to a weir, over which water is actually flowing, there may be again observation error in measuring the head Sometimes these different errors balance one another, but sometimes, as before remarked they all accumulate in one direction

The coefficients for different cases contain probable errors of very different amounts. For sharp edged apertures under favour able circumstances, the probable error is only about 50 per cent. For channels and especially for pipes owing chiefly to the causes above indicated (arts 9 and 11) it may easily be 5 or 10 per cent.

Although in the above instance the final operation of observation introduces an additional error, complete observation is much better than calculation. If no coefficient had been assumed at all, but the discharge of the stream carefully observed, as well as the head on the wear, then both the discharge and the coefficient for that particular case would have been obtained in the bist possible manner.

The results of individual experiments nearly always show irregularities, that is when plotted they do not give regular curves. The usual method is to draw a regular curve in such a manner as to average the discrepancies and correct the original observations. Most published co efficients have been obtained in this manner.

When an experimenter obtains a series of co efficients for any particular case, he often connects them by an empirical formula involving one or two constants. This has been done by Brain and Kutter for open channels, and by Iteley and Stearns, I runers and Brain for certain kinds of weirs. What the engineer really needs and uses is a table of the co efficients, but the formular may be useful in finding a co efficient when a table is not at hand or in finding its value for cases intermediate between those given in the tables or outside the range of the observations. This last practice must, however, be adopted with caution and within narrow limits.

Further experiments are required in all branches of hydraulies A feature in future experiments will no doubt be the increased use of automatic and self recording methods, electric communications, and photography.



The co efficients given, except for conical tubes, are approximate and average values, further details being given in the succeeding articles The length of a tube must not exceed three times the diameter, otherwise the co efficient is reduced, owing to friction and the tube becomes a pipe A tube generally has its axis hori zontal, but may have it in any direction. If the lengths of the cylindrical tubes (Figs 28 and 29) are reduced till the jet springs clear from the upstream edge, the co efficients change to the values shown for Figs 25A and 30 The length at which the change takes place may for a very great head be two diameters or more, but is generally less than one diameter The cross sections of all the tubes are supposed to be circular, but the co efficients apply nearly to square sections and to others differing not greatly from circles and squares Thus 'cylindrical' includes 'prismatic,' and similarly with the others In the case of an elongated section, 'diameter' is to be understood as 'least diameter'

For orifices up to a foot in diameter, metal edges filed sharp should be used, if full contraction is required. For larger orifices wooden edges can be made sufficiently sharp. These remarks apply to all kinds of orifices in which the edges are supposed to be sharp, that is to all except bell mouths, though with a convergent conical tube the effect of want of sharpness is probably small, the final contraction occurring outside the tube

In experiments made by Mair and Simpson's with circular orifices 1 to 3 inches in diameter in thin metal plates it was found that a hardly per ceptible rounding of the edge caused in one instance (the diameter is not stated) an increase in the discharge of about twenty per cent, but this increase seems excessive, even if the diameter was only an inch

The co efficient of discharge does not generally alter much as the head varies, so that, neglecting the effect of velocity of approach, the discharge through a given orifice under different heads is nearly as  $H^2$ . In order to double the discharge H must be quadrupled. If the head is doubled the discharge is increased in the ratio of about 14 to 1

To facilitate the working out of problems, the theoretical velocities corresponding to various heads are given in table 1. V can be found from H or H from V.

2 Measurement of Head — Upstream of an orifice there may be a vortex in the water, or, when the velocity of approach is high,

<sup>1</sup> Minutes of Proceedings of the Institution of Civil Eigineers vol

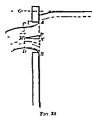
a wave or heaping of water where it strikes the wall, and the head should be measured a short distance upstream from such rortex or water If the part of a reversion adjoining an orifice is closed (Fig. 33) the head may be measured at J, but if the length of the closed portion is more than thrice its least dismeter, it is necessary to fin I the lose of lead in it, treating it as a pipe



45

Smith states that for an orifice in a

thin will the head should probably be measured to the centre of gravity of the year contracts. The matter seems to admit of no doult, and the rule should apply to all kinds of orifices in which there is contraction. It is at the sens contracts and not elsewhere that the theoretical velocity is \-gH In a bell mouthed orifice



in a horizontal wall the head would be measured to the 'discharging side' of the orifice, and the jet from an orifice in a thin horizontal wall issues under the same conditions, except that friction against the sides is removed a small head the set from an orifice in a thin vertical wall may drop appreci ably in the distance PM (Fig. 34), and the true head, that at M, is not the same as at P, the centre of the orifice Nearly all co-efficients have been obtained from orifices in vertical walls under considerable heads, so that it

has made no difference how the head has been measured, but in applying these co-efficients to orifices in other

positions the head should be measured to the vena contracta

3 Incomplete Contraction - The contrac tion in an orifice with a sharp edge may be partly suppressed by adding an internal projection AB (Fig. 35), extending over a portion of the perimeter of the orifice traction is then said to be 'partial' If the length AB is not less than 1.5 times the least



diameter of the orifice, the co-efficients for orifices in thin walls are, according to Bidone-

For a rectangular ornice 
$$c_p = c \left( 1 + 152 \frac{S}{P} \right)$$
 (20),

For a circular orifice  $c_p = c \left( 1 + 128 \frac{S}{p} \right)$  (21),

where c is the co efficient of discharge for the simple orifice, P its perimeter, and S that of the portion on which the contraction is suppressed Partial suppression may be caused by making one or more of the sides of an orifice flush with those of the reservoir The above formulæ were obtained with small orifices and heads under six feet. They are not applicable when  $\frac{S}{p}$  is greater than

 $\frac{1}{4}$  for a rectangle or  $\frac{2}{3}$  for a circle They are not quite reliable in any case, and especially when the orifice is elongated With a rectangular orifice of length twenty times its breadth the suppression of the contraction on one of the long sides has been found to increase c by 8 to 12 per cent, whereas by the formula the increase should be 7 2 per cent

For a square orifice in a thin will c is, say, 62 with full contraction and 10 when all contraction is suppressed. Therefore, if the contraction is suppressed on half the perimeter, that on the other half remaining unchanged, c will be about 81. But by equation 20 it is  $62 \times 1076$  or 667. It is clear, therefore, that if the contraction is suppressed on one part of the perimeter that on the remaining part increases, and this is what would be expected. The increase is, no doubt, most pronounced on the side opposite to the suppressed part, because the contracting filaments

of water are no longer directly opposed by others In a bell mouthed tube the contraction must be complete, whatever the clear margin may be In all other cases decrease in the cleur murgin causes the contraction to be 'imperfect' In chapter (art 3) some rules are given regarding the allowance to le made for imperfect contraction with weirs in thin walls sidering them in connection with the above formule for partial contraction the figures shown in table it are arrived at table S is the length of the perimeter on which the clear margin is reduced, G the width of the margin in the reduced part, d the le ist diameter of the orifice, and c, c, the co efficients for the orifice with complete and incomplete contraction respectively table is me int for orifices in thin walls, but even for these it is only approximate. It probably applies almost as well to other orifices with sharp edges. The allove formule and figures apply to c as well as to c, loth probably altering in about the same pro

portion and c, being constant. It may happen that the contraction is suppressed on one part of the perimeter of an orifice and imperfect on another part. Example 4, page 74, shows the method which may be adopted for such cases. When the contraction is either suppressed or very imperfect on nearly the whole perimeter the approximation becomes very doubtful

When an orifice 30 feet long and 05 feet lugh was bisected by vertical bras sheets of various thicknesses, it was found that a very thin sheet had little or no effect either on c or on the jet, but a sheet 0 if feet thick increased c nearly 1 per cent, the jets, however, uniting a short distance from the orifice?

4 Changes in Temperature and Condition of Water — The results of some experiments by Smith, Mair, and Unwin respectively are shown in the following table —2

Kind of Orifice	Dia meter	Ar ount ly which Tempera ture of Nater was raise!	Lifect on the Discharge	Head	Remarks
Orifice in thin wall,  Bell mouthed tube,	Inches 24	Fal r 82°	Decrease of 1 }	Feet 56 to 3 2	In all cases the initial
	40	144"	Decrease of 1 per cent	1 to 1 5	temperature of the water
	25	96°	Increase of ½ per cent	1 75	was normal namely, 45°
	∫ 40	110°	Increase of 31	1 to 1 5	to 61° Fahr
	15	115°	Increase of 2 per cent	1 75	

It is clear that it requires a great change of temperature to cause an appreciable change in the discharge, and that the change is greater the smaller the orifice. The law governing the change is not clear. Smith considers that with a head of 10 feet a change of 50° in temperature probably has no appreciable effect for orifices of more than 24 inch in diameter 3°.

Smith states that for small orifices (05 foot and less in diameter, and with heads less than 1 foot) the discharge fluctuates consider ably, and that this is perhaps due to unknown changes in the character of the water. With either larger heads or larger orifices

<sup>1</sup> Smith s Hydraulies, chap in 2 Ibid and Min Proc Inst C L, vol lxxxiv

<sup>3</sup> Hydraulies, clap m

the uncertainty disappeared It was not due to experimental error

Smith also states as follows Water containing clayey sediment may have a greater co efficient because of its oilness Thick oil, though very viscous, has a greater co efficient than water. When the water is in a disturbed condition, and approaches the orifice in an irregular manner, the jet may be ragged and twisted, but c is not affected appreciably Greasy matter adhering to the edge of an orifice slightly reduces the discharge, if the diameter is 10 foot or less, the reduction being due to the diminished size of the orifice

5 Velocity of Approach —The subject of velocity of approach is of more importance for weirs than for orifices, and a full discus sion regarding it is given in chapter iv (art 5) In equations 8 and 10 (pp 13 and 14) n may be taken to be 10, when the aperture is opposite that part of the approach section where the velocity is greatest-that is generally the central part and near the surface-and about 80 when it is opposite a part where the velocity is lowest-that is near the side or bottom. The method of solving the above equations has been stated in chapter in (art 7) For an orifice with sharp edges, whenever velocity of approach has to be taken into account, there will very likely be imperfect contraction on some part of the perimeter, and c, must be substituted for  $\epsilon$ 

Another method of procedure is to alter the forms of the equations Since  $h = \frac{v^*}{2g} = \frac{a^2}{d^2} = \frac{V^*}{2g}$  therefore equation 8 may be

written 
$$V^{2} = c_{v}^{2} \left(2gH + n\frac{a^{2}}{A^{2}}F^{2}\right)$$
  
Whence  $V^{2} \left(1 - c_{v}^{2} \quad n \quad \frac{a^{2}}{A^{2}}\right) = c_{v}^{2} \quad 2gH.$   
Or  $V = c_{v} \sqrt{2gH} \sqrt{\frac{1}{1 - c_{v}^{2} n \quad \frac{a^{2}}{A^{2}}}} \quad . \quad (22)$   
And  $Q = c \quad a \quad \sqrt{2gH} \sqrt{\frac{1}{1 - c_{v}^{2} n \quad \frac{a^{2}}{G^{2}}}} \quad . \quad (23)$ 

These can be solved directly The quantity  $\sqrt{\frac{1}{1-e^{-1}n^{\frac{d}{n}}}}$  is 'a co-efficient of correction' for velocity of approach. It may be

denoted by c. Table in shows some values of at for different

values of  $\frac{a}{A}$ , and it also shows the value of  $c_s$  and of the quantities learning up to it, for  $c_s=97$  and n=10. For a bill monthed tube a is simply the area of the discharging side of the tube and  $c_s$  is c

When  $\frac{\sigma}{A}$  is less than  $\frac{1}{3}$  a change in  $\epsilon_r$  or in  $\pi$  make, very little difference in  $\epsilon_r$  and a mere inspection of the table will enable its proper value to be found. Thus the use of  $\epsilon_r$  simplifies matter. For other kinds of orifices  $\epsilon$  mut be expirated into its factors  $\epsilon_r$  and  $\epsilon_r$  and  $\epsilon$  found by multiplying a by  $\epsilon_r$ . But it will be seen from the examples  $\{p, 72, \epsilon', e_2\}$  that the use of  $\epsilon_r$  may often be convenient. In all cases the use of  $\epsilon_r$  causes a little maccuracy when  $\frac{A}{\epsilon}$  is small. If greater accuracy is required  $\epsilon_r$ 

may be used for the first approximation only Another form of  $c_s$ :

 $\sqrt{\frac{1}{1-e^2n}a^2}$ , which would be very convenient for sharp-edged of the convenient for sharp-edged outles, but there are so many values of c that extensive tables would be needed.

Let  $\alpha_{\bullet} = C$ , then C is an 'inclusive co-efficient an  $Q = Ca \sqrt{2gH}$  (24)

This formula is not convenient for general use, because it would be difficult to tabulate all the values of C for different kinds of orifices for various velocities of approach. But where it is desired to ascertain by experiment the co-officients for any orifice to as to frame a di charge table for that orifice alone, then equation 24 is by far the best and simplest to use

If there are two ordices supplied from the same reservoir and situated not far apart, the discharge of each may be increased by the effect of the other, e.pecially when both are in the same will In Bazins experiments twelve orifices, cach S'x's nearly, and capable of being closed by gates were placed side by side. The following values of the inclusive coefficient C were found—

Number of gates open 1 2 3 4 5 or more Total co-efficient for all 633 642 646 649 650 When one gate was raised two inches and the others were fully opened the co-efficients were as follows —

opened the co-emerats were as follows —

Number fully open 1 2 3 4 5 or more

Co-efficient for the one | 6.00 6.07 6600 662 663 partly open |

The contraction was not complete, the twelve orifices being in

the end of a chamber only 18 feet wide. In order that two orifices in the same plane may have no effect on one another, it is probable that there should be no overlapping either of the minimum clear margins or of the minimum areas of approach sections requisite for full contraction and for negligible velocity of approach respectively (of chap v art 2)

6 Effective Head -The 'effective head' over an orifice is the head which would produce the actual velocity supposing c, to be unity If H and H, are the actual and effective heads

$$V = c_v \sqrt{2gH} = \sqrt{2gH_o}$$
 (25)

If  $H-H_c=H_r$ , then  $H_r$  is the head wasted in overcoming resistances Let  $\frac{H_r}{H} = c_r$ , then  $c_r$  is the 'co efficient of resistance,' or ratio of the wasted to the effective head

Since 
$$1+c_r = \frac{H_c + H_r}{H_e} = \frac{H}{H_e}$$
  
And from equation 25  $\frac{H}{H_e} = \frac{1}{c_v^4}$   
Therefore  $c_r = \frac{1}{c_r} - 1$  (26)

If there is velocity of approach H+nh must be put for H in the foregoing The following table shows the values of c, for different values of c. The head wasted is only a small per centage of the effective head, when c, is high, but it may be more than the effective head when co is low

$c_{o} = 995$	99	98	97	95	90	
$c_r = 010$	020	041	063	111	233	
$c_v = 85$	82	80	75	72	715	70
$c_{r} = 384$	489	563	778	929	956	1 049

The equation  $V = \sqrt{2gH_4}$  gives the actual velocity for an orifice referred to an imaginary water surface situated Hr feet below the actual surface (Fig. 40), but the equation will not apply to another similar orifice in the same reservoir at a different level, because H. will not have the same value

7 Jet from an Orifice -The jet of water from an orifice retains its coherence for some distance and then becomes scattered With an orifice in a thin wall, not circular and not in a horizont if plane, and with a head not very great compared to the size of the orifice, a phenomenon called 'inversion of the jet' occurs The section of the jet is at first nearly of the shape of the orifice,

OUTITIES.

but afterwards specule into sheets perpendicular to the sides of the orfice. Those portions of the jet which issue under different heals behave somewhat similarly to separate jets, which, if two of them meet of liquely, spread into a sheet perpendicular to the plane containing them. This expansion into sheets reaches a limit and the jet contracts again to nearly the form of the orifice,

but if its coherence is retained it again throws out sheets in direction herecting the angles between the previous sheets. This is probably due to surface tension or capillarity. The fluid is enclosed in an envelope of constant tension, and the recurrent form of the



51

jet is due to all rations of the fluid column, as they would be if the offices were far apart.

Fig 30 shows the cross sections of jets from two square orifices.

At a corner the two streams A and C



and some fluid is forced towards the corner. The full line in Fig. 37 shows the form next assumed, and the dotted line that assumed subsequently. The dotted lines in Fig. 36 show the form of jet where the two squares are joined to form a rectangular ornice.

Let H, be the effective head over an orifice Them if the jet issues vertically upwards and H is not great, it rises to a height very nearly equal to H. It then expands on all sides (Fig 38) and scatters Let be the head, measured from the plane AL, over any cross section of the jet, and y the dismeter of the jet at the cross section. The velocity of the jet is very nearly

 $\sqrt{2gx}$  and its sectional area is as y'. But since the discharges at all cross sections are equal the velocities are inversely as the sectional areas. The

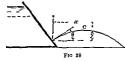
inversely as the sectional areas. Therefore if d is the diameter of the jet at the vena contracta where the velocity is  $\sqrt{2gH_*}$ .

<sup>1</sup> Encycloperdia Britannica minth edition Article Hydr meel anics

$$\frac{y}{d} = \frac{\sqrt{2qH_e}}{\sqrt{2_{JX}}} = {H_e \choose x}^{\frac{1}{2}}$$
Or 
$$y = d\left(\frac{H_e}{x}\right)^{\frac{1}{2}}$$
 (27)

Theoretically y should be infinite when x=0 but practically the jet breaks up and scatters. The velocity of the jet decreases uniformly, that is, decreases by equal amounts in equal periods of time. When the head is great the jet does not retain its coherence long enough to rise to the height  $H_x$ .

A body of water issuing from an orifice in a direction not vertical describes like any other projectile, a curve which if the



resistance of the air is neglected, is a parabola with a vertical axis and apex upwards. If the jet issues with velocity V, and at an angle  $\theta$  with the horizon (Fig. 39) the

equation to the parabola as given in Dynamical Treatises is

$$y = x \tan \theta - x \frac{g \sec^2 \theta}{2V^2}$$
 (28)

where y is the height of any point above the orifice corresponding to any horizontal distance x. The maximum value of y that is the height of the point C above the orifice is  $\frac{Y}{x} \sin^2 \theta$ . If y = 0

$$z = \frac{2V}{a} \frac{\tan \theta}{\sec \theta} = \frac{V^2}{I} \sin(2\theta) \qquad (29)$$

This gives the range of the jet on a horizontal plane passing

through the orifice If  $\theta = 45^\circ$ ,  $\tau = \frac{V^*}{q}$ . This is the maximum range, and in this case the maximum height is V.

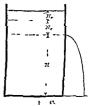
If the jet issues horizontally (Lin
10) equation 28 becomes

$$y = x_{2I}^{*}, y = x_{4II}^{*}$$
 (30)

and the range of the jet on a horizontal plu o H feet below the orifice is

$$\tau = 2\sqrt{H}.H$$
 (31)

The range is a maximum when He=II, et, for a plane passing



OPIFICES 53

through the bottom of a reservoir, when the orifice is slightly below mid depth (See also Nozzles, art 16)

### Section II -ORIFICES IN THIN WALLS

8 Values of Co efficient -The co efficient c has been determined for a great variety of cases, and its values for orifices with full contraction are given in tables iv to vii They are all for orifices in vertical planes, but if the head is measured to the vent contracts they probably apply to orifices in other planes, except when the head is small compared with the height of the orifice. These cases, marked off by horizontal lines in the tables, will be considered in article 19 Tables is and a contain the figures arrived at by Smith 1 from a discussion of various experi ments, including some made by himself Smith states that the probable error in these co efficients is about 5 per cent Tables vi and vii contain the results arrived at by Fanning2 and Bovey 3 respectively, the latter from his own observations and the former by a consideration of various experiments, some of which, however, do not seem to be quite reliable The table given below contains selections from the above tables A rectangle with ratio n to 1 means a rectangle having the horizontal side n times the vertical side

The co-efficient c, is about the same for orifices in thin walls as for bell mouthed orifices (art 14). It is about 96 for small heads and 99 or more for great heads. By dividing c by c, the value of c, may be obtained. It is clear from Fig. 36 that the jet from a rectangular orifice formed from two squares is greater relatively to the size of the orifice thin for a single square, and that the relative size will go on increasing as the orifice is lengthened. In other words, the effect of the end contractions decreases as the orifice is lengthened.

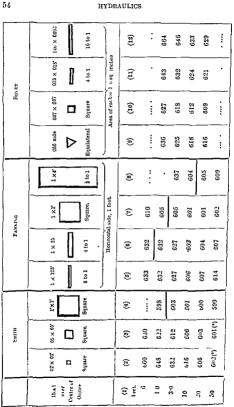
9 Laws of Variation of Co-efficient—The following laws regarding the variation of the co-efficient c are easily traced for laws 1 to 6 this only necessary to compare the figures in any horizontal line of a table, for law 7 in any vertical line

(1) With high heads (relatively to the size of the orifice) c is about the same for a given rectangular orifice whether the longer or the shorter side is horizontal

1 Hy tra lies chap in

\* Hudraulies chap &

<sup>2</sup> Treatise on Hater Supply Ingineering, chap xi



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- (2) For a square with sides vertical c is nearly the same as when the diagonal is vertical
- (3) Comparing a square with a rectangle having its shorter side equal to the side of the square, c is least for the square and mercases with the length of the rectangle. The difference is less marked when H is great

(4) For a circle c is about '005 less than for a square of the same diameter, and for the Bovey's orifices it is about '007 less than for a square of equal area

(5) For a square c is about 007 less than for a triangle of equal 3703

(6) For orifices of the same shape, c is greatest for small orifices and decreases for larger orifices, the decrease, however, becoming less and less rapid as the size and head in crease This law does not apply to Fanning's rectangles (cf., say, columns 6 and 8 of the table on page 54)

(7) As II decreases e increases, especially for small orifices and small heads There are some exceptions for Fanning's orifices with large heads

Since the values of c, do not differ much the variations in c must be due chiefly to variations in c. It will be seen below (art 13) that for Bordas mouthpiece the value of c can be found theoretically, and is about 50 For orifices in thin walls it is clear that c must be more than 50, but theory does not show how much more The main fact, namely, that the general value of c is about 61, and the next most important ficts, namely that c usually increases for small heads and small orifices (laws 6 and 7), do not admit of theoretical proof But the laws governing the minor variations of the co-efficients can to some extent be ex Laws 1 and 2 are what might be expected and are proved by Bovey's results because he used the same orifice in different positions, and therefore no error could arise from accidental differences in its size or character. The notes to table vii indicate some minor laws which cannot be explained Law 3 is clearly proved by Fanning's results, and also indirectly by Bovey's, although he used rectangles of equal area to the square and not with least side equal The cause of law 3 is clear from what has been said above regarding c. Legarding law 4, the higher co efficient of the square is owing to the smaller con traction in the angles Smith states that if this were the case the co efficient for a square would be greater than for a rectangle but he probably did not consider the matter carefully with the

aid of a diagram. The cause of law 5 is similar. The angles being more acute than in a square the suppression of contraction in them is still greater.

The co efficients cannot apparently all be quite correct. The difference between columns 2 and 3 of table vi is appreciable only for great heads, while between columns 3 and 4 it is greatest for small heads. The co efficients in column 10 of the table on page 54, when compared with columns 2 and 3, agree well except for the head of 20 feet. Fanning's figures showing c as increasing for great heads seem to be incorrect. The experiments considered by him do not seem to have included heads greater than 23 feet, and only a few of these

The manner in which the coefficient varies for orifices of different sizes and shapes is the opposite to what it would be if the friction of the orifice had any appreciable effect. The smaller the orifice, and the greater its deviation from a circle, the greater is the ratio of the border to the sectional arca, but the greater the co-efficient. It is remarkable that as H increases laws 3 and 6 become less pronounced, and that there is a strong tendency for the coefficients of all orifices of one shape to become equal 10. Co-efficients for Submerged Orifices—All the coefficients

above mentioned are for cases in which the orifice discharges into air. Table viii shows the results found by Smith for drowned orifices, the downstream water being 57 feet to 73 feet above the centre of the orifice. The co efficients are less by about 1 per cent, or for small heads 2 per cent, than for similar orifices discharging into air. The cause may perhaps be the formation of eddies, and the friction of the jet against the water surrounding it.

11 Remarks — If an orifice in a thin wall is in a surface not plane, the co-efficient will be greater or less than for a plane surface, according as the surface is concave or convex towards the reservoir.

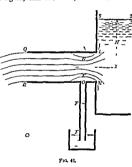
In some districts in America, where water is sold for mining purposes, the quantity taken is measured by orifices. The 'Miner's Inch' is a term which often means the quantity of water discharged by an orifice I inch square, in a vertical thin wall, under a head of 61 inches. In this case, if a taken at 621, Q is 153 e.ft. per minute, but the head is not always the same, and the orifices used are of many different sizes, generally much larger than a square inch. the Miner's Inch is then some fraction of the total discharge, and its value in c.ft. per minute varies from 1.20 to 1.76. The Miner's Inch is, in fact, a name with local variaties.

of meaning. The wall containing the orifice is often made of 2 inch plank, and the chief practical point to be noted is, that with a small orifice, or a very long orifice of small height, not only is exactness of size more difficult to attain, but there may be a chance of the orifice acting as a cylindrical tube, and giving a greater discharge than intended. Before the discharge of the orifice can be known, the size, shape, head, degree of sharpness, thickness of wall, width of clear margin, and velocity of approach must all be known.

#### SECTION III - SHORT TUBES

12 Cylindrical Tubes —In a cylindrical tube (Fig 41) the jet contracts, but it expands again, fills the tube, and issues 'full bore' The sectional

area at GK is, as in a simple orifice in a thin wall, about 63 times the area at LM, but the velocity at GK is greater than  $\sqrt{2gH}$ . and the discharge through the tube is greater than that from an ornice of area LM When the flow first begins, the air in the spaces NG, KO is at the atmospheric pres sure, and the discharge is not greater than that from an orifice LW The action of the water



exhausts the air and produces a partial vacuum. If t p be the pressure in NG, kO. The pressure in the jet GK is also p. The pressures at QR and ST are  $P_*$ . Let  $V_*$ , r be the velocities at GK and QR. The loss of head from shock between GK and QR. (equation 18, p 32) is  $\frac{(V-t)^3}{2j}$ . Then from equation 5 p 11, if the tube is horizontal,

$$H + \frac{P}{H} = \frac{p}{H} + \frac{I}{-J} \tag{A}$$

And 
$$H + \frac{P_a}{ll'} = \frac{P_a}{ll'} + \frac{v}{2g} + \frac{(V-v)^2}{2g}$$
 (B)  
But  $v = 63 P$  and  $V - v = 37 V$ 

Therefore from (B) 
$$H = \frac{V^2}{2g} \left\{ (63)^2 + (37)^2 \right\} = \frac{534 V^2}{2g}$$

Or 
$$V = \sqrt{\frac{2gH}{534}} = \sqrt{\frac{2gH}{73}} = 1 \ 37 \ \sqrt{2gH}$$

Practically there is some loss of head between LM and GK and actually

$$V = 1 \text{ 30 } \sqrt{2gH} \qquad (32),$$

$$v = 63V = 82\sqrt{2gH} \qquad (33)$$
Also from (A)
$$H + \frac{p}{l^{2}} = \frac{p}{l^{2}} + \frac{V}{2g}$$

$$= \frac{p}{l^{2}} + (1 \text{ 30})^{2}H$$

Therefore

58

 $\frac{P_a}{W} - \frac{p}{JV} = 69H \qquad (34),$ 

Or the pressure at GK is less than the atmospheric pressure by 69WH. The result is nearly the same if the tube is not hori zontal, provided H is large relatively to the length of the tube if  $c_c$  is not exactly 63, or if the actual loss of head differs from that assumed, the above results are somewhat altered. With a great head the vacuum becomes more perfect, the contraction, owing to the diminished pressure on the jet, less complete and the figures 130 and 69 are reduced. For moderate heads they are found to be about 132 and 75

If holes are made at N. O. water does not flow out but ar enters, and the discharge of the tube is reduced. If a sufficient number of holes are made, or if the whole tule and reservoir are in a victum, or if the tube is greased inside, so that water cannot adhere to it, the discharge is no greater than for a simple orifice If the holes are made at a greater distance from LM than about 11 diameters the discharge is unaffected. If a tube is added communicating with a reservoir I, the water for ordinary heads rises to a height FF= 75H, and if the height EO is less than this, water will be drawn up the tule and discharged with the jet This is the crudest form of the jet pump' The height to which water can be pumped, even if the vacuum is perfect, is limited to 34 feet. The discharge of the tube is reduced by the pumping With a great head the quantity 75H may exceed 34 feet, but in no case can the difference of pressures exceed that due to 31 feet

The co efficient of discharge for a cylindrical tube, like that for a simple orifice, increases as the head and diameter decrease approximate values are given in table ix, but the number of observations made has not been great

The coefficient for a tube ACG or ACGE (Fig 42) CD being  $AB \times 79$ , has been found to be the same as for a simple cylinder

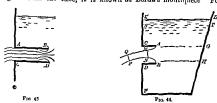


13 Special forms of Cylindrical Tubes

F10 42.

-If the tube projects inwards (Fig 43) the contraction and loss of head by shock are greater than in the preceding case, and if the edge of the tube is sharp the co efficients c, and c are reduced to about 72 This is because some of the water comes from the directions AB and CD

When the length AC (Fig 44) is so short that the jet does not again touch the tube, it is known as Borda's monthpiece



small heads AC is about half of AB The co efficient c, is about the same as for a simple orifice, but the contraction is greater is the greatest that can be obtained by any means. The value of G 19 52 to 54 That of c 1s 51 to 53 and it does not vary much The 1ct also retains its coherence longer than those from other kinds of orifices

The co efficient for Borda's mouthpiece can be found theoreti cally The velocity of the fluid along the sides of the reservoir FD, SC, which in most orifices is considerable is here negligible Thus the pressures on all parts of the reservoir are taken to le the simple hydrostatic pressures and they all balance one another except the pressure on GH, which, resolved horizontally is The horizontal pressure on AMMP is  $P_a\sigma$ 

difference between the two is Wall In a short time T let the

water between KL and MN come to STQP Its change of horizontal momentum is the difference between the horizontal momenta of KSTL and of MNQP, and that is the horizontal momentum of MNQP, since KSTL has no horizontal momentum. This change of momentum is caused by the force Wall Fquiting the impulse and momentum.

$$WaIIt = WQt \frac{I'}{g} = II \ r_c a V t \frac{I'}{g}$$
Therefore 
$$H = c_c \frac{I''}{g}$$
Let 
$$V'' = 2gII$$
Then 
$$H = \frac{I''^2}{g} = c_c \frac{I''}{g}$$
Or 
$$c_c = \frac{I}{g}$$

When a tube is placed obliquely to the side of the reservoir (Fig. 45) the coefficient is about c 00160 where  $\theta$  is the number of degrees in the angle made by the axis of the tube with a line perpen licular to the side of the reservoir, and c is the coefficient for the tube when  $\theta$  is 90 (Neville)



For a cylin ler with a tin diaphragm at its entrance (Fig. 4C) ti follow ag co efficients are given by Neville. They apply only when the tile is filled which it will be if not too long nor too short.

Rati of Ar a	Coefficient flichunge for 1
0	000
1	066
-2	139
3	219
i	107
-	399
6	4 13
ž	557
ų	675
-1	7.3
1-0	821

14 Bell mouthed Tubes —A simple bell mouthed tube (Fig. 8, page 12) is made of the shape of the jet issuing from an orifice in a thin wall. The length bL is half the diameter AC, and the curves AC, bD have a radius of 1.30 times AB. This makes  $CD = 80 \times AB$ . The edges at A and B must be rounded and not left sharp. We subsch found the following co-efficients for small bell mouthed tubes —

Head in feet 61 1 64 11 48 55 77 337 93 Co-efficients (c, and c) 959 967 975 994 994

This form of tube is often used as a mouthpiece for pipes to prevent loss of head by contraction. If the tube is not carefully made according to the above description c will probably not exceed 95. For tubes of square cross-section 1 foot in diameter resembling bell mouths co-efficients of 94 and 95 have been found.

15 Conical Converging Tubes —In a conical converging tube (Fig 47) the stream contracts on entering and again on leaving

(Fig. 47) the streum contracts on entering the tube. The co-efficients vary with the angle of the cone, but c, is always greater than for a cylinder. The following table shows the co-efficients found by Castel for a tube whose smaller diameter was 61 inch, and its length 26 times the smaller diameter. The co-efficients have reference to the smaller end of the tube. As the angle of the cone increases c, diminishes and c, increases. Their product c is a maximum for an angle of 13° 24. The co-efficients were found to be independent of the head.



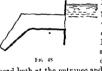
Fig 47

		 								1
ŀ	tr ale of cor		1	1	16 36	21 0	9 9	40 %	48 50'	
	810 01 001				969	915	19	-85	61	П
	_				91	9.1	9 .		-847	ì
					938	918	890	\$69	-817	

The following have also been found -

Cross seet on of Tube	Head In Feet	8maller en 1 of Tube	Larger end of Tube	Len.th of Tube	Angle of Conver gence	•
Circle Circle Circle Rect angle	300 27 18	1 20 in diam 1 21 , , , 2 17 ,, ,, 44 ft × 62 ft	4 20 in diam 1 50 , , , , 2 75 , , , 3 50 , , , 5 0 , , , 9 63 , , , 2 4 ft × 32 ft	10 ins 92 ,, 7 67 ,, 9 59 ft	4° 20 10° 20° 45° 11° 38 and 15° 18	1 00 934 903 898 888 864 976 to 987

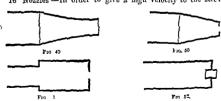
Conteal converging tubes are used to obtain a high velocity, but the above tables show that the velocity is not generally greater than for a bell mouthed tube. The angle is usually 10° to 20°. A cylindrical tip is sometimes added, its length being about 2½ times its diameter. In the case shown above, with a head of 300 feet, the jet did not touch the cylinder. If the tube projects inwards into the reser



your the co efficient is reduced,
but is greater than for an in
wardly projecting cylinder Com
cal tubes (Fig 48) are used in
India at canal falls for delivering
streams of water on to wheels for
driving mill stones There is loss

of head both at the entrance and at the bend 'The loss would be reduced by using a bell mouth and a curve

16 Nozzles -In order to give a high velocity to the sticam



resumn from a hose pipe a nozzle is applied to its extremity. Figs. 19 and 50 show 'smooth nozzles,' and Figs. 51 and 52

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two forms of 'ring nozzle' The diameter, d, of the orifice is usually about one third of the dirmeter, D, of the pipe, and the length of the nozzle six to ten times d Lixperiments with nozzle have been made by Ellis, Freeman, and others' The pressure, p, at the entrance to the nozzle being measured by a pressure gauge, the head on the nozzle is  $\frac{p}{H'}$ . The following co efficients have been found for the smooth nozzles, the pressure being 15 to

80 lbs per square inch

Diameter of orifice =  $\frac{3}{4}$  in  $\frac{7}{8}$  in 1 in  $1\frac{1}{8}$  in  $1\frac{1}{4}$  in  $c_n = 983 \quad 982 \quad 972 \quad 976 \quad 971$ 

For the ring nozzle c is for Fig 51 about 74, and for Fig 52, where a Borda's mouthpiece is added, about 52 In both cases c, is about the same as for smooth nozzles

To allow for velocity of approach since  $\frac{D}{d} = 3$ , therefore  $\frac{A}{a} = \frac{D^2}{d} = 9$ 

From table n, noting that  $c_0$  is greater than 97, it is clear that  $c_0$  is about 101, and the true co efficient c must be increased 1 per cent to give the inclusive co efficient C

The following table shows the vertical heights attained by jets from nozzles in experiments made by Ellis. It will be seen that the height of the jet is greater for the smooth nozzle than for the ring. It is also greater the larger the diameter of the nozzle, and this may be due to the jet longer retaining its coherence

#### VERTICAL HEIGHTS OF JETS FROM NOZZLES

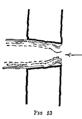
Pressure in pou de	Pressure lead in	1 nch	<b>\ozzle</b>	1} nel	i cl Nozzle	
per square inch	feet	S nooth.	R ng	Smooth	Ring	5mooth.
10 20 30 50 70	23 46 69 115 161 230	22 43 62 94 121 148	22 42 61 92 115	23 43 63 99 129 164	22 43 63 95 123 155	59 92 113 133

The total height to which the jet remains serviceable as a fire stream is less than that to which the scattered drops rise, the former height being about 80 per cent of the latter for small

<sup>2</sup> Transactions American Society of Civil E gineers vol xxi

heads and 60 or 70 per cent for greater heads, but it is difficult to say exactly to what height the stream is serviceable. The heights given in the above table are the total heights. Many kinds of nozzles have been tried, but with none of them does the stream remain clear, polished, and free from spraying up to the end of the first quarter of its course. Such a stream can be obtained for a pressure of 5 or 10 lbs per square inch, but not for a good working pressure

17 Diverging Tubes —With a conical diverging tube (Fig 53) the jet contracts on entering and expands again. With a tube



having an angle of 5°, smaller diameter 1 meh, and length 3¹ mehes, the coefficient of discharge for the smaller end
was 948, but with a tube having an
angle of 5° 6 and a length of nine times
the smaller diameter, a co-efficient of
146 was found. The case is similar to
a cylindrical tube. If the angle exceeds
7° or 8° the jet may not fill the tube,
and the co-efficient is then reduced. If
the angle is further increased, the jet
does not touch the tube, and the case
becomes an orifice in a thin wall.

If the tube projects inwards into the reservoir the co-efficient's reduced, but is greater than for an inwardly projecting cylinder. If the length of the tube is now reduced so that the jet does not touch the tube, the coclicent's greater than 51, the value for Borda's monthpiece, and I comes about 61 if the taper is increased till the case becomes a simple orifice

A compound diverging tube (Figs. 54 to 60) consists of a converging or bell mouthed tube with an additional length in which the tube expands again. If there are no angularities no head is lost by shock. The case is similar to that of a cylindrical tube. The air in the neck is partially removed by the water and the pressure reduced.

The following table contains information regarding various diverging tubes. It is clear that the co-efficient increases with the ratio of expansion (column 5) and decreases as the taper (column 6) increases, the highest co-efficients being obtained with high ratios of expansion and gentle taper. With a mean taper of 1 in 13.7 the limit seems to be reached when the ratio of expansion is 3.1%, but with a taper of 1 in 5.33, not till the ratio is 5.00.

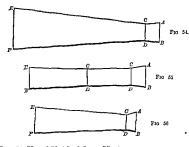
ORIFICES 65

A negative pressure in the neck is impossible (chap ii art 1), but if the vacuum there were perfect the pressure would be zero and the velocity would be  $\sqrt{2g(H+\frac{P}{H^*})}$  or  $\sqrt{2g(H+34)}$ . By making H small the discharge could be increased enormously, but practically the vacuum is always imperfect, and at a certain point the water ceases to fill the tube at the discharging end. The

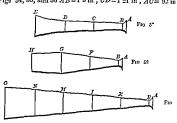
maximum co-efficient ever obtained is 2.43

The remarks regarding pumping action made under cylindrical tubes apply equally to diverging tubes. In a vacuum or with a greased tube the discharge from a diverging tube is no greater than from the mouthpiece alone, and the same may be the case with a great head, the stream passing the expanding portion without touching it

DU HYDRAULICS



In Figs 54, 55, and 56  $AB\!=\!1$  5 in ,  $CD\!=\!1$  21 in ,  $AC\!=\!92\,\mathrm{m}$ 



In Figs. 57, 58, and 59 AP is a bell monthed tube with diameter at B=2 in All the other segments except DL (I io. 57) are conical, and each is 2 in long



of the cone is least for

1 ft to 15ft, the
because the a man

1 to 15ft bein for

1 to 1 10ft the co

(I)	(2)	(3)	(0)	(5)	(6)
Reference to Tigure	Tol-	Coefficient for Smallest 1) ameter	*ma*lest Dia meter	Ratio of Plameter at D set arring Fnd to Smallest D ameter	Taper of Tube or flate at which Dismeter increases,
1 ig 54	Ar Ar	1 40 1 38	Inches 1:21 1:21	1-24 5 48	1 in 55 1 in 14 1
: -6	AC+CT AE	1·43 1·57	121	1-24 1 59	1 in 14 1 1 in 0 1
lig 57	AC	1 52	·375	1 58	1 in 9 1
	AD	1 78	375	2 17	1 in 9 1
	AE	1 57	375	3 83	1 in 5 6 (mean)
" <i>t</i> s	AF	1 69	375	2 33	l in 40
	AG	1 79	375	3 67	l in 40
	AH	1 79	375	3 33	l in 66(mean)
,, *9	AK	1 SS	375	20	1 in 5 33
	AL	2 03	375	30	1 in 5 33
	AM	2 07	375	40	1 in 5 33
	AN	2 09	375	50	1 in 5 33
	AO	2 09	375	60	1 in 5 33
Fig 60	AQ	1:48 to 1 60	1-22	1 42	1 in 23 3
	AE	1:98 to 2 16	1-22	2 30	1 in 15 1 (mean)
	AS	2 08 to 2 43	1-22	3 15	1 in 13 7 (mean)
	AT	2:05 to 2 39	1-22	4 0	1 in 13 1 (mean)

In Fig. 54 EF = 3 in.

CE=9 75 in

In Fig 55 EF=15 in

 $CC' = 3 \ 0 \ \text{in}$   $CE = 4 \ 1 \ \text{in}$ CD = CD

In Fig 56 EF=1 92 in. CE=6 5 in

In Fig to Er 21 02 M. CE = 0 5

In Fig. 57 Diameters at C, D, E are  $\frac{10}{32}$  in ,  $\frac{13}{15}$  in ,  $1\frac{7}{15}$  in

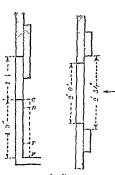
In Fig. 58 Diameters at F, G, H are  $\frac{7}{8}$  in ,  $1\frac{3}{8}$  in ,  $1\frac{1}{4}$  in.

In Fig 50 Diameters at K, L, M, N, O are  $\frac{3}{4}$  in ,  $1\frac{1}{5}$  in ,  $1\frac{1}{5}$  in ,  $1\frac{7}{5}$  in ,  $2\frac{1}{5}$  in

In Fig 60 Diameters at B, P are 1 22 in , and at Q, R, S, T 1 74 in , 2 81 in , 3 85 in , 4 90 in

## CO EFFICIENTS FOR SLUICES, ETC.

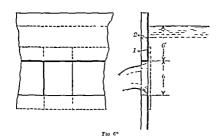
Kinds of Aperture	Description	Wilth of Opening	Height of Opening	Co efficient.	Hea 1
Sluice, <sup>1</sup> .	Shown in Fig. 61.  As above, but with boards CF or DE added		1 31 ft to 10 ft Do	61 to 69 (averages) 64 to 70 (averages)	9 8 ft over upper edge
Do,	In woodwork 177 ft thick at bottom, and 87 ft else where	4 265 ft Do	17ft 39ft	625 803	6ft to 14 ft over centre
Iron gates, <sup>3</sup> Bari Doab Canal, India	Working in grooves in the masonry heads of distribu taries	4 ft to 10 ft	3 ft to 2 ft	72 to 78 (averages)	25 ft to 4 8 ft
Orifice,3 .	Shown in Fig 62 1 inch plank placed against a 6 inch space between two 2 inch planks	5 ft 1 0 ft 1 5 ft 2 0 ft 2 5 ft	5 ft ,, ,,	593 607 615 621 626	5 ft over upper edge



<sup>1</sup> The smaller values of c oc curred with the greater height of opening For any given height of opening c varied as the head changed, being generally greatest for a head of about 1 ft

\* The co efficient includes the allowance for velocity of approach which was considerable. There was no contraction at the bottom and indes. The openings were generally submerged. O increases as II decreases, and it also increases with the size of the opening.

The co-efficient varies in a similar mainer to that for an orifice in a thin wall

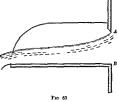


### SECTION IV -SLECIAL CASES

18 Sluices and other Apertures -A sluice is an orifice provided with a gate or shutter Generally there are adjuncts which complicate the case and render the co efficient uncertain When the gate is fully open the case may approximate to that of an orifice in a thin wall When it is nearly closed the case may resemble that of a prismatic tube Where accuracy is required the co efficient must be determined experimentally It may have any value from 50 to 80, or even outside these limits The preceding table shows some values Sometimes when a thick gate is lifted the flow tends to force it down again, especially when it is raised slightly. This is

probably due to the forma tion of a partial vacuum under the gate

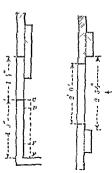
If the sides and lower edge of an orifice are pro duced externally so as to form a 'shoot' (Fig 63) the co-efficient c may be greatly altered The air has access to the issuing stream, so that reduction of pres sure in the vena contracta



cannot take place, as in a cylindrical tube. On the other hand the

## CO EFFICIENTS FOR SLUICES, FTC

Kinds of Aperture	Description	Width of Opening	Height of Opening	Co efficient	Head	
	Shown in Fig 61	2 0 ft	1 31 ft to 10 ft	61 to 69 (averages)	98ft over	
Sluice,1 .	As above, but with hoards CF or DE added	Do.	Do	64 to 70 (averages)	upper edge Do	
Do,	In woodwork 1 77 ft thick at bottom, and 87 ft else where	4 265 ft Do	1 7 ft 39 ft	625 803	6ft to 14 ft over centre	
Iron gates, <sup>2</sup> Barı Doab Canal, India	Working in grooves in the masonry heads of distributaries	4 ft to 10 ft	3 it to 2 ft	72 to '78 (averages)	25 ft to 4 8 ft	
Orafice,3 .	Shown in Fig 62 1 inch plank placed against a 6 inch space between two 2 inch planks	5 ft 1 0 ft 1 5 ft 2 0 ft 2 5 ft	5 ft	593 607 615 621 626	5 ft. over apper edge	

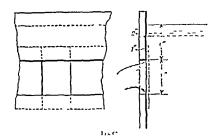


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<sup>1</sup> The smaller values of c oc curred with the greater height of opening For any given height of opening c varied as the heal changed, being generally greatest for a head of about 1 ft

<sup>2</sup> The co efficient includes the allowance for velocity of approach which was considerable. There was no contraction at the bottom and sides. The openings were generally submerged. O increases as II decreases, and it also increases with the airs of the origin.

3 The co efficient varies in a similar manner to that for an orifice in a thin wall

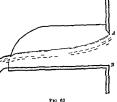


## SECTION IV -SELECTE CISES

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If the sides and lower edge of an orifice are produced externally so as to form a 'shoot' (Fig 63) the co-efficient c may be greatly altered The air has access to the issuing stream, so that reduction of pressure in the vena contracts.



On the other hand the

cannot take place, as in a cylindrical tube

irrction of the shoot has to be overcome. When the head is more than two or three times the height AB the discharge of the shoot may be nearly the same as that of the simple orifice, but otherwise it is reduced. For an orifice 8 inches by 8 inches with  $H_1$ ,  $H_2$  inches the addition of a horizontal shoot 21 inches long reduced c from 57 to 48. With a horizontal shoot 10 feet long the following co efficients have been found, the orifice being 656 feet wide.  $H_1$  and  $H_2$  are the heads over the upper and lower edges of the orifice

H - H1			H <sub>1</sub> is	ı feet			
n -n1	066 164		3*8 656		1-64 0 84		Remarks
feet •656 164	48 49	51 58	54 62	57 63	60 63	60 61	Full contraction
656 164	53 59	55 61	57 63	59 65	61 65	61 65	Lower edge of orifice flu h with bottom of reservoir

## 19 Vertical Orifices with small Heads -Let ACDL (Fig 61)

c D B

11161

0

be a bell - mouthed ornice. The equations for ornices of different forms are found by integration. An ornice is supposed to be divided into an infinite number of horizontal layers. The discharge of any layer is  $\epsilon_0 \sqrt{2g}I^2 \cdot ldH$  where H is the head over the layer, I its length in the plane of the ornice, and dH its thickness. For a rectangular ornice.

$$Q = c_i J \sqrt{2g} \int_{II_i}^{H_i} II_j^i dH$$

$$= \frac{1}{2} c_i J \sqrt{2g(H_i)^2 - H_i^2)} \qquad (75),$$
where  $H_i$  and  $H_i$  are the heads at  $C$  and  $D$  respectively. The

discharge is the difference between the discharges of two weirs

<sup>1</sup> Mering Hy leanly que, sec n le litt n, IP 36 and 37

with crests at C and D respectively, and no contraction For a triangle whose base is upward and horizontal and of length l  $Q = \frac{a}{5}c_e l \sqrt{2g} \left( \frac{1}{2} \frac{H_e^{\frac{a}{2}} - H_e^{\frac{a}{2}}}{H_e - H_e} - H_e^{\frac{a}{2}} \right) \qquad (36)$ 

$$Q = \frac{2}{3}c_{\tau}l\sqrt{2g}\left(\frac{2}{3}\frac{H_{b}^{5} - H_{c}^{3}}{H_{b} - H_{c}} - H_{c}^{2}\right)$$
(36)

For the same triangle with base downwards and horizontal

$$Q = \frac{2}{3}c_{v}l\sqrt{2g}\left(H_{b}^{\frac{3}{2}} - \frac{2}{5}\frac{H_{b}^{\frac{5}{2}} - H_{c}^{\frac{5}{2}}}{H_{b} - H_{c}}\right)$$
 (37)

For a trapezoidal orifice, the lengths of whose upper and lower sides are I, and I, respectively, these sides being horizontal, the equation is obtained from equation 35 with 36 or 37 It is

$$Q = \frac{2}{3}c_{\bullet}\sqrt{2g}\left\{l_{\bullet}H_{\bullet}^{3} - l_{t}H_{t}^{3} + \frac{2}{3}(l_{t} - l_{\bullet})\frac{H_{\bullet}^{\frac{4}{3}} - H_{t}^{\frac{4}{3}}}{H_{\bullet}}\right\}$$
(38)

For a circle whose radius is R and H the head over its centre

$$Q = \frac{\pi}{3}c_v B \sqrt{2gH} \left(1 - \frac{1R^s}{32H^2} - \frac{5}{1024} \frac{R^s}{H^s} - \frac{105}{65.536} \frac{R^s}{H^s} - etc\right)$$
 (39)

If velocity of approach has to be allowed for nH must be added to each of the heads in equations 35 to 39 Thus equation 35 becomes

$$Q = {}_{3}^{n} \epsilon_{v} l \sqrt{2g} \{ (H_{b} + nh)^{\frac{n}{2}} - (H_{t} + nh)^{\frac{n}{2}} \}$$
 (40)

In every case the discharge calculated by the above equations is less than that obtained with the same co efficient by equation 9 or 10, p 14, but owing to the much greater simplicity of these last, it is better to use them, and to multiply the result by a second co efficient to correct the error These 'co-efficients of correction,' co are given in table x1 In this table D is the height, measured vertically, between the upper and lower edges of the orifice C and D (Fig 64), and the head in column 2 is that over a point halfway between these edges This, in the case of triangular or semi circular orifices, is not the head over the centre of gravity of the orifice,2 but this latter head must be used in equation 9 or 10 The correction required is practically negligible when H=2Dis greatest when H= 50D, that is when the upper edge of the orifice is at the surface, which of course it never can be exactly

All the above equations apply to orifices with sharp edges, but they ought to be applied to the vens contracta Not only is D less for CD (Fig 34, p 45) than for AL, but H is greater because of the fall PN which the jet undergoes between AB and CD Thus the ratio in column 2 of table x is always greater for

<sup>1</sup> Smith's Hydraulies, chap 11 The distance of the centre of gravity of a semicircle from its diameter is

<sup>1244</sup> of the radius

72

CD than for IB The co efficients for orifices in thin walls, those above the horizontal lines in the tables (iv to 11 and p 54), have however been obtained by applying the above equations to the orifice AB, and for such orifices the co efficients should be so used, or if equation 9 or 10 is used, c, should be taken with reference to AL But for a sluice, cylindrical tube, or other aperture for which some other co efficient c is to be employed, the correct method is to ascertain c, and c,, obtain the approximate dimensions of the jet, and find the fall PN by equation 31 (p 52) This has been done for some square orinces, and the results utilised by adding column I to For any entry in this column the corresponding entry in column 2 gives the approximate figure for the jet, and the value of c. (to be applied to the result found by equation 9 or 10) is that in column 3 For a rectangle whose horizontal side l is less than D, the vena contracta is nearer to the orifice, the full PN is less, and the contraction of the jet in a vertical direction less, so that the figures in column 1 approach nearer to those in column 2 When l is less than 5D column l is not needed

The co efficients for vertical orifices under small heads are not well determined. The smallness of the margin on the upper side of the orifice tends to produce incomplete contraction there and to increase c, but, on the other hand, there is a fall in the water surface upstream of the orifice, the head is measured above the fall, and this, according to Smith, reduces c. A vortex may also be formed, and possibly it may penetrate the orifice and reduce c. Columns 4 and 7 of the table on page 51 do not agree, though in both cases the head was measured back from the orifice Smith's co efficients are to be preferred

With an orifice in a horizontal plane under a small head the proportion of water approaching axially is reduced and the contraction is probably increased, except with bell mouths. The co-officients for such cases having nearly all been obtained for orifices in vertical planes, are not likely to apply correctly to others, even if the head is measured to the vera contracts.

The matter in this article refers to cases where H is small compared to the orifice If, in addition, H is actually small, the difficulties attending such cases (chap ii art 7) are added

#### EXAMILES

Example 1 —Water enters the condenser of a steam encine at the sail vel from a reservoir who e water surface is 10 feet above the injection orince. The pressure in the condenser is 3 lbs per square inch Find the theoretical velocity of flow into the condenser

The atmospheric pressure in the reservoir is 14.7 lbs per square inch. The resultant pressure is thus 11.7 lbs per square inch or 1685 lbs per square foot. This is equivalent to a head of  $\frac{1685}{62.4} = 27$  feet. The total effective head is therefore 37 feet.

From table 1 the velocity is 48 7 feet.

Example 2 —Find the discharge from a circular bell mouthed tube, 1 foot in diameter, situated in the middle of the end of a horizontal trough of rectangular section, 2 feet wide and 2 feet deep

The head is 1 foot From the table in article 14 c, is probably 96 From table x the coefficient of correction for small heads is 992 A is 4 square feet and a is 7854 square feet  $\frac{A}{a} = \frac{4}{7854} = 501$  From table in the coefficient of correction for velocity of approach is 102 From table i  $\sqrt{27H} = 802$  Then

Q= 96×8 02× 785× 992×1 02=6 12 cubic feet per second

Example 3—A culvert 3 feet long, consisting of a semicircular

arch of 1 foot radius resting on a level floor, has to pass a discharge of 9 feet per second. There is a free fall downstream What will be the water level upstream?

From table ix c may be taken to be  $^{60}$  Also  $a=2 \times 785 = 1.57$  square feet

To obtain an approximate solution

$$Q=9=80\sqrt{2gH\times 1.57}$$
  $\sqrt{2gH}=\frac{9}{50\times 1.57}=7.17$ 

From table 1 H=80, or the water will be 80 foot above the centre of gravity of the aperture or 22 foot above the crown of the arch

The contraction, supposed to be complete elsewhere, is nearly absent at the crown, and may be taken to be suppressed on one fourth of the perimeter, thus (table ii) making

 $c=80\times104=832$ In table x D=10 foot, and the head over the centre of the orifice is 22+50=72 foot or 72D. This corresponds to 8DH7 the year contracts, and the figure in column 8, differing no doubt.

the year contracts, and the figure in column 8, differing no notice, hardly at all from column 4, is 9.00.

The above two corrections are 4 per cent. plus and 1 per cent minus, so that Q is really 3 per cent more than a seried. To

make it right deduct 6 per cent from H, while will the le 80 × 94 = 752 foot, that is, the water is 18 foot above the crown.



Example 4 -For the culvert shown in the annexed diagram (2 feet wide and 5 feet long), let there be an open approach channel 4 feet wide, with vertical walls and floor level with that of the culvert Find the discharge when the unstream head is I foot above the crown of the arch, and the downstream head 6 inches above it

In this case there is incomplete con traction on all sides, and also velocity of approach From example 3, a=3 57 square

feet, A=12 0 square feet, P=4 0+3 14=7 14 feet, S=2 0 feet If the contraction were complete on ALB, c, would be (art 3) about  $80 \times (1 + 152 \times 7) = 80 \times 1043 = 834$  The average margin on AEB is about 130 feet. Therefore  $\frac{G}{d} = \frac{130}{9} = 65$ , and

$$\frac{S'}{P} = \frac{514}{714} = 75$$
 From table  $n \frac{c_t}{c} = 1035$  about Therefore  $c_t = 834 \times 1035 = 863$ 

The head is 5 foot, and as the orifice is wholly submerged no correction for small head is needed. From table 1  $\sqrt{2gH}$  is 5.67  $Q = 863 \times 5 67 \times 3 57 = 17 47$  cubic feet per second

To allow for velocity of approach by the usual method,

$$i = \frac{1747}{12} = 146$$
 feet per second Let  $n = 10$ 

From table 1 h = 033, H + h = 533 From table 1 V = 5.87Then  $Q = 863 \times 5.87 \times 3.57 = 18.08$  cubic feet per second

To allow for velocity of approach by a coefficient of correc tion, for the contracted section c. is (art 12) about 1 30, and

 $c_e = \frac{863}{130} = 664$  Therefore  $a = 3.57 \times 66 = 2.36$  square feet, and  $\frac{A}{a} = \frac{120}{2.36} = 5.09$  From table 111, noting that c, 18 about 1.30 instead of 97, and that the figures in column 3 are to be increased, ca is about 103, that is, 3 per cent must be added to 17 i7,

Note -Further examples may be obtained by taking cases at alogous to some of those in examples of chap is

making 17 99 cubic feet per second

## TABLE I -HEADS AND THEOPETICAL VELOCITIES (Art 1)

I or a head greater than 10 feet divide the lead by 100 and take ten times the corresponding velocity. Thus for a head of

120 feet the velocity is \$7.9, or ten times the velocity given for a head of 1.2 feet. For a velocity over 25 divide it by 10 and rulliply the corresponding head by 100. The same methods can be adopted to facilitate interpolations. Thus for H=-032 look cut 3.2.

In the first fifteen entries the heads correspond to certain definite selective. These entries may be useful increes of selecity of approach. After that the selectives correspond to definite heads.

II .	,	н	1	н	1	17	1	11	1	п	1
				_		ı—			-	1	í
·W 22	35	13	250	45	- 38	84	1 7 75	23	12-2	6-2	200
10 125	40	135	24,	46	5 44	85	7 40	24	124	63	20 1
-0027	42	14	3-00	47	5 50	56	744	25	127	اةا	20 3
10/130	44	14"	3-05	45	5 -6	87	748	26	120	1 65	20 5
0033	40	15	3 11	-49	* 62	88	7 73	27	13-2	1 66	20 6
*CH136	45	1"5	3 16	50	1 - 67	59	7.7	25	134	67	20 7
7/179	-0	16	3 21	1	573	-50	7-61	20	137	68	20 9
0012	72	165	3 26	-3	5.9	-91	7 65	3	13.9	69	21.0
10013	54	17	3 71	53	* 45	92	770	131	141	17	21 2
10040	76	175	3 36	14	5 20	าว	7.74	3-2	143	71	213
0052	55	15	3 40	-5	595	-01	778	33	14 5	7.2	21 5
7.00	-6n	185	1 45	1.6	6.00	-05	7 82	34	148	73	21 6
2300	-65	12	3.0	57	6 06	ಾರ	756	35	150	74	218
0976	70	195	3 35	55	611	-97	7 90	36	15-2	73	21 9
10047	75	-20	3 . 9	19	6 17	98	. 791	37	154	76	221
10.	50	-21	3 65	-60	6.22	99	798	38	156	77	222
015	-98	-22	376	-61	6-28	1	8.02	39	158	78	224
02	1 13	223	355	62	632	1.05	8-22	4	160	79	22 3
0.25	1-27	24	3 93	-63	C 37	111	8 41	41	162	3	227
03	1 79	23	4-01	64	6 42	1 15	8 60	42	164	81	228
035	1 50	-26	4-09	65	6 47	12	8 79	43	166	82	23 0
04	1 60	27	4 17	66	6 72	12,	8-97	44	168	83	23 1
045	1 70	29	4-25	67	6 57	13	9 15	45	170	84	232
05	1 79	29	4 3.2	GB	l e cr	1 35	9 32	46	172	8 5	234
055	1 \$8	30	4 39	69	6 66	14	9 49	47	174	86	235
06	1.97	31	4 47	70	671	1 45	9 (6	48	176	87	236
065	204	12	4 4	71	676	15	9 83	49	177	88	238
07	212	33	461	72	6 81	1.55	9 98	5	179	89	23 9
075	2 20	34	4 64	73	686	0.1	102	51	181	9	24 1
08	2 27	35	4 75	74	6 91	1 65	103	52	18 3	91	24 2
085	234	36	4 81	75	6 95	17	105	53	185	92	24 3
09	241	37	4 87	76	6 99	1 75	106	5 1	187	93	246
095	2 47	38	494	77	7 04	18	108	55	188	9 4	247
10	2 54	39	5 01	78	7 09	1 85	10.9	57	102	96	248
105	2 60	40	5 07	79	7 13	19	11 1	58	193	97	24 9
11	2 66	41	5 14	80	7 18	1 95	11 3	59	195	98	250
115	2 72	42	5 20	81	7 22 7 26	2 1	117	6	196	99	25 2
12	278	43	5 26	82		21	11 9	61	198	10	25 4
125	284	44	5 32	83	7 31	22	113	" 1		••	
L											

Taiif II—Imierfect and Partial Contraction for Rectangular Orifices with Shapp Edges (Art 3)

$\frac{S'}{I}$	3	2 67	2	1	5	0	Ren arks
		Δ.	pproxima	te Values	ot <del>c</del>		
		[	1				* These are cases
25	1	1 000	1 002	1 006	1 015	1 04*	of partial contraction, see equation 20, page 46
50	1	1 001	1 003	1 013	1 030	1 08*	+ These are quite
75	1	1 001	1 004	1 019	1 045	1 12*	
875	1	1 001	1 005	104†	1 10†	1 40†	pressed on all sides
1	1	1 002	1 006	1 05†	1 20†	1 61‡	18 increased by 61 per cent above its mean value (62)

# Table III —Coefficients of Coppetion for Velocity of Alphosch (Art 5)

 $(c = 97 \quad n=10)$ 

				· -	
(1)	(2)	(3)	(4)	(5)	(6)
শ্ব	, 2 , 2	C.2n Q.2	1 c2s 4	VI + + 1	$\sqrt{\frac{1}{\cot C_a}} \frac{1}{d^2}$
1 33 1 5 2 2 5 3 5 10 15	5625 4444 2100 1596 1111 0400 1010 1004 10025	529 418 23, 150 104 039 010 001 0014	471 782 765 850 896 962 990 996 9976	687 763 875 922 917 981 995 -997 -999	1 456 1 311 1 143 1472 1 076 1 410 1 405 1 403

77

TABLE IV —CO EFFICIENTS OF DISCHARGE FOR CIRCULAR ORIFICES IN THEN WALLS (Art 8)

1				Pin	eter of (	Orifice in	Feet			
Hea !	-0	-03	*04	105	107	1	15	2	6	1
1 cet.			_				_			
3(*)	· 1			637	628	621	608		• •	١.
5			637	631	624	618	606			[
5		643	633	627	621	615	605	600	592	[ ·
6	655	640	630	624	618	613	605	601	593	
8	648	634	626	640	615	610	603	601	594	591
1	644	631	623	617	612	608	603	600	595	591
15	637	624	618	612	608	605	601	600	596	593
2	632	621	614	610	607	604	600	ا 99د	237	595
25	629	619	612	608	605	603	600	599	598	596
3	627	617	611	606	604	603	600	599	598	597
4	623	614	609	605	603	602	599	599	597	596
6 8	618	611	607	604	602	600	599	593	597	596
8	614	608	605	603	601	600	598	598	596	596
10	611	606	603	601	599	598	597	597	596	595
20	103	600	599	598	597	596	596	596	596	594
50 (*)	596	596	595	595	594	594	594	594	594	593
100 (*)	593	593	592	592	592	592	592	592	592	592

Table V —Co efficients of Discharge for Square Orifices in Thin Walls (Art 8)

				S d	e of Orli	ice in Fe	et.			
Head	-02	103	-04	05	-07	1	15	-2	6	1
Feet.										
3(*)		l i		642	632	624	612			Į .
4		ا ـ . ـ ا	643	637	628	621	611			ĺ
5		648	639	633	625	619	610	605	597	Į.
6	660	645	636	630	623	617	610	605	598	۱ ــ
8	652	639	631	625	620	615	608	60 o	600	59
1	648	636	628	622	618	613	608	605	60	59
15	641	629	622	617	614	610	606	605	602	60
2	637	626	619	615	612	608	606	605	604	60
25	634	624	617	613	610	607	606	605	604	60
3	632	622	616	612	609	607	606	605	604	60.
	628	619	614	610	608	606	605	605	603	60:
6	623	616	612	609	607	605	605	604	603	60:
8	619	613	610	608	606	605	604	604	603	609
10	616	611	608	606	605	604	603	603	602	60
2ŏ	606	605	604	603	602	602	602	602	601	600
ر <sup>د</sup> ) 50		601	601	601	601	600	600	600	599	59
00 (r)		598	598	598	598	598	598	598	598	598

For errollar and square orifices 2 feet in diameter under heads of 2 to 10 feet co officients of about 60 have been found, and for a best of circular orifice 033 foot in diameter under a head of 35 feet a co-efficient of 25 foot

Table VI —Co efficients of Discharge for Rectangular Orifices, One Foot wide, in Thin Walls (Art 8)

Head			13	le ght of O	rifice in F	eet.		
Head	1°5	25	50	5	1	1.0		1
Feet								
2	634	1	1	1	1	1	į	1
3	634	632		1	1	!		ļ
4	633	632	621	1	1			1
5	633	632	619	615	1	1	1	1
6	633	632	619	613	610	ĺ	1	ſ
8	633	632	618	612	606	630	1	1
1	632	632	618	612	605	624	l .	l
1.25	631	632	618	611	604	624	632	1
15	630	631	618	611	604	619	627	
2	629	630	617	610	605	617	628	i
25	628	628	616	610	605	615	627	645
3	627	627	613	610	t Oa	613	619	637
4	624	624	614	609	605	611	616	630
6	615	615	609	604	602	606	610	618
8	609	607	603	602	601	602	604	013
10 ]	606	603	601	601	601	601	602	604
20	607	604	602	601	601	601	602	605
30	609	604	603	602	100	602	603	605
10	611	606	604	603	602	603	605	607
50	614	607	605	604	602	603	606	609

TABLE VII —CO EFFICIENTS OF DISCHARGE FOR SMALL OPIFICES (area 196 square inch) IN THIN WALLS (Art 8)

	(-		24.	• •••••	,	· · · · · · · · · · · · · · · · · · ·
Hea l	Fqui lateral triangle base	Square * with ailes	Circular	lone	gle with si le	Remark«
	upward	Vertical		4 to 1 t	15 to 1 1	
Feet.						* With diagonal verti
1	636	627	620	643	661	calcisabout 0014 greater
2	628	620	613	636	651	† With long at le verti
4	623	616	608	629	612	cal c 14 about 0014 less
6	C20	614	607	627	637	I With I ng s le verti
10	618	612	605	G24	637	cal c 1s about '0005 lees
14	618	610	C04	622	630	fr heads up to 10 feet
20	616	602	603	621	629	and als ut 10005 more f r
•		1	1			the breater heals
		í				

TABLE VIII -- CONTROLLING OF DESCRIPTOR FOR SUPPRESED OF DESCRIPTION WALLS (Art. 10)

	tredth into the											
Tire?	€ 11 to 11 to 12	• , , , .	112	F 117	Paring's							
1	416	רק	4.12	100	722							
1 1	-610	415	12	10.05	722							
1.5	4.7	412	401	701	-621							
2	474	מי צי	10	<b>T76</b>	7620							
. 22	4 12	414	:22	T-04	~619							
3	4.12	₹17	272	101	cts							
4	1 (4)	477	:02	·en:	·							
· 			!		· 							

Taile IX.—Corffeens of Discharge for Cylindrical Turs (Art. 12.)

,	-	-	-	
ſ		frameter of T	ite in Inches	1
Head				1
Į.		,	1	, ,
				1
Feet.				1
<b>:</b>	51	53	82	)
2	. 53	52 1	81	80
-	1 "	[	. 1	1
22	ł	1	80	80
1	1		i	}

TABLE X —Co EFFICIENTS OF CORRECTION

FOR VERTICAL ORIFICES WITH SMALL HEADS (Art 19)

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Head over centre of square orifice with sharp edges	Head over centre of bell mouthed orifice or of vens contracts for sharp edged orifice	Rect	Circle or semicircle with d ameter vertical	Tri angle with base up ward,	Tri angle with base do vn ward	Semi circle with dia meter up ward	Bemi c rele with d a meter down ward	Remarks
	50 <i>D</i>	943	960	924	979	937	965	
	52D	950	965					The co
1 1	55D	957	970					not been
	60 <i>D</i>	966	975					detail for tri
52D	70D	976	982				Í	semicircles,
64 <i>D</i>	80 <i>D</i>	982	987					easily esti
78D	90 <i>D</i>	986	990				- 1	the figures
92 <i>D</i>	1 0D	989	992	1	İ	- 1	İ	hrst and tenth lines
1 13 <i>D</i>	1 2D	992	994		- 1	ĺ	[	When the
1 44 <i>D</i>	15D	995	997	996	998	996	997	greater than
	2 0D	997	998	j			i	efficients for
	2 5 D	998	999	- {		į	- 1:	shapes are nearly equal
} }	3 0D	999	999	1	1	-	- {	
	4 0D	999	1 000	ļ				

#### CHAPTER IV

#### WEIRS

[For preliminary information see chapter ii articles 4, 6, 7, 14, and 15]

## SECTION I -WEIRS IN GENERAL

1 General Information —The following statement shows a few typical kinds of weirs, and gives some idea as regards the coefficients. Further co-efficients will be given in subsequent 
articles, and from them the values for many cases occurring in 
practice can be inferred, but the varieties of cross section are 
innumerable, the co-efficients vary greatly, and generally can only 
be found accurately by actual observation. When the length, I, of 
a weer is great relatively to II, it makes little difference whether 
there are end contractions or not.

To ensure complete contraction iron filed sharp should be used for the upstream edges with small heads For heads of over a

foot planks or masonry may be used

Since the inclusive co efficient C increases with H, it follows that when there is velocity of approach Q increases faster than H! If H is doubled Q is about trebled To double the discharge H must be multiplied by 15 If a given volume of water passes in succession over two similar weirs, one of which is three times as long as the other, the head on it will be half that on the other. If a volume of water, passing in succession over two weirs, alters, the heads on both will alter in nearly the same ratio These rules are only approximate, and when there is no velocity of approach they are somewhat modified. To facilitate calculations the values of H<sup>1</sup> corresponding to different values of H are given in table xi

Smith states that with low heads such as 2 foot the discharge may be affected by a change in the temperature of the water of 30° Fabr. If the water is disturbed by waves or eddies the discharge is probably reduced, unless 'haffles' are used to calm it 84

## VARIOUS KINDS OF WEIRS AND THEIR CO-EFFICIENTS.

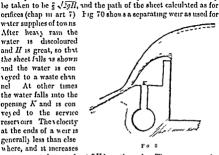
Type of Weir		ich Co	ns of N e efficien		t C for	Manner in which Co-
	Height	Top Width.	Upstream Slope.	Down stream Slope.	Co efficient Head of 1 f	efficient varies as Head increases
Survey mellenge Sh	Fret	Feet				
Fig 65. Thin Wall,	1.64				·67	Increases slowly
Flat top, vertical face and back	2:46	1-31	verti- cal	verti- cal	-51	Increases rapidly
Fig. 67 Steep back and sloping face	1 64	-33	2 to 1	ert:	·75 1	neri ases
	1 64	33	verti 5	to I	61 [1	acteures
Rounded.	61			1.	5 In	CPCARCA

These were are some of the types used by Bazin in his experiments. There were no end contractions. The co-efficient C includes the allowance for velocity of approach.

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In every case the initial horizontal velocity of the whole sheet may water supplies of towns After heavy rain the water is discoloured and H is great, so that the sheet falls as shown and the water is convered to a waste chan At other times the water falls into the opening K and is con veyed to the service reservoirs The velocity at the ends of a weir is generally less than else

where, and it increases



un to a point distant about 3H from the ends The pressure in the water passing over the crest of a weir is less than that due to the head

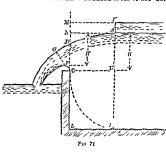
the velocity is greatest at the lower side, but with a broad topped weir the friction on the top reduces the velocities nearest the weir

The following statement shows the chief experiments on weirs in thin walls --

Observer	No of Obser	Length	He	ađ	Helgi t	State of Contrac	D stance of Measur
Observer	t ade	of Welr	Fron T		of Reir	tion	from Cres
	1	} eet	Feet.		Feet		Feet
Francis	46	10	6	16	46	Com	6.0
,	19	10	6	10	20	plete	60
	6	4	7	10	46220	or	6.0
Smith	12	26	6	17	38	nearly	76
Lesbros	21	1 77	1	6	18	com	115
or celet& Lesbros	16	66	08	7	18	plete :	115
I teley & Stearns	54	23 to 5	15	94	36 1	) Vari	60
Lesbros	34	66	06	7	18	fable	115
Francis	1 1"	10	7	10	46	,	60
Fteley & Stearns	10	19	5	16	66	Lnd	6.0
	30	5	07	8	32	con	60
Leabros	14	66	06	s	18	trac	11 3
Bazın	295	6 56	-23	10	37 to 8	tions	16 4
	38	3 28	23	13	33	absent	16 4
	48	1 64	23	18	33	]	164

Bazin's observations are the most recent and extensive. They included observations of the form of the upper and under surfaces of the falling sheet and of the air pressure beneath it. Brins states that under some circumstances the discharge of a weir can be ascertained better by observing this pressure than by observing the head. (Of art 8)

2. Formulæ —The ordinary weir formula (equation 11, p 15) and the other formulæ deduced from it are defective in form. It



is often said that the head XD(Fig 71) ought to be taken into account, the dis charge of the weir being con sidered to bethat าก orifice whose bottom edge is C and top edge D , but the formula would be much more complicated, and the height ND

is not well known. Any shortcomings in the formula are mide good by the values given to the co-efficients. Moreover there is no special reason why the section NO should be selected for measurement. From C to F the under side of the sheet rises if the weir has its upper edge sharp. The heads should probably be measured, as with an orifice in a thin will, to F and G at the contracted section. The flow over a weir with a wide top is still more complex. The case is really one of variable flow in a short open channel.

In all weir formule m can be written for  $\frac{2}{3}r$ , and this plur is adopted by Bazin, but c is the true co efficient expressing the relation between the actual and the theoretical discharge, and, following the usual practice, c will be used both in formule and in tables. Since  $\frac{2}{3}\sqrt{2}g=5$  37 this figure can be used in cikulations instead of 8-02, and multipheation by  $\frac{2}{3}$  is thus innecessor. The values of  $\frac{2}{3}c\sqrt{2}r$  corresponding to different values of c are given in table an and denoted by  $q_m$  being the discharges per foot run over a weir with H=1 foot

3 Incomplete Contraction —From a comparison of the coefficients obtained for various weirs in thin walls, Smith arrives at the formula

$$c_r = c \left(1 + 16 \frac{S}{I}\right)$$

where c, and c are the co-efficients for two equal wears, one with partial and one with full contraction P is the complete perimeter of the weir, that is 1+2I, S the length of the perimeter over which the contraction is suppressed. This formula applies for heads ringing from 3 foot to 10 foot, it is not exact, but may be used for finding co-efficients not otherwise known.

When the contraction is imperfect, whether or not the margin is sufficient to give a negligible velocity of approach, the formula arrived at by Smith is

$$c_i = c \left(1 + x \frac{S}{I}\right)$$

where  $c_i$  is the co-efficient for the weir with imperfect contraction, S the length of its perimeter on which the contraction is imperfect, and x is as follows, d leng the least dimension of the weir and G the width of the clear margin

$$\frac{G}{d} = 3 \quad 2 \cdot 67 \quad 2 \quad 1 \quad 5 \quad 0$$

$$z = 0 \quad 0016 \quad 005 \quad 025 \quad 06 \quad 16$$

When the contraction is imperfect over the whole perimeter S=I', and when

rhen 
$$\frac{G}{d} = 3 \quad 2.67 \quad 2 \quad 1 \quad 5 \quad 0$$

the increase in c per cent

$$=$$
 0 16 50 25 6 16

But when S is a very large fraction of P, or when S=I and  $\frac{G}{d}$  is very small—that is, when there is not much contraction left except at the surface—the rules become of doubtful application A Flow of Approach —Bazin observed some surface curves for

wers 372 feet and 1 15 feet high, and for each werr with several heads ranging from 5 feet to 1 of feet. He finds y (Fig 71) to be in every case about 3H, but the upper portions of the curves are so flat, especially for the lower heads, that it is impossible to say exactly where they begin. Observations made by Fteley and Stearns, with H nearly constant and different values of G, give results somewhat similar to Bazins, but when G is less than H, yis

For definitions of partial and imperfect see than in art 3

about 2.5G The above indicates the proper distance from the weir to the measuring section. In weirs with end contractions G, the distance of the end of the weir from the side of the channel

must be used instead of G if it exceeds G. In a wer with a long sloping face Smith found y to be 40 feet with H=7 24 feet. The fall ND or F for were in thin walls is generally between

In the last ND or F for wers in thin walls is generally between  $\frac{1}{10}$  and  $\frac{H}{4}$ . It is much greater with broad topped nears. In the above experiments with weight in thin walls F was found to be as

rbove experiments with weirs in thin walls  $\frac{F}{H}$  was found to be as follows—

$$G=3\,56$$
 17 5 372 115 feet  $H=614$  606 564 5 to 15 5 to 15 ,  $\frac{F}{H}=148$  145 114 149 143 ,  $\frac{F}{H}=148$  145 114 149 Bigin

Some other values are

90

$$H = 68$$
 37 20 08 feet Poncelet and Lesbros, were  $\frac{F}{H} = 09$  11 15 25 ... Poncelet and Lesbros, were to the sum of t

And for flat topped weirs

$$H = 5$$
 1 5 1 feet  $\frac{P}{H} \approx 27$  28 29 40 64 67 ,...

Top width 5 inch 2 inches 7 inches

According to Smith P is somewhat greater in weirs with no end contractions than in others, and increases slightly with I

I teley and Stearns found that just upstream of a weir the pressure, at least near the bottom, as greater than at the same level further upstream. Gener ally the difference is nearly as h or \frac{1}{2f}, and it also increases as \( T \) decreases. It never exceeded the amount due to a head of 05 foot, and was generally

much less

5 Velocity of Approach —The ordinary formula for weirs with

5 Velocity of Approach —The ordinary formula for weirs with velocity of approach are

$$Q \approx \frac{3}{4} c l \sqrt{2j} (H + nh)^{\frac{3}{2}}$$

$$\approx m l \sqrt{2j} (H + nh)^{\frac{3}{2}} ... (11)$$

By using a variable co-efficient of correction e, we of tain the inclusive co-efficients C=ee, and M=ie.

The formule with inclusive co-efficients are

$$Q = \frac{3}{3}CI\sqrt{2g}H^3$$

$$= MI\sqrt{2\pi}H^3$$
(42)

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For weirs in thin walls with complete contraction equation 42 is not ordinarily suitable, because while the values of c are known and tabulated those of C are not known, and if calculated for many different values of v would fill a formidable set of tables. But for other kinds of weirs C is often known as well as or better than c. In these cases, and also in cases where C is to be measured for some particular weir, and the co-efficients ascertained and recorded, equation 42 is eminently suitable

Where e is not known the use of  $e_e$  renders the adoption of the indirect or tentative solution unnecessary in certain cases, and so saves trouble (see examples 1 and 5). It is not convenient to give a formula, as in the case of orifices (equation 22, p. 48), for calculating  $e_e$  because equation 11 gives Q and not r. In order to find e it would be necessary to separate e into  $e_e$  and  $e_m$  and these quantities are not properly known. Values of  $e_e$  have, however, been found by working out various cases, and are given in tible xim for two values of e. Others can be interpolated if required. The excess of  $e_e$  above 10 is nearly as  $e^*$ , and for a given value of e nearly as n. The co-efficient  $e_e$  may be used either for solving ordinary problems of for obtaining values of e from e or n from M is as

follows —

Therefore from equation 42  $\frac{t^2}{2gH} = \frac{M^2l^2H^2}{l^2} = M^2 \frac{a^2}{A^2}$  (42a)

But 
$$Q = ml \sqrt{2j} \left( H + n \frac{v^3}{2g} \right)^{\frac{1}{2}}$$
  
 $= ml \sqrt{2g} H^{\frac{1}{2}} \left( 1 + n \frac{v^3}{2gH^2} \right)^{\frac{1}{2}}$ 

Since the last term in the brackets is small compared to the first term, the expression in brackets is nearly equal to  $1 + \frac{3}{2}n \frac{t^2}{2fH}$ 

Adopting this value and substituting from equation 42A

$$Q=ml\sqrt{2g}H^{\frac{1}{2}}\left(1+\frac{3}{2}nH^{\frac{1}{2}}\frac{a^{\frac{1}{2}}}{l^{\frac{1}{2}}}\right) \qquad (43)$$

From equations 42 and 43

$$1 = \frac{M}{1 + \frac{3}{3} \pi M^{\frac{1}{3}} \frac{a^{\frac{1}{3}}}{f^{\frac{1}{3}}}} \tag{44}$$

It is of course impossible to observe either is or a directly

observations give M directly, and either m or n can be found by assuming a value for the other Generally m is assumed or deduced from its values for a similar weir with no velocity of approach, and n is then calculated When the length of a weir is the same as the width of the channel of approach and G is the height of the weir equation 44 becomes

$$m = \frac{M}{1 + \frac{3}{2}nM^2 \frac{H}{(G+H)}}$$
 (15),

and in this form is given by Bizin

On the assumption that the effect of the energy due to the velocity of approach is the same as that of raising the water level by a leight AA (Fig. 71) equal to  $\frac{t^2}{2q}$ , the discharge is the same as that through an orifice with heads AA and KE, and the old form of equation was

$$Q = \frac{2}{3}cl\sqrt{2J}\left\{ (H+h)^{\frac{2}{3}} - (h)^{\frac{2}{3}} \right\},\,$$

which is similar to equation 35, p 70 This equation cannot be of the true theoretical form, chiefly because the original weir formula (equation 11 p 15) is not so It would, however, be right to use it as the best attenpt at a theoretical formula, if there were any advantage in doing so last term hi is generally small and often minute, while the farmula is m re complicated than equation 12 The method of allowance for a is largely empirical, and it is better to use the more simple formula 12. With this formula n might be expected to be somewhat less than unity

From article 7, chapter in it is clear that for weirs with velocity of approach the contraction may be either perfect or imperfect When it is imperfect the increase of discharge is due partly to the energy of the water represented by  $\frac{x^2}{2L}$  and partly to reduced contraction due to smallness of the margin. The value of n from both causes combined has been found to be, for weirs in thin walls, from 10 to 25 Smith rightly separates the two causes, and, discussing various experiments concludes that n should be 1 ! for weirs with full contraction, and 1 33 for weirs with no end con tractions The effect of reduced contraction, if any, was estimated separately, but the allowance made in the cases of weirs with no end contractions was not quite suffi ient according to the rules given in article 3 alove, so that n was a little overestimated and Smith himself suggests that this may be so Since Smith wrote, the results of Bazin's experiments on weirs with no end contrue tions have appeared. Owing to their general regularity and extent they are entitled to great weight. In analysing them en

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Smith's principle it is found that n varies from 86 to 137, and averages about 11 For moderate electries of approach Q depends only a little on n (see table xiii), and it is not worth while to give here the detailed analysis <sup>1</sup> Bann himself gives 154 as the mean value of n, but this includes the effect of reduced contraction Both sets of experiments, namely Bann's and those discussed by Smith, include high velocities of approach, the ratio  $\frac{\mathcal{A}}{a}$  being sometimes only 16 For weirs with full contraction the experi

sometimes only 16 For weirs with full contraction the experiments discussed by Smith are not numerous, and his resulting figure 14 somewhat doubtful It seems high in comparison with the others, and may be put at 133

The variations in n, and especially its exceeding the value 10 are not

easy to explain. A weir is usually in the centre of a channel, and the average deflection of the various portions of the approaching stream is then a minimum, especially if its greatest velocity is also in the centre, so that a large proportion of the water flows straight. In a weir so placed n will be a maximum, but this is no reason for its being greater than unity The whole of the water, and not only the quickest water has to pass over the weir At the approach section the velocity distribution (chap. ii art, 21) is normal. The total energies of the various portions of the stream may (chap in art 10) exceed the energy due to a, but the differ ence is probably only a few per cent, and nothing like 33 or even 20 Moreover, some little energy must be lost in eddies between the approach section and the weir Thus in no case will the available energy appreciably exceed that due to  $\frac{t^2}{2a}$  A high velocity of approach does not of itself reduce contraction. The high velocity occurs in the portion EB (Fig. 71) as well as in AE With an orifice in the side of a reservoir a high velocity does not cause reduced contraction, but rather the contrary The surface curves for wears do not indicate any reduced surface contraction when r is high. Peduction of the clear margin is allowed for separately and there are high values of n for cases in which the clear margin is ample

due to the incorrect form of the equation used If a curved crest FC is added, the flow will not be appreciably affected, but the head will now be H instead of H. The co-efficients of the two weirs must be such that  $cH^{\frac{1}{2}} = c'H^{\frac{3}{2}}$ . Suppose A now reduced so that r becomes considerable then  $c(H+nh)^{\frac{3}{2}}$  must equal  $c(H+nh)^{\frac{3}{2}}$ , and this occurs when n=n H. If c is 60 and c is 80 (values likely to occur in practice),  $H = \frac{n}{H} = 1$ . Thus it

It is probable that the deviations of n from unity are chiefly

1 It will be foun I in Appendix A.

can be seen how imperfections in the formula may cause n to change, and also that for a weir with a sharp edge n is greater than for a rounded weir

The following values for n seem suitable for weirs situated in the centre of the stream —

	Weirs witl end contractions	Weirs with out end contractions
Weir with sharp edge,	1 33	1 2
Rounded weir,	11	10

For other kinds of weirs the value can be estimated. For a weir not in the centre a reduction can be mide. When the edges are sharp, and the margin insufficient for complete contraction, an additional allowance for this must be made by the rules of article 3

## SECTION II -WEIRS IN THIN WALLS

6 Co efficients of Discharge -The chief experiments on weirs in thin walls, except Bazins, have been analysed by Smith, who has prepared tables of the values of c at which he arrives, and his results somewhat condensed are shown in tables xiv to xvi, but he notes that when II is less than 2 foot the figures are not reliable The first part of the following statement gives an abstract of Smith a results (except for very short weirs), disregarding decimals of 001 or 002 The figures marked \* Smith considered doubtful, owing to the absence of observations for such cases For the others he gives the probable error as only 3 per cent It is of course known that end contractions reduce the discharge, and that their effect increases with H and decreases with I Smith in his analysis considers all the experiments (except Barms) mentioned in article 1-those with and those without end contractions and those having various degrees of contraction-together, and to a certain extent infers one set of values from the other

Brain's extensive observations, already to some extent discussed in article 5, give results differing somewhat from Smiths. They are shown in the lower part of the above Interment. Smiths resplicitly for any weir without end contractions attain a mini-

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mum as II increases and then increase, but Barin's decrease as long as II increases. Smith's co-efficients increase as I decreases, but Bazin's are constant. The discrepancies are not very large, and they occur chiefly for small heads, but they are important because of the different laws which they indicate, and because of

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	
Kind of		l	Length of Weir in Feet							
Weir	Head	1-64		33	s	6-6	10	19	Remarks	
Full Con- traction	10 25 50 10 14 17		65 -62 605 59 58	65 623 61 595 59		65 625 615 605 60 50	655 635 615 61 60 60	635 63 615 61 61 605	Smith s Co efficients	
No End Contrac- tions	10 -25 50 10 14 17		64* 635* 65*	64* 635* 64* 645*	66 635 625 635 64 645	66 635 625 63 63 635 64	66 63 62 62 63 63	635 63 62 62 62 62 625	Smith's Co- efficients	
No End Contrac tions	10 25 50 10 14 17	66 64 63 63 625		66 64 63 63		66 64 63			Bazin s Co- efficients	

the high standard of accuracy obtainable with weirs in thin walls. The methods used for observing the head are described in chapter viu article 6. The measuring sections of Francis and Fteley and Stearns could not have come within the surface curve, but it seems possible that the erratic pressures (art. 4) may have had some effect. Bazin's measuring section was far enough away to avoid this, and jet not far enough for the surface fall to cause over estimation of H. Bazin's arrangements for starting and stopping the flow, and for measuring the volume discharged, were not quite so good as those of the American observers, and his individual experiments show more fluctuation among themselves, but the

can be seen how imperfections in the formula may cause n to change, and also that for a weir with a sharp edge n is greater than for a rounded weir

The following values for n seem suitable for weirs situated in the centre of the stream —

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For other kinds of weirs the value can be estimated. For a weir not in the centre a reduction can be made. When the edges are sharp, and the margin insufficient for complete contraction, an additional allowance for this must be made by the rules of article 3

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(1)	(2)	(3)	(4)	(8)	(6)	(7)	(6)	(9)	(10)
Kind of				Length	of Weir	in Feet			
# cir	Head.	144	2	33	3	6-6	10	19	Remarks,
Full Con- traction	10 -25 50 10 14 17		-65 -62 -603 -59 -58	-65 -625 61 595 59		625 615 605 CO	635 615 61 60 60	635 63 615 61 61 61 605	Smith s Co- efficients
No End Contrac- tions	10 25 50 10 14		64* 635* •65*	64° 64° 645°	66 -635 625 635 64 645	66 635 62, 63 637 64	66 63 62 625 63 63	635 62 62 62 62 625	Smith's Co- efficients
No End Contrac tions	10 25 50 10 14 17	66 64 63 63 625		66 64 63 63		60 64 63			Bazin's Co- efficients

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number of his observations was far larger, and his figures when averaged are remarkably consistent

On the whole it seems that Bazin's results are probably more accurate than the others, and the use of his co efficients for wers 15 to 7 feet long, and without end contractions, is recommended For longer wers there is nothing to shake Smith's figures Decrease of  $\epsilon$  with increase of l may seem improbable, but it is quite possible It may, for instance, be due to the surface at the measuring section being higher at the sides than elsewhere. The head is measured at the side, and this would make H seem to be greater than its real average value from side to side of the stream, especially for long weres

The detailed values of Bazin's coefficients given in table virtues, owing to Bazin's values of n not being accepted (art 5), slightly higher for the greater heads than the values arrived at by Bazin himself. They accordingly differ less from Smith's figures. Bazin calculated c, or rather m, for heads ranging from 16 to 197 feet, but his actual observations were within the range shown in table xvi. Bazin also gives a complete table of the values of M, and from it table xviii giving values of C has been framed

It has been found that when there are no end contractions the sheet of water after passing the crest of a weir tends to expand laterally, except when H is less than 20 feet, and the side-wills have usually been prolonged downstream of the crest, openings for free access of air beneath the sheet being left. If the sides are not so prolonged  $\sigma$  will be increased about 25 per cent when  $H = \frac{1}{10}$ , and more or less as H is more or less. It also appears that in such weirs moderate roughness of the sides of the channel

that in such weirs moderate roughness of the sides of the channel has no appreciable effect on the discharge

For small wers of triangular section in thin walls, with the apex a right angle, c has been found to be 617

7 Laws of Variation of Co efficients — The following laws, governing the variation of the co-efficient for complete contraction, are apparent —

(1) When the length of the werr is 216 feet or more, c is a minimum when I is equal to II or thereabouts, that is, when the section of the stream is nearly square, and is increases as the section deviates from a square. The deviations are all in

the direction of increase in H

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(2) When l is less than 216 feet deviation from the square section is due to decrease in  $\frac{l}{H}$ . The coefficient c does not

increase with the deviation, and for the smallest weirs it decreases

(3) For sections of the same shape e is less as the section is

greater

(4) The value of c is less or greater than for an orifice of the same size and shape according as the length of the weir is greater or less than 246 feet

Laws (1) and (3) are the same as for ornices and are due to the same causes. As to law (4), having regard to the remarks made above (vrt. 5) concerning the defective form of the weir formula, it is clear that the two sets of co efficients could not be expected to agree. The reasons for law (2) are not known. It is not certain that it applies to any except very small weirs.

8 Flow when Air is excluded — With four weirs in thin walls, of heights 246 feet, 164 feet, 115 feet, and 79 foot, further observations were made by Bazin, the access of air beneath the falling sheet being prevented by the closure of the openings which had been left for that purpose The following statement shows the results noticed The pressures under the sheets were observed, and the discharge was found to increase as the pressure decreased

An interesting point for consideration is the conditions under which the different forms are assumed. This is stated by Bazin, and is shown in the above statement with which wers not exactly similar to those of Bazin, it may be difficult to say when the various changes will occur, but it will at least be possible to foresee them and to take some account of them when they do occur. The occurrence of the form called 'drowned underneath' will obviously be affected by the condition of flow in the down stream reach. One lesson to be learnt is, that if complications are to be avoided and discharges accurately inferred the free access of air under the sheet is essential

#### 9 Remarks -

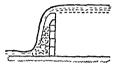
For a given weir in a thin wall c decreases as H increases the effect of the end contractions increasing with H. I that seen stated that if the site are given a slope of \(\frac{1}{2}\) to \(\frac{1}{2}\), c is constant for all heads the sloping sides having the effect of lengthening the weir as H increases. This has however, been proved to be true only for some weirs whose length of crest did not exceed 1 foot. In order that for a given weir c may be constant for all heads the side is more likely to curred than straight, and it is unlikely that its general slope will be the same for weirs of different length

Reference to Fig	Name given to Case by Bazin	Description of Case	Conditions under which it occurs	Affect on the Co efficient of Discharge, C
Fig 72	Adherent sheet	Sheet in con tact with weir and no air under it, or it may spring clear from the inconsistence of air, and then ail here to the plank, or it may adhere to the top and bevelled edge and then spring are as in the case following		C may possibly execut that for a free sheet by 33 per cent
lig 73	Depressed sheet	Air partly exhausted by the water and at less than atmo	When case 1 does not occur, or when it oc curs and H is	C is higher than for free sheet, generally only slightly, but it may be 10 per cent higher when a contract to point of as m 'drowned
	ļ ,		, ,	·
Fig 71	Sheet drowned under neath	Water under sheet rives to level of crest and all air is expelled (a) Il accata distance	creased so that  II is not less than about 4G  When the fall H <sub>1</sub> +H <sub>2</sub> is greater than about 3G	Value Value of Conf.
Fig 75		of sheel	When the fall H <sub>1</sub> +H <sub>2</sub> is not greater	The level of the tail water affects the discharge, and approximately $\frac{d^2}{dt^2} = (105 + 15\frac{H_2}{H_1})$ (40) See also article 13

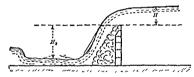
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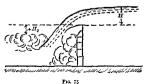
Fra. 72.



Fra. 73.



Fra. 74



110. 1

Francis found that end contraction might be allowed for by considering the length of the weir to be reduced by 20H, that is, by substituting (l-2H) for l in equation 11, page 15. He found that with the formula thus modified, the co-efficient, provided l is not less than 3H or 4H, is nearly constant, its value being 620 to 624, and averaging 623 for heads ranging from to 19 inches. Results obtained by this formula are hable to differ by l or 2 per cent from those of the ordinary formula with Smith's co-efficients. Francis' formula is specially mentioned here because it is well known.

Bazin, taking mean values of M and  $n_1$  puts equation 45 (p 83) in the form

$$m - \frac{M}{1 + 55 \left(\frac{H}{G + H}\right)^{\circ}} \tag{47}$$

But he admits that simplicity is obtuined at some expense of accurroy. His value of n, as shown above (art 5), is not correct, and this formula should not be used as a general one. For Bazin's own experiments it is fairly accurate, but there is no use for it since his co-efficients c and C are tabulated. Bazin also states that m may be taken as  $\frac{405}{H}$  (H being in metres) and this agrees closely with his values of N, but as these have now been slightly altered the equation does not agree with them

#### SECTION III -OTHER WEIRS

10 Weirs with flat top and vertical face and back.—Gener illy
the water at B (Fig 76) holds back that upstream of it, and the
discharge is less than for a weir in a thin will under the same
head. It is a soit of drowned



weir, B being the full water level. At A there is eddying water. When H is about 16W to 2W—N' being the top width—the sheet springs clear from the top, and the case becomes a weir in a thin wall. But if the sheet nearly



10 "7

touches at C (Fig. 77) the water gradually abstracts the air, and the sheet is pressed down, touches at C, and Q is slightly greater than for a weir in a thin will. Table xin (prepared by Frele, and Stearns) shows the corrections to be applied to c, the co-efficient for weirs in thin will, in order to give c, the co-efficient for weirs with flat top and vertical face and lack. The corrections apply

$$\frac{C_{p}}{C} = 70 + 165 \frac{H}{H^2} \qquad (44)$$
 The results given by this formula agree with the observed results

generally within about 2 per cent., but for the wilths of C 56 feet, 2 C2 feet, and I 51 feet the errir may be 3 or 4 per cent. They also agree with Fieles and Stearn's results within I or 2 per cent. When H was increased to about 2H the sheet spring clear, but if H was gradually lowered the sheet remained clear till H was about 16H. Between these limits it was unstable. When the sheet springs clear the above formula of course is not needed. The thick lines in the table mark off the cases when H was less than 2H. While H varies from  $\frac{3H}{2}$  to 2H, the ratio  $\frac{C}{2}$  may change

2W While H varies from \(\frac{1}{2}\) to 2W, the ratio \(\frac{1}{6}\) may chang from 98 to 1.07 if the sheet remains attached to the crest.

When air was excluded depressed and drowned sheets occurred under somewhit similar conditions to those with weirs in this walls. Remarks regarding them are given in table xix. Their occurrence sometimes preceded and sometimes succeeded that of detachment of the sheet from the lack or top of the weir, and rendered the conditions very complicated.

rendered the conditions very complicated

11 Weirs with sloping face or back.—Bazin's chief results for
weirs of this class are given in tables xxi and xxii, and the

<sup>1</sup> Transactions of the American Society of Civil Ingineers, vol xliv

Cornell results are included Table XXI contains the cases where the back of the weir was steep, so that the sheet generally sprang clear of it Apparently no air openings were left, and the adherent depressed and drowned sheets often occurred Table XXII shows the cases where the back slopes gradually In these last the streum flowing down the back is in uniform flow in an open channel Weirs of this kind with back slopes about 10 to 1 are used on some large canals in India and termed 'Rapids,' the profile of the water surface being as sketched in Fig 68, page 82 The flow at the crest is virtually that of a drowned weir At the foot there is a standing was e (chip xii at 11)

In weirs of these classes there are several variable elements. Pairs of cases in the tables can be compared in which only one element varied, so that its effect can be traced. By studying these cases and the tables generally it will be seen that C generally increases as the height of the weir decreases, as the top width of the weir decreases (but not so much for the greater heads), as the upstream slope is flattened, and as the downstream slope is made steeper. For a weir with slopes of face and back both 3 to 1 and sharp top, C has been found to be 51 and 43 for heads of 25 feet and 10 feet respectively.

12 Miscellaneous Weirs — For a weir made of plank with a rounded crest of radius L the discharge with head II is about the same as for a weir in a thin wall with a head II The following

table is given by Smith 1 -

		Values of 1	
11	25 in	J0 in	-4 in
_		Values of H' - H	
116	006	004	003
166	014	013	015
217		021	018
284	011	029	028
351	015	028	039
41	014	028	044
49	015	-030	052

The chief results of the Bazin and Cornell observations on rounded weirs are given in table ax

<sup>1</sup> Hy trailers chap v





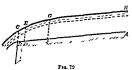


a. 78 Pro 7S1 Pro 7

For a weir formed entirely by lateral contraction of the channel, and having a crest length of 2 feet to 6 feet (Fig. 82, p. 107), c is 65 to 73 and C is 70 to 78, being greater for the larger sizes

For a fall (Fig. 79) in which there is neither a raised weir nor a lateral

contraction there is no local reduction of the approach ing atream due to eddies or walls, and therefore no local surface fall of the kind ordinarily occurring The surface curve is due to draw (chap il art. 11) If the alope AB is not very steep the curve extends for a great distance



If I' is the velocity at DE near to BC, then I' is both the velocity of approach and the velocity in the weir formula, so that

$$V^2 = 4c^2 2g \left( H + n \frac{V^2}{2g} \right)$$
  
 $V^2 = 4c^2 2g H + 4nc^2 V^2$ 

If 
$$c = 79$$
 and  $c^2 = 63$  and  $n = 1.0$ ,  

$$V^2 = \frac{^{\circ}28}{1 - ^{\circ}28}c^22gH$$

or  $V'' = \{c^2QH + inc^2V^2\}$   $V''(1 - \frac{1}{2}nc^2) = \{c^2QH\}$ . If the channel AB be supposed to be very smooth or steen the water surface

HG will be parallel to the bed, but there will always be a short length GG in which draw will occur Falls of this kind occur at the ends of wooden troughs and shoots. They were used on one of the older of the great Indian canals, but the high velocity due to the draw caused such scour and damage that rasted wers had to be added

#### SECTION IV -SUBMERGED WEIRS

13 Weirs in Thin Walls—The following statement shows the chief experiments which have been made

	•							
ĺ	Observer	Length of Weir	Upstres H	m Head 1	Downstre		Height of Weir	l
			From	То	From	To		
	Francis, Fteley and Stearns, Bazin,	1 eet. 11 5 6 56	Feet. 1 0 33 •19	Feet. 2 3 '81 1 49	Feet 24 07 79	Feet. 1 1 80 1 26	Feet 5 8 3 2 8 to 2 5	

The weirs were all without end contractions The level of the tail water was measured measurements difficult

at M (Fig 80), which is theor etically wrong, the surging of this water renders exact co efficients for submerged weirs are not, in most cases. well known, and exact results cannot be expected them

Let q, be the discharge through AB and q, through LC

Hoth, be heights of A + M alone P Then  $q_1 = \frac{2}{3}c_1l\sqrt{2aH}$  H

$$q = c_2 l \sqrt{2gH} \quad H_2 \tag{50}$$

If c has the same value for both portions,

$$q = \frac{2}{3}cl\sqrt{2gH}\left(H + \frac{3H_{2}}{2}\right)$$
 (51),  
or  $q = cl\sqrt{2gH}\left(H_{z} + \frac{2H}{3}\right)$   
or  $q = cl\sqrt{2gH}\left(H_{1} - \frac{H}{3}\right)$  (52)

The last two formule are those for an orifice having a height equal to the downstream head plus two thirds of the full there is velocity of approach H+nh must be put for H and  $H_1+nh$ for  $H_1$ , but  $H_2$  is left unaltered

Francis makes  $c = 921c_1$ , that is, he multiplies  $H_2$  in equation Smith, discussing the experiments of I rancis and Fteley and Stearns, and reviewing a previous discussion by Herschel, substitutes 915 for 921 and recommends the formula-

$$\mathcal{G} = c_1 \sqrt{2g} \left( H + nh \right) \left( 915 H_2 + \frac{2 \left( H + nh \right)}{3} \right) \tag{53}$$

This formula is for weirs in thin walls without end contractions c, is the co efficient taken from table wi for the equivalent weir with a free fall (that is, the weir with a free fall giving the same discharge) and n is 1 33 The formula may le applied to weirs with end contractions and the same co efficients used if I- 2H, b substituted for I

If Q is the discharge for a free weir, and if H, remains constant while the tul water is raised by some cause operating in the Writs 101

downstream reach, Q decreases very slowly till  $H_1$  is about  $\frac{H_1}{L}$ . The discharge through AB is the same as before, while the velocity in PG is altered in the ratio  $\sqrt{\frac{H+\lambda H_1}{H}}$ . The relative discharges are as follows, c being constant and velocity of approach being supposed to be negligible—

Practically, this law is somewhat modified. Let it be supposed that for the free weir there is ample access of air. As the tail water rises above the crest the air is shut out. The under side of the sheet springs up to a somewhat higher level than the crest, but the surging of the tail water shuts out the air almost at once. The sheet of water is pressed down, and the discharge instead of decreasing increases a little. Practically it remains nearly constant during a certain rise of the tail water and then decreases. If the air passages become obstructed just before the tail water rises to the crest level, Q will begin to increase then, but this does not necessarily occur. Neither equation 52 nor 53 takes account of the increase in discharge when the tail water rises above the crest. If the air was shut out from the commencement, Q begins to decrease as soon as the tail water begins to rise. See equation 46, page 94.

Bann uses the simple weir formula  $q=C_d\sqrt{2gH_1}$  (where  $C_d$  is the inclusive co-efficient for the drowned weir and  $H_1$  the upstream head) and finds the ratio  $\frac{C_d}{C}$ . C being the inclusive co-efficient for the 'standard weir,' 3.72 feet high with a free fall and with the same head  $H_1$ . His results are as follows —

$\frac{H_2}{G}$ or			-	H 7 or R	atio of	Fall i	n Wate	r to B	leight	of Wel	r		
Ratio of Down stream	05	10	15	70	-25	30	35	40	45	50	60	0	F*
Head to Height of Weir		Rat o c4											
0	1 05	1 05	1 05	1 05	1 05	1 05	1 05	1 05	1 05	1 05	1 05	1 0ა	1 06
05	84	93	96			1 01	101				1 03	104	1 05
10	74	85	90	94	96	97	98		1 00	1 01	1 02		104
15	68	80	86	90	92	94	96	97	98	99	1 00	1 01	1 03
20	64	76	82	87	90	92	94	95	96	98		1 00	1 02
30	58	70	77	82	86	88	90	92	94	95	98	99 98	1 00
40	54	66	74	79	82	85	88	90	92	93	96	96	97
60	50	61	69	74	78	81	84	87 84	89	90	92	94	95
80	47	58	66	71 69	75 74	79 77	82 80	83	87 85	89 87	91	94	94
1 00 1 20	45 44	57 55	64 63	68	72	76	79	82	84	87	90	93	93
1 50	43	54	61	67	71	75	78	81	84	86	89	92	92
1 30	*3	34	101	01	11	10	10	91	0.	00	00		3-
* This at a distant	nce (aı	-	c ·	. ,	Ca		ıs bel					nd ng v	

\* This column shows  $\frac{G}{G}$  when it stail water is below the crest and the stand rg ware is at a distance (art 8).

Actually the ratio  $\frac{G}{G}$  is somewhat different with the weirs of different heights for the same values of  $\frac{H}{G}$  and  $\frac{H}{G}$ , but the error in the figure given is usually only 1 or 2 per cent, except for very small values of  $\frac{H}{G}$  and  $\frac{H}{G}$  and in these cases the ratio is always uncertain. The values 1 05 in the first line of the table agree with the figure obtained by equation 46 (p 94), when  $H_1=0$  If, for any given weir, G is supposed to be 1 0, the above figures show  $\frac{G}{G}$  for various values of H and  $H_2$ . In this case, for a given value of  $\frac{H}{H_2}$ , the figures are high when H is high. This is due to velocity of approach, the standard weir having been high

Bazin's figures may be compared with those given on page 101 Take for instance the cases where  $H_*=2H$ 

$\frac{H}{G} = 70$	50	30	10	05	_
G = 140	1 00	60	20	10	The figures on p 101 are 77 and 71
$\overset{C_d}{C} = 93$	87	81	76	74	ana 71

101

Again for the case where  $H_1 = \frac{H}{3}$ 

WFIRS

In the above case, where  $\frac{H}{G} = 70$ ,  $\frac{H_s}{G} = 210$  and  $\frac{d}{A}$  or  $\frac{H_s}{G + H_1} = \frac{21}{31}$ . The excessive velocity of approach accounts for the high value of  $\frac{G}{G}$ .

Bain found that when H is reduced to about 160 or 210, the sheet, instead of plungug beneath the surface (Fig. 76), auddenly assumes the form shown in Fig. 80 (which he terms the 'undulating' form, there being generally waves near M) but this does not affect the co-efficient. If H is now gradually increased, the undulating form remains till H is about 2NG or 29%, but is unatable or liable at any moment to revert to the other form 2.9 %.

14 Other Weirs —The results of Bizins observations on weirs of other lands are shown in the following table. Instead of giving the coefficient ratios Bazin gives the equivalent heads. The conditions of flow are complicated in such cases, and formulae can probably apply only with the coefficient varying to a great extent. The height  $H_1$ , to which the tail water can rise before it begins to affect the discharge, varies greatly for different weirs. For a weir in a thin wall it is very small, and it is largest for weirs with flat tops. For the weir No. 5 in the table  $H_2$ , was  $\frac{3}{2}H_1$ . For weirs with a sharp top it was minus, zero, and plus for downstream slopes of 1 to 1, 3 to 1, and 5 to 1 respectively, the flat downstream slope in the last case having the same effect has a large top width. For weirs with flat tops 66 foot wide, back slopes varying from 2 to 1 to 5 to 1,  $H_2$  is nearly  $\frac{H_1}{2}$ , but when the

top was 1 32 feet wide H, was  $\frac{2H_1}{3}$ 

	Dime	nsions	of the W	eira	#	1_	schar indard inbic n	ges pe Ne r netres	r foot 1 in Tl it per sec	un of Wall cond	
1					135	06	ı   n	0 1 16	9 31	0 480	1
Refer ence Num ber	1	Top width		etres	Downstream Head	He	ads ff	on S metr	tandar	1 We r	Remarks
uer	Down stream	width	Up stream	I A	l st s	10	15	1 20	30	40	1
	Slope	me tres	Slope	Height in metres	Pod		respor	nding l	Heads	H <sub>1</sub> on	
<u> </u>	<u> </u>	<u> </u>		<u>  =</u>	1	_			irs ne		<u> </u>
1		1		1	1-	erra M	_~		ce or l		1)
1	1 to 1	0.0	Vert	75	L*	6	14			36	H <sub>1</sub> <h for<="" td=""></h>
1	1 50 1	00	cal	13	06	1	16			38	the greater
, ,	ļ	<u> </u>	)	}	12	Į.	18	22		40	discharges
_					24	ļ.	-	-	35	43	and when
	,	2	l to I	75	£*	1	16	21	29	37	II218 small
2	1 to 1	"	3 (0 1	10	24		1"	27	32	39	
				<u></u>	E*	!-	16	21	31	42	í
3 (	5 to 1	0.0	Verti	75	12	(	(17	21	(	( (	1 1
1 .1	0.001	00	cal	,,,	24	l	ł	27	33	45	1 1
					36 E*	_	17	-	31	41	1 1
!					12		17	22	31	41	1
4	5 to 1	2	⅓ to 1	79	24	ŀ	ļ -·	]	33	41	$II_1>II$
				_	36	_	L	_	<u>L</u>	42	
					Wen	with	flat to and	p and back	vertica	l face	<b>1</b> [
1 1					12	14	18	i	Γ.		1
5		20		75	24		}	27	35	1	}
<u> </u>	]				36		<u>                                     </u>	<u> </u>	40	;	(
			ł		E*	12 14	17   18	21 22	29 31	38	) [
6		2	-	75	24	14		28	34	41	
1 1		'	- 1	Į	36				41	- 11	For small discharges
i				Ì	E*	12	17	21	29	37	$H_1 > H$
7	1	2		35	12	13	17	22	30	39	For greater
		1			36				41	\	discharges
		;			1 * T	11	15	19	27		when H, 12
8	)	1		75 !	12	14	18	22	31 35	13	emall a l
					24	11	1-	19	27	37	$H_1 > H$ when $H_2$ is
	1	ı			12	14	17	21	28		larger
9	í	1		35	24	- 1	1	33	36	40 [	- 1
l ł	1	1			36		- 1		- 1	44  )	

WEIRS 105

Hughes, adopting equation 51 with n=1, has worked out 1 the values of c for wers Nos 5 and 6 on the above list, and the results condensed are as follows —

Discharge in		Welr \a. 5		[	Weir to 6	
per second	II1 metres,	H <sub>2</sub> metres.	e	II <sub>1</sub> metres	II3 metres	,
-061	122 122 161	-031 091 150	50 70 87	119 123 135 163	-000 -090 120 150	50 67 85 74
169	-236 -247 -293	151 211 271	61 81 84	216 -219 -220 -233 277	-000 -060 120 180 240	56 56 63 74 72
310 {	353 360 396	-242 303 361	63 80 88	301 307 319 413	000 120 210 360	61 63 71 72
392 {	409 418 439	300 360 389	68 83 84			
450 {				382 384 406 442	000 060 -240 300	65 63 70 68

It will be seen that e increases rapidly with  $H_z$ , and apparently attains a maximum and then decreases

The effect of a submerged were varies greatly according to the state of the discharge. With low water it may act as a free weir, and have great effect, for however smill the discharge may be, the upstream water surface must be higher than the top of the weir. With larger discharges the heading up is less, and with a great depth of water the weir may be almost imperceptible.

15 Contracted Channels—These are (chap ii arts 6 and 19) analogous to submerged weirs—The co efficients are very roughly known—When an open stream issues from a reservoir, or from a

Weirs

known When an open stream issues from a reservoir, or from a

Madras Government Paper on Bazin's New Experiments on Flow over

larger channel, or passes between contracted banks, or bridge abutments, or piers, c may have any value from 50 to 95, being smallest when the angles of the apertures are sharp and square (especially if there is a decrease in section both vertically and laterally), greater if the angles are chamfered or curved, and greatest when there are bell-mouths. The co efficients are also greater for large than for small openings 1

When a bridge or other obstruction in a stream has a waterway less than that of the stream the real obstruction is generally much less than it seems to be It is to be measured, not by the difference between the waterway at the obstruction and that upstream of it, but by the difference in the upstream and down stream water levels. This is very often meonsiderable A fail of 1 foot gives a theoretical velocity of 8 feet per second, and 25 foot gives 4 feet per second. Bridges are sometimes un necessarily altered or rebuilt owing to 'obstruction' which is nearly harmless. Heading up is most likely to be considerable with high discharges, because the mean width of the channel is then increased, while perhaps that of the contracted place is not thus the effect varies in just the opposite manner to that of a submerged weir.

The real objection to a contraction is very often the expansion which succeeds it and the eddies and scour which occur (chap ii arts 17 and 23, and chap vii art 1)

#### SECTION V -SPECIAL CASES

16 Wers with Sloping or Stepped Side-walls —For n were of triangular section the formula is obtained by putting  $H_i=0$  and L=l in equation 36 (p. 71) Thus—

$$Q = \frac{4}{15}c\sqrt{2g}lH^{\frac{3}{2}} \qquad (54)$$

Since l increases as H, in any triangular weir in which c does not vary greatly, Q is nearly as  $H^3$ , that is, it varies much more rapidly than with an ordinary weir. If two weirs, one triangular and one rectangular, are so designed (Fig. 81) as to hold up the water of a stream to a given level with ordinary supplies, the triangular weir will allow floods to pass with a smaller head. This applies to any weir with sloping sides. The triangular form

<sup>1</sup> The co efficients for narrow openings are, roughly, for sparse piers, 6; obtuse angled, 7, curved and acute, 8 For wiler openings add 1

is suitable for small drains. By making the sides of a weir at any given level DP (hig. \$1) horizontal, and extending them uniwards, the rise of the water above DP can be limited.



The formula for the discharge of a trapezoidal weir (Fig. 92) is



obtained by putting H = 0 in equation 35 (p. 71) Thus-

$$Q = \frac{2}{3}c\sqrt{2\pi}H^{\frac{3}{2}}\{l_{1} + \frac{2}{3}(l_{1} - l_{2})\}$$
 (55)

The quantity in the outer brackets is the crest length of the equivalent ordinary weir. This length is less than  $\frac{h+h}{2}$  because

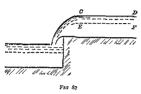
the velocity of the water at the bottom of the section is greater than at the top. If there is velocity of approach (H+nh) must be put for H in equation 55, or else C put for e. If r is the ratio of the side slopes, that is, the ratio of AB to BC, then AB  $= r = \cot a$ ,  $AB = rH = H \cot a$ , and  $I_r - I_p = 2rH = 2H \cot a$ 

Thus equation 55 may be written-

$$Q = \frac{3}{4}C\sqrt{2g}H^{\frac{3}{4}}(l_0 + 8rH) \qquad (56)$$

17. Canal Notches —A common problem on irrigation canals is to design a weir so that the water levels, CP, FF, etc (Fig. 83), upstream of it, corresponding to different discharges in the channel of approach, shall be the same as they would have been if the weir had not existed and the channel had continued uniform and uninterrupted. If the cross section of the channel of approach is transproadal, the form of the aperture will be approximately

trapezoidal, and its crest will be at the bed level of the canal Such a weir is termed a notch. It is usually, for convenience in construction, built exactly trapezoidal and of the form shown in Fig. 82, the hip being added to cause the falling water to spread



out and exert less effect on the downstream floor. In a large channel two or more notches are built side by side instead of one very large notch. The coefficients, so far as known, are given in art 12. If C is the same for all heads the true theoretical form of the \$20 hours remarked.

notch is curved, the angles at C, F (Fig. 82) being rounded. The slope of the sides is great for small depths because the coefficient for flow in channels increases rapidly for small depths, but if C increases fast with the head at small depths, as is highly probable, judging from other weir coefficients, the form is more neatly a trapezoid. To design the notch, find Q and q, the discharges (or the fractions of the discharges if there are to be several openings) of the channel for two depths D and d. Then from equation  $S^{B}$ 

$$l_{b} + 8id = \frac{q}{3C_{1}\sqrt{2gd^{3}}}$$
(57)  

$$l_{b} + 8iD = \frac{Q}{\frac{q}{3C_{1}\sqrt{2gD^{3}}}}$$
(58)  
Therefore 
$$8r(D-d) = \frac{Q}{\frac{q}{3C_{2}\sqrt{2gD^{3}}}} - \frac{q}{\frac{q}{3C_{1}\sqrt{2gd^{3}}}}$$
Or 
$$i = \frac{2}{8\sqrt{2g}(C_{1}Qd^{3} - C_{2}qD^{3})}$$
$$= \frac{C_{1}Q^{3} - C_{2}qD^{3}}{128(D-d)C_{1}C_{2}d^{3}D^{3}}$$
(59)

The depths d and D can be so selected as to make the notch specially accurate for any given range of depth. In irrigation canals (and still more in their distributaries) there is a certain minimum depth, d<sub>f</sub> below which the channel is not run. In such a case it does not matter if the notch is inaccurate for depths less than d<sub>f</sub>. To make its accuracy a maximum for depths between d<sub>f</sub> and any greater depth, D<sub>f</sub>, the range of depth should be divided

into four parts and the depths d and D taken at the quarter to nts. Thus if

$$D_1 - d_1 = 1$$

$$d = d_1 + \frac{1}{4}$$

$$D = d_1 + \frac{3!}{4}$$

If general accuracy is required over a range of depth from zero to  $D_0$  then  $d=\frac{D_0}{4}$  and  $D=\frac{\pi D_0}{4}$ . The formula are, however, most simple when D=2I. In this case equation 19 becomes—

$$\tau = \frac{C_1(t)! - 2 \cdot 2 \cdot 2 \cdot C_1 t^{\frac{1}{2}}}{4 \cdot 2 \cdot 3 \cdot C_1(t^{\frac{1}{2}})! \times 2 \cdot 2 \cdot 2^{\frac{1}{2}}} \\
= \frac{C_1(t) - 2 \cdot 2 \cdot 2 \cdot C_1(t)}{12 \cdot 10 \cdot C_1(t)!} \quad (60)$$

Substituting this value of r in 57

An I

$$\begin{split} I_{i} &= \frac{q}{\frac{q}{3}C_{i}\sqrt{-q}t!} - \frac{8(C_{i}(Q - 2.828C_{i}q))}{12.10C_{i}C_{i}d!} \\ &= \frac{2.262C_{i}q - 8C_{i}Q + 2.262C_{i}q}{12.10C_{i}C_{i}t!} \\ &= \frac{2.262C_{i}q - 1C_{i}Q}{6.92C_{i}C_{i}d!}. \quad (61) \end{split}$$

If C, and C, are each assumed to be equal to C,

$$r = \frac{Q - 2 \cdot 8287}{12 \cdot 10 \cdot 10^{1}}$$
(62)  
$$l_{s} = \frac{2 \cdot 2627 - 10}{6 \cdot 2874}$$
(63)

If it is desired to build a notch to the true form, that is not strictly traperoidal, the lower part corresponding to a small depth in the channel may first be designed traperoidal and the upper parts designed in instalments, working upwards

In deciding in which direction a notch is to deviate from the true form, and for what water levels accuracy is to be aimed it, regard must be had to the special circumstances of the case. If seour of the canal bed is feared or if there is difficulty, with low supplies, in getting enough water into the distributaries, the notch can be designed narrow.

If a notch is drowned its true form is modified. In Fig. 82 let

DE be the upstream water level when the tail water is just level with the crest CF. The portion CDEF of the notch obviously need not be altered. As the tail water rises above CF the discharge through the notch becomes gradually less than it would be for a free notch with the same upstream water level, and the upper part of the notch must be widened as shown by the dotted lines. In this case also a trapezoid can be drawn so as to closely agree with the true form. As before, the trapezoid can be designed so as to give nearly exact discharges for any particular range of depths, or the notch can be designed to the true form as above explained. The formulæ for a drowned notch are as follows. For an upstream depth d let  $q_1$  be the discharge through ADEG and  $q_1$  through DCFE

$$g = q_1 + q_1$$

$$= {}_{3}^{2}C_1 \sqrt{2g(d-h)}{}_{2}^{2}[l_b + 2rh + 8r(d-h)]$$

$$+ C_2 \sqrt{2g(d-h)}(l_b + rh)h \qquad (64)$$

For a greater discharge let D and H be the heights of AG and DE above CF Then

$$Q = {}_{\delta}^{*}C \sqrt{2g(D-H)^{\frac{3}{2}}}[l_{\delta} + 2rH + 8r(D-H)]$$
  
+  $C_{z}\sqrt{2g(D-H)}(l_{\delta} + rH)H$  (65)

If the upstream and downstream channels are similar in all respects d-h=D-H and D-d=H-h Let D=2d Then d=D-d=H-h and H=d+h Therefore

$$Q = \frac{2}{3}C_2\sqrt{2g(d-h)^{\frac{3}{2}}}[l_b + 2rH + 8r(d-h)] + C_2\sqrt{2g(d-h)}(l_b + rH)H$$
(66)

Subtracting 64 from 66 and putting  $C_1 = C_2 = C$  and  $C_1 = C_2 = C$ ,

$$Q-q=\frac{2}{3}C\sqrt{2g}(d-h)^{2}[2rd]$$

 $+C\sqrt{2g(d-h)}[l_b(H-h)+r(H^2-h^2)]$  (67) from which r can be found, and  $l_b$  can then be found from 65,

from which r can be found, and l, can then be found from or, Q and Q, being selected at such depths as to make the trapezoid most accurate at the points desired. If D is not taken as 2d, or if C, and C, differ, the equation will be complicated, and it may be easiest to adopt the instalment process and design the notch to the true curve, afterwards straightening it if necessary.

18 Oblique and Inclined Weirs—If r were is built obliquely

neross a stream the discharge is that due to the full length of the weir, provided the section of the stream passing over the weir is small compared to that of the stream at the approach section In this case the water approaches the weir nearly at right angles But when the stream is in flood, or when, under any circumstances, the two sections become more equalised, the water passing over the weir travels more nearly parallel to the axis of the stream, and the discharge over the weir tends to become could to that over a weir found by projecting the oblique weir on a plane perpendicular to the axis of the stream By making a weir extend from bank to bank of a stream with its alignment very oblique, so that its length projected on the axis of the stream is considerable, it can be made to offer less obstruction to floods, but its length is also increased so that it does not hold up low supplies so well The problem of constructing a weir so that it will hold up low supplies and yet not form a serious obstruction to floods cannot usually be solved by means of oblique weirs The only solution is to have a 'movable weir,' that is, gates or shutters which can be placed across the stream at times of low supply and removed or placed parallel to the stream in floods or high supplies

When the plane of a weir in a thin wall, instead of being vertical, is inclined, the co-efficients can be obtained by multiplying that for a vertical weir by a co-efficient of correction c<sub>4</sub>, whose value was found by Bazin to be as follows —

Inclination of plane of weir-

Upstream
1 to 1, 2 to 1, 3 to 1, vertical, 3 to 1, 3 to 1, 1 to 1 2 to 1, 4 to 1
Average value of c<sub>4</sub>—

93 94 96 10 1-04 107 110 112 109

The heights of the weirs when vertical were 3.72 feet, 1.64 feet, and 1.15 feet. The co-efficient is a maximum when the weir is inclined downstream at 2 to, that is, when the height of the crest above the bed is half the distance of the crest downstream from the base of the weir. The weirs were without end contractions, and the head ranged in each case from about 33 feet to 1.48 feet.

#### ELAMPLES

Example 1—A werr in a thin wall is 25 feet long and 3 feet high, and H is 1 foot The channel of approach is 30 feet wide Find Q

The crest contraction is complete, and the end contraction so nearly complete that no allowance need be made for it from table xii e is probably 612 From table xii  $q=35\times3$  275=81 88 cubic feet per second

To allow for v by the usual method,  $A = 30 \times 4 = 120$  square feet.

Let Q be assumed to be, say, 84 cubic feet per second. Then  $n=\frac{n}{n-1}=70$  From table 1 h=0076 Let n=13 Then nh=0101, H+nh=1010. The corresponding correction in  $(H+nh)^3$  and in Q is 15 per cent, and Q is thus 83 14 cubic feet per second.

To allow for i by table xiii  $\frac{A}{a} = \frac{30 \times 4}{25 \times 1} = 4.8$  When c is 60  $c_a$  is about 1 015 When c is 61  $c_a$  is about 1 016 This makes

Q=83 10 cubic feet per second Example 2—A river 50 feet wide has a maximum discharge of 600 cubic feet per second, the depth being then 3 feet. A were with a rounded crest (e=80) is to be built in the river so as to raise the flood level by 1 foot. What must be the height of the crest above the bed f

The discharge, q, per foot run of weir is 12 cubic feet per second, and table xii for c= 80 gives q,=428 Therefore

 $(H+nh)^2 = \frac{12}{428} = 2.80$  From table xi H+nh=1.99 feet. But i=3.0, and h (table i) = 14 foot. Therefore, n being 1.0, H is 1.85 feet, and the erest must be 2.15 feet above the bed. The result is quite accurate, supposing that the channel downstream of the weir is altered for a long distance so is to give a free full over the weir. Otherwise the weir will be drowned,  $H_1$  being 85 foot, but judging from Bazin's results (art 14) with weirs having a moderate top width and sloping back and face, the discharge will hardly be affected,  $H_2$  being only 46 $H_1$ . Actually H would perhaps be 1.9 or 1.95 feet.

Example 3 —A river whose mean width is 50 feet, depth 10 feet, and mean velocity 3 feet per second, has a bridge built across it The piers and abutments are square, and the total width of the water-way in the bridge is 30 feet. Tind the heading up caused by the bridge

Let c be 60 Since Q is 1500 cubic feet per second, and a is 300, therefore  $V = \frac{1500}{300 \times 60} = 8.33$  feet per second. From tible i

H=1 08 feet nearly, but as there is high velocity of approach H will be less, say 1 0 foot. Therefore  $f=50 \times 11$  0 = 550 square feet, and  $f=\frac{550}{530} = 2$  73 feet per second

From table 1 k=115 Let n=10 Then H+nk=1 115 From table 1 F=8 47 feet per second, which is too great by nearly 2 per cent, and H is therefore less than 1 foot by 4 per cent, that is, it is 90 foot

Example 4 -The depth of full supply in a canal is 5 feet The discharges with depths of 4 feet and 2 feet are 153 cubic feet and 46 cubic feet per second respectively Design a trapezoidal notch for a free fall in the canal The co-efficient is 66

From equation 62, page 109,

$$r = \frac{\overline{153 - 2828 \times 46}}{\overline{1210 \times 66 \times 2^{\frac{5}{2}}}} = 51$$
From equation 63, page 109.

From equation 63, page 109,  $I_1 = \frac{2.262 \times 4.6 - 4 \times 153}{6.05 \times 66 \times 31} = 3.78 \text{ feet}$ 

Example 5 -A weir in a thin wall is 4 feet high and H is The bed of the stream becomes filled up, so that the depth above the weir becomes 25 feet instead of 5 feet, but Q is unaltered How is H affected ?

The ratios  $\frac{A}{a}$  are 5 and 2.5 nearly From table xiii, c being 60 and n being 1 33, the values of ca are 1 013 and 1 057, so that Q is increased about 4.4 per cent if H is the same H will therefore be less than before by 3 x 4 4 per cent, that is, it will be 97 feet

Table XI  $\label{eq: Values of $H$ and $H^{\frac{1}{4}}$. (Art 1) }$ 

					<del></del>					
,	II	nt	D ft 01 H	Н	H <sup>2</sup>	Diff 01 H	n	из	Diff 01 JJ	
	04	0080	0032	60	4648	0119	18	2 415	0202	_
i	05	0112	0035	62	4889			2516		1
- 1	06	0147	0038	64	5120			2 619		
1	07	0185	0041	66	5365			2 723		ı
1	os	0226	0014	68	5607			2 828		ł
	09	0270	0041	70	5857			2 935		J
3	10	0316	0019	72	6109		21	3-043	0218	1
1	îĩ	0365	0051	74	6366		2 15	3 152	0221	ł
-{	12	0416	0053	1 76	6626		22	3 263	0224	1
ì	13	0469	0055	78	6889		2 25	3 375	0226	١
1	14	0524	0057	80	7155		23	3 488	0228	J
l	15	0381	0059	82	7496		2 35	3 602	0231	ì
- 1	16	0640	0061	84	7699	0138	24	3 718	0234	١
1	17	0701	0063	86	7975	0140	2 45	3 834	0237	ĺ
ŧ	18	0764	0064	88	8255	0142	25	3 953	0238	ł
J	19	0828	0066	90	8538	0143	2 55	4 072	0240	j
l	20	0894	0068	92	8824	0145	26	4 192	0242	ſ
-	22	1032	0072	94	9114	0146	2 65	4 314	0544	l
ł	24	1176	0075	96	9406		27	4 437	0246	l
Į	26	1326	0078	98	9702	0149	2 75	4 560	02.0	l
}	28	1482	0081	10	1 000	0152	28	4 685	0°52	į
ı	30	1643	0084	1 03	1 076	0156	2 85	4 811	0254	
ļ	32	1810	0087	1 10	1 154	0158	2 90	4 939	0255	
1	34	1983	0089	1 15	1 233	0163	2 95	5 066	0260	
ŀ	36	2160	0091	1 2	1 315	0166	30	5 196	0262	
ı	38	2342	0094	1 25	1 398	0168	3 1	5 455	0266	
ſ	40	2530	0006	I 3	1 482	0172	32	5 724	0275	
ı	42	2722	0099	1 35	1 568	0176 0178	3 3	6 269	0279	
ł	44	2910	0101	14	1 657	0182	34	6 548	0293	
ł	46	3120	0103	1 45	1 746 1 837	0186	36	6 831	0287	
١	48 50	3326 3536	0106	15 155	1 930	0158	37	7 117	0291	
ſ	52	3750	0112	16	2 024	0170	38	7 108	0294	
۱	5±	39G8	0113	1 65	2 119	0121	39	7 702	0299	
Ì	56	4191	0116	17	2-217	0197	40	8 000	0702	
Ì	58	4417	0117	i 75	2 315	0200			Į	
ţ		' '	1		- 1		ſ			

Tielf XII —Values of q, or  $\frac{2}{3}c\sqrt{2g}$  of 5 35c. (Art 1)

e	4,	•	7,	·	<i>q</i> ,
001	00535	61	3-264	81	4 334
002	0107	62	3 317	82	4 387
-003	·01605	63	3 371	83	4 441
1004	-0214	64	3 424	84 (	4 494
1005	0268	65	3 478	85	4 548
006	0321	66	3 531	86	4.601
007	0375	67	3 581	87	4 655
008	0428	68	3 638	88	4 708
-009	0482	69	3 692	89	4 762
5	2 675	7 71	3 745	9 (	4 815
51	2 729	71	3 799	91 [	4 869
52	2 782	72	3 852	92 (	4 922
53	2 836	73	3 906	93	4.976
54	2 889	74	3 959	94 (	5-029
55	2 943	75	4 013	95	5 083
56	2 996	76	4 066	96 (	5 136
57	3 050	77	4 120	97	5 190
58	3 103	78	4 173	98	5 243
59	3 157	79 8	4 227	99	5 297
6	3 21	8	4 28	[1]	5 35
	1			l	

### TABLE XIII —CO-FFFICIENTS OF CORRECTION, c., FOR VELOCITY OF APPPOACH (Art 5)

		c= 60		1	~0		
4 4	Values of m.		Values of a			alues of	-
	14	1 33	1	14	1 25	1	
2 2-2 2-5 3 4 5	10°8 1079 1060 1041 1022 1014 1007 1003	1093 1075 1057 1039 1021 1013 1007 1003	1067 1055 1042 1028 1015 1009 1005 1001	1198 1176 1115 1074 1041 1072 1002	1159 1149 1110 1071 1039 1024 1011 1006	1129 1105 1079 1030 1028 1017 104 \$	

#### Tables XIV and XV—Co efficients of Discharge, c, for Weirs in Thin Walls with Complete Contraction (Art 6)

#### XIV -Ordinar | Wens

Head	Length of Weir in Teet												
Feet	6o	1(7)	,	3	5	19	19						
1	632	639	646	652	653	655	656						
15	619	625	634	638	640	641	642						
2	611	618	626	630	631	633	634						
25	605	612	621	624	626	628	609						
3	601	608	616	619	621	624	625						
5	595	601	609	613	615	618	620						
5	590	596	605	608	611	615	617						
6	587	593	601	605	608	613	615						
7	585	590	598	603	606	612	614						
8	1	į	595	600	604	611	613						
9	l l	l	592	598	603	609	612						
1 )	J	j	590	595	601 )	608	611						
12			585	591	597	605	610						
14	- 1		580	587	594	602	609						
16	ļ			582	591	600	607						
17	- 1	ſ	1	ſ	ſ	599	607						
2		1	585(*)										

#### AV -Slort Weirs

Head		Length of Weir in Feet												
in Feet	-033	-066	-099	164	*16	3 9	1654							
03 05 10 13 16 25 33 39 60 80	668 668 679	6 3 648 647 640 642	620 629 628 627 627 627	60 613 614 612 612 612 614 615	674 618 608 60 60 t 60 t	618 607 98 789 5.33 5.14	604 618 611 794 91 590							

TABLE XVI —COFFICIENTS OF DISCHAFGE, 6, FOR WEIES IN THIN WALLS WITHOUT END CONTRACTIONS, BUT WITH FULL CREST CONTRACTION (Art 6)

				length o	Welt in	Feet								
Icad In	176 to 676	2(7)	ŧ0	٠	5	7	10	25	12					
eet.	Bazin s Co efficients		Smith a Coefficients.											
1				. 1	659	-658	428	657	₹5					
15	1 1	6-2	-649	647	645	645	44	-644	-64					
-2	662	645	642	641	638	637	£37	636	-63					
·25	655	641	638	136	634	C33	€32	£31	-73					
3	652	-G39	636	+33	631	450	628	₹27	C2					
4	646	636	633	630	628	₹25	623	622	62					
5	-640	637	-633	-630	-627	624	-621	-620	-61					
G	637	638	634	630	627	623	620	-619	۴l					
7	-635	640	635	-631	628	624	€20	-619	61					
8	633	643	637	633	629	625	₹21	f20	-61					
-9	633	645	639	635	631	₹27	.622	-620	61					
1	-632	648	641	637	·C33	-629	624	621	43					
1-2	631		-616	641	636	4.33	626	-623	· Gr					
14	630			644	440	₹34	€29	652	€3					
16	627	l		647	C42	-(37	421	620	62					
17	626	ĺ				679	632	J.C.J.	€2					
18	€25	٠.		1				į.						

TAILY AVII - COLLECTIONS FOL WEDE CLESTS (Art. 10)
(The correction is always minus except when marked plus)

(T	he correction						( au )	,
11-01			Will d	of ( rest is	in ice	_		
Feet.	1 1 2	1	4	•		19	12	••
-	_	1						_
10	107 1010	418	4115	-017	-017	× 17	٦1°	4.15
	1002 1017		4101	025	4 5	*C*5	<b>₹</b> 23	4 7
20	1012		1 27	1023	1 72	1 33	-033	1 34
30	100		131	-041	44.		145	٠,
40 1		₹ 10	122	045	4.5*	11	** :	446
45		+ KK 9	•••					
- 50	ŧ		444	4110	415	4063	4.74	• • •
•(0	1			131	٠,	4 - 3	40.3	
70 1				417	٠.	4 * 5		11:
				4>>	4.4	4-1	1-01	1
-91				. 119	1:-	0		127
140	1			• • •	4.6	4 3	٠:	142
1-	1			+		< :1	×1	16.
ii	1		l	1	• •	113		1.
1.5			1				. !"	

# Tables XIV and XV—Co efficients of Discharce, c, for Weirs in Thin Walls with Complete Contraction (Art 6)

XIV -Ordinary Weirs

Head			Lengt	of Weir i	n Feet		
Feet	66	1()	9	8	5	10	19
1	652	639	646	652	653	655	656
10	619	62a	634	638	640	641	642
2 }	611	618	626	630	631	633	634
25	60a j	612	621	624	6%	698	699
3	601	608	616	619	621	624	675
5	595	601	609	613	615	618	600
5	590	596	60a	608	611	615	617
6	587	593	601	605	608	613	615
7 8	585	590	598	603	606	612	614
8	- 1	J	595	600	604	611	613
9 ]	j	J	592	598	603	600	612
1	ì	1	590	595	601	608	611
12		ļ	585	591	597	605	610
14	1	)	580	587	594	602	609 607
16	1	- 1		582	591	600	607
17	- 1	}	585(*)	- 1	ļ	599 j	501

AV -Slort Werrs

Head			Lengt	h of Werh	n Peet		
Feet	1033	1066	-0.19	164	*16	379	456
03 05 10 13 16 25		6 3 -648	620 629 628 62*	60 613 614 612 612	631 618 608 60 601 702	618 60° 598	6°4 618 611 94
80 80	679 664 666	612 612	62" (	614 617		593 593	<i>"90</i> 91

TABLE XVI —CO EFFICIENTS OF DISCHAPGE, c, FOR WEIRS IN THIN WALLS WITHOUT END CONTRACTIONS, BUT WITH FULL CREST CONTRACTION (Art 6)

	Length of Weir in Feet.														
Head in	1 % to 6 %	•(7)	3 (7)		5	7	10	Į5	19						
Feet.	Baz n a Co efficients		S ith a Co-efficients.												
1					659	658	658	657	65						
15	{	652	649	647	645	645	644	644	-643						
-2° -2° 3	662	645	642	641	638	637	637	636	63						
<b>-2</b> 0	655	641	638	-636	634	633	632	631	-63						
3	652	639	636	633	631	629	628	627	624						
4	646	636	633	630	628	625	623	692	62						
o	640	637	633	630	627	624	621	620	61:						
6	637	638	634	630	627	623	620	619	618						
7 8	635	640	635	631	628	624	620	619	-618						
8	633	643	637	633	629	625	621	620	618						
9	633	645	639	635	631	627	622	-620	-619						
1	632	648	641	637	633	628	624	621	611						
1-2	631	į	646	641	636	632	626	623	620						
14	630	- 1		644	640	634	629	625	-623						
16	627	. 1	]	G47	642	637	631	626	-623						
17	626					638	632	606	62:						
18	625		1			. 1		1							

Table \VII —Corrections for Wide Crests (Art 10) (The correction is always minus except when marked plus)

Head	l			Width o	Width of Crest in Inches														
in Feet.	1	2	3	4	6	8	10	1*	21										
10	-007	016	018	-018	017	-017	017	-017	017										
15	+ 002	-017	-023	-024	025		025	025	026										
20		-012	024	029	-031	032	033	-033	034										
30	1 )	+ 1005	017	1030	1947		047	048	050										
40			-010	-022	045	-055	-060	-062	-066										
45	1	i	+ -003																
50	i !			-006	041	-060	-069	074	082										
GO	1				-031	-0.9	-075	-083	1007										
70			i 1		-017	-052	075	-089	112										
80	ì		1		-000	040	071	-091	125										
-90	1	1			+ 019		-062	-089	137										
10					1	-056	-050	082	149										
i 2					1	+ 025	-021	-061	163										
14	1 '	1	1	i i	1 '	1. /	+ 1013	032	150										
î ŝ		ı						-015	,										

# Tables XVIII to XXII—Inclusive Coefficients, C, for Weirs 6 56 Feet Long without End Contractions

XVIII -Weirs in Thin Walls (Art 1)

He gl t		Head in Peet														
in Feet	164	23	33	53	66	80	98	1 15	1 31	1 48	14	1 80	1-17			
66				]	]	]	-	]		-		1				
98 1 31 1 64																
1 97 2 62					•						•					
3 28 4 92	674 672	660	650	641	638		636	636	636	638	656 639	640	641			
6 56	672	659	650	641	635	633	632	632	632	632	632	632	632			

## XIA —Werrs with Flat Tops and Vertical Face and Lack (Art. 10)

					(Art	10)			
Dime of W	t stons			11	eals in	Feet			Remarks
W 4th in Feet	Height in Feet	3		10	14	2 3	4	6	Armsias
6 ə6	4 57 2 46	45		49 (*) 48	48 (*) 50	47 (*)	50(*)	51 (*)	When the up stream edge was rounded to a m
2 62	4 57 2 46	48			L_ 1	1	 		.:
1 31	2 46	50	51	54	59				
66	2 46 1 15	52 53	58 60	65 C7	70	nd	erneat!	All c	sheets drowned ther fgures are the correspond
33	2 46 1 15	57 57	65 72	90* 77*	71*	i g	figures	for al ec derneat	ta lepresse l or ! are the same
16	2 4° 1 15	63	80*	77 <b>*</b> 72*					

XX -Weirs with Bounded Tops (Art 12)

	D mena of Wel	ne rv.		•	Head	in Feet.		
vet one of Weire	Ra Has	Height Fret	3	-	14	-3	10	6-0
Fig 69, p. 82,	34 ft. up- stream, 40 ft. down stream	1 64	-67	79	86			
Fig 78, p. 99, .	-26 ft.	1-64	72	54	54			
Fig 78a, p. 99, .	7 37 ft	53		57 (*)	62(*)	66 (*)	68 (*)	69 (*)
Fig 78s, p 99,		1 64	57	59	65			_

XXI - Weirs with Steep Back-slopes (Art 11.

54		i	_	Back	Vertica	L		Bac	k į	to 1	Bac	k į	to 1
Height of Welr in Fert.	Slope of lace of Weir			Head	in Fee	t.			ead Feet			lead Feet	
in in		3		14	•-3	4	6	3	Ē	1 4	3	-	1 4
1-64	Vertical	Н		'				65	76	71	75	78	71
1 64	1 to 1	1-6S	78	74	]		) [			1			
1 64	2 to 1	75	79	77		ı		'					
1.64	Vertical		_	_	_			56	73	70	J-6	73	7
1 61		59	72	80									
1 64					1			٠.	••	١.	}		
17	2 to 1				-68 (°)	69 (°)	69 (*)						
-		-	-	1	- }				-	H	''		_
1 64	2 to 1	58		73									
	2 to 1										١.		1
		ιi											į
	1-64 1 64 1 64 1 64 1 64 1 64 1 64	1-64 Vertical 1-64 1 to 1 1-64 2 to 1 1-64 Vertical 1-64 1 to 1 1-64 2 to 1	1-64 Vertical 1-64 1-75 1-64 2-10 1-75 1-64 1-10 1-10 1-10 1-10 1-10 1-10 1-10 1-1	1-64 Vertical 1 65 78 164 2 to 1 75 79 164 1 to 1 55 72 164 1 to 1 61 71 67 79 164 2 to 1 55 65 65 69 2 to 1 62 79 49 3 to 1 77 (7)	1-64 Vertical 1-64 1 to 1 1-64 2 to 1 1-65 78 1-74 1-64 2 to 1 1-75 79 17 164 Vertical 164 1 to 1 164 2 to 1 164 2 to 1 164 2 to 1 164 2 to 1 164 2 to 1 165 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	1-64 Vertical 1-64 Vertical 1-64 2 to 1 75, 79 77  1-64 Vertical 1-64 1 to 1 59, 72 80 1-64 2 to 1 61, 77, 79 1-7 2 to 1 63(1), 65(1), 65(1) 1-64 2 to 1 55, 65, 73 1-9 2 to 1 62(1), 67(1), 69(1) 1-64 2 to 1 55, 65, 73 1-9 2 to 1 62(1), 67(1), 69(1) 1-64 2 to 1 70(1), 72(1), 68(1) 1-64 2 to 1 70(1), 72(1), 68(1)	1-64 Vertical 1-64 Vertical 1-64 2 to 1 75 79 77  1-64 Vertical 1-64 1 to 1 59 72 80 1-64 2 to 1 61 71 77 1-7 2 to 1 63 (1) 65 (1) 65 (1) 69 (1) 1-64 2 to 1 58 65 73 1-9 2 to 1 62 (1) 67 (1) 69 (1) 69 (1) 1-64 2 to 1 58 65 73 1-9 2 to 1 62 (1) 66 (1) 69 (1) 69 (1) 1-9 3 to 1 70 (1) 72 (1) 68 (1) 66 (1)	1-64 Vertical 1-64 Vertical 1-64 2 to 1 75 79 77  1-64 Vertical 1-64 1 to 1 59 72 80 1-64 2 to 1 58 65 73 1-75 79  1-75	1-64 Vertical 65 78 74 65 65 65 65 66 65 66 66 66 66 66 66 66	1-64 Vertical 1-64 Vertical 1-64 2 to 1 75, 79 77  1-64 Vertical 1-64 1 to 1 59, 72 80 1-64 1 to 1 61, 71 77  1-64 2 to 1 61, 71 77  1-64 2 to 1 61, 71 77  1-64 2 to 1 63 (7), 66 (7), 69 (7), 69 (7)  1-64 2 to 1 63 (7), 66 (7), 69 (7), 69 (7)  1-64 2 to 1 55, 65, 73  1-64 2 to 1 62 (7), 67 (7), 69 (7), 69 (7), 69 (7)  1-64 2 to 1 70 (7), 72 (7), 68 (7), 69 (7), 69 (7)  1-64 2 to 1 70 (7), 72 (7), 68 (7), 69 (7), 69 (7)  1-64 2 to 1 70 (7), 72 (7), 68 (7), 69 (7), 69 (7)  1-64 2 to 1 70 (7), 72 (7), 68 (7), 69 (7), 69 (7)  1-64 2 to 1 70 (7), 72 (7), 68 (7), 69	1-64 Vertical 1-64 Vertical 1-64 2 to 1 1-75 79 1-77 1-64 Vertical 1-64 2 to 1 1-75 79 1-75 1-75 1-75 1-75 1-75 1-75 1-75 1-75	1-64 Vertical 1-64 Vertical 1-64 2 to 1 1-75 79 1-75 1-64 Vertical 1-64 2 to 1 1-75 79 1-75 1-75 1-75 1-75 1-75 1-75 1-75 1-75	1-64 Vertical 1-64 Vertical 1-64 2 to 1 75 78 74  1-64 2 to 1 75 79 77  1-64 Vertical 1-64 1 to 1 59 72 80 1-64 2 to 1 61 71 77 1-64 2 to 1 61 71 77 1-64 2 to 1 61 71 77 1-64 2 to 1 63 (7) 66 (7) 69 (7) 69 (7) 1-64 2 to 1 63 (7) 66 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 69 (7) 1-64 2 to 1 65 (7) 69 (7) 69 (7) 69 (7) 69 (7)

#### HYDRAULICS

XXII - Wens with Flat Back-slopes (Art 11)

Slope of Back of Wer	Top Width of Weir in Feet	He gl t of Weir	Head in Feet			Face 1 to 1			_	Face 2 to 1  Head in Feet				
						F	Head in Feet							
			3		1 4	3	7	1 4	3	-	14	2 3	4	6
1 to 1	00 { 33 66	1 64 2 46 4 9 1 64 1 64	72		1		80 72			79 (*)	77 77 (*) 79 74	73 (*)	70(*	68 (1
2 to 1	J	1 64 2 46 4 9 2 46	48 49	56 51	68 58	58 51	63 61	74 71	58 55	64 62 63 (*)	78 78 73 70 66 (°)	68 <i>(</i> °)	69 (*)	69(*
3 to 1	00	1 64	55	64	68			ĺ						_
5 to 1		1 64 2 46 1 64 1 9 1 64	58 54	58 58	60 63	66 56	66 64	70 	58	66 (°)	71 69 68 (*) 68	66(*)	66 (*)	66 (*)
0 to 1	00	2 46	52	54	56		7	Î	-					

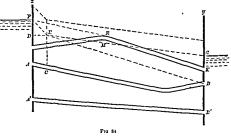
#### CHAPTER V

#### PIPES

[For preliminary information see chapter it articles 8 to 21]

#### SECTION I -- UNIFORM FLOW

1. General Information —In a uniform pipe, AB (Fig. 84), let the length AC, amounting to two or three times the diameter, be termed



the mouthpiece of the pipe. At the entrance of the pipe a head  $\frac{\Gamma^2}{2\eta}$  must be spent in imparting momentum to the water. This causes a loss of pressure head only, and not of total head. In exchange for the loss of pressure the water obtains a clocity head  $\frac{\Gamma^2}{2\eta}$ , but this is finally lost in the receiving reservoir, where the energy possessed by the water is wasted in eddies. There is also a loss in the mouthpiece depending on the co-efficient of resistance (chap, in art. 5), and varying from about  $\frac{\Gamma^2}{2\eta}$  in a bell-

mouthed, to about  $50\frac{V^2}{2g}$  in a cylindrical mouthpiece. This last occurs if the pipe simply stops short flush with the side of the reservoir without being splayed out. If the pipe projects into

the reservoir, and ends without a flange, the loss of head is about  $93\frac{V^2}{2g}$  The total loss of pressure head at the entrance of a pipe

is thus  $(1+z_s)\frac{V^s}{2g}$  where  $z_s$  varies from 06 to 93. This loss of head is the height FD. The line of hydriulic gridient is FLG.

In equal lengths L , L , etc , the falls in the line of gradient or losses of head by friction are equal If the inclination of the pipe is uniform, as in AB, the line of virtual slope is strught, but not otherwise Generally, however, the variations in the inclination of the pipe in lengths Li, L , etc , are not enough to cause great differences in the lengths of their horizontal projections, and the line of virtual slope is practically straight. Sometimes the length of a pipe is so great that the loss of head at the entrance may be neglected in estimating H, and the length of the mouthpiece in estimating L S is then found more easily The actual posi tion of the pipe is of no consequence. The virtual slopes and discharges of the pipes AB, AB, etc, are all equal, provided the roughnesses, diameters, and lengths are equal If the pipe discharges freely into ur, the virtual slope is IB Pipes are always assumed to be circular in section unless the contrary is stated

If it any point I the line of the pipe rises above the line of the hydraulic gradient, the pressure is less than the atmospheric pressure. At such a point air may be disengaged from the water and the flow impeded, the line of gradient being shifted to II (loss of head at entrance not considered) and the pipe I K running only partly full. If the height MR is more than 31 feet the pressure becomes negative and flow impossible. The above refers to cases in which the water is subjected throughout to ordinary atmospheric pressure. If the pressures on the two reservoirs are unequal the heads must be calculated (chap ii art. 1) and the gradient z / drawn accordingly. Arrangements must be made for periodically drawing off the air which accumulates at 'summits' such as I I lying above the gradient line.

With small pipes a great increase in the temperature of the water increases the discharge. The following results have been found —

riefs 12'

]	Dam teref	Increase in	Temperature Cater	In rease of Discharge			
	Pipe	Firen	7	_ · · · · · · · · · · · · · · · · · · ·			
	In hea.	co•	515.	25 per cent.			
	15	-7*	120*	8 per cent. (1' about 8 5) 10 per cent (1 about 5 7).			
	2	.5.	10,	Discharge was percej tibly increased			

The pressure in a pipe, after allowing for difference in head, decreases somewhat in going from the circumference to the centre

Let D be the diameter of a pipe. Then B is  $\frac{D}{4}$  or half the actual radius. Since the sectional area is as  $D^1$ ,  $\sqrt{R}$  as  $\sqrt{D}$ , and since C also increases with D, the discharge increases more rapidly than  $D^1$ . If two pipes are nearly equal in diameter, their discharges will be nearly as  $D^1$ . Allowing for increase of C, a pipe of 2 feet diameter will discharge nearly as much as six pipes of 1 foot diameter. To double the discharge of a pipe it is only necessary to increase the diameter by about 30 per cent. Since F increases as  $\sqrt{S}$ , and C also increases slightly with S, the discharge increases rather more rapidly than  $\sqrt{S}$ . In order to double the discharge S must be more than trebled. Doubling the slope increases the discharge by perhaps 50 per cent. For a given head H the slope is inversely as L, and Q therefore increases

more rapidly than  $\frac{1}{\sqrt{L}}$  It is clear that slight errors in measuring the diameter of a pipe, or an insufficient number of measurements when the diameter varies—is it nearly always does—may cause considerable errors in discharges or co-efficients

All the ordinary problems connected with flow in uniform pipes can be solved by means of equations 14 and 15 (p 21), some directly and some by the tentative process. The problems referred to are those in which one of the quantities Q, S and D has to be found, the others being given F can, of course, always be found from D and Q without difficulty, or either of those quantities from F and the other. Pipes are generally manufactured of certain fixed sizes, and when the theoretical diameter has been calculated the most suitable of these sizes can be adopted, unless a special size

is to be made To fucilitate calculations various tables have been prepared. The method of using them and of dealing with the above problems will be clear from the examples given and the remarks which precede them.

2 Short Pipes —When the length of a pipe is not very great the velocity may be high the co-efficient C may be outside the range of experimental data, and its value then can only be estimated For cases in which L is not more than 100D the pipe may be treated as a short tube, and equation 7 (p. 13) used The following values of c have been found —

	Co effic ents	of D sel arge c	ł
Ratio of L to D	Small Metal Pipes	P per of Un glazed Earth enware D ameters 285 foot to 48 foot	Remarks
2 3 5 10 25 31	82 82 79 77 71		With the earthenware pipes the discharge of two pipes lack side by side was 24 times that of a single pipe Segreat a difference we 11 not
37 5 50	64	50 52	have leen expected With long pipes no such effect would occur The coefficients for
53	1	25	these earthenware pipes are
60 100	60 55		very irregular

All the experiments were made with small heads. The shorter the pipe the greater the proportionate loss of head at the entrance and the less the variation of c for a proportionate increase in L. Thus when L increases from 25I to 50L c does not decrease so much as when L increases from 50L to 100L

3 Combinations of Pipes — If a pipe does not simply connect two reservoirs, but is, say, a branch supplied from a larger pipe and itself bifurcating its discharge can only be ascertained by tapping it and attaching pressure columns

When a water main gives off branches it may undergo reductions in diameter. Suppose that the conditions in such a main are to be determined when no water is being drawn off by the branches. If the discharge of the main is known the loss of heal and gradient in each length can be found. Suppose however that only the total loss of head H is known. Obviously the

PIPES gradient in any length will be flatter as D is greater, and JS will be roughly as  $\frac{1}{D^3}$  or  $\frac{H}{L}$  as  $\frac{1}{D^3}$  or H as  $\frac{L}{D^3}$ . Thus if the total loss

of head is known the loss in each length can be roughly found, the gradient being sketched and the discharge computed When greater accuracy is required let D' be an approximation to the average diameter of the whole main With this diameter and gradient  $\frac{H}{I_c}$  find an approximate discharge Q, and thence the

velocities  $V_1$ ,  $V_2$ , etc. Then for any length  $L_1$ ,  $C_1 \sqrt{R_1} = \frac{V_1}{\sqrt{S}}$ The slopes S1, S2, etc , can then be found, and the losses of head are L, S, L, S, etc If these when added together are not equal to H the discharge Q must be corrected When Q has been found accurately the diameter D of the equivalent uniform main is known. It is such as gives the discharge Q with the gradient If the above problem again occurs with the same pipe, but a different value of H, there will be no difficulty, for D will be practically unaltered

Let Fig 85 represent a main of uniform diameter, and let its discharge be drawn off gradually by branches If the dis charges at M and N are Q and zero respectively, and if the discharge is supposed to decrease uniformly along the whole length of the pipe, then the



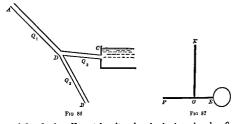
line of gradient will be a curve If x and y are the ordinates of any point in the curve, and A and B are constants, Q = Ax

But if C is supposed constant,  $Q=B\sqrt{S}=B\left(\frac{dy}{dz}\right)^{\frac{1}{2}}$  Therefore  $\frac{dy}{dz} = \frac{A^2}{R^2} x^2 \quad \text{Integrating, } y = \frac{A^2}{3R^2} x^3$ 

When x=L,  $y_1=\frac{A^2}{2E^2}$   $L^3$ , and the mean gradient  $\frac{y_1}{L}=\frac{A^2}{3L^2}$   $L^2$  But

when x=L,  $\frac{dy}{dx}$  is  $\frac{A^2}{D^2}$   $L^2$ , or the mean gradient is one third of the gradient at M The total loss of head is one third of what it would have been if the whole discharge Q had been delivered at N As C increases with S the fraction is really greater than one third

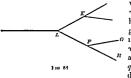
If in a branched pipe (Fig. 86) the pressures at A, B, C are known, the discharges can be found by assuming a pressure head, H, at D, and calculating the discharges  $Q_1$ ,  $Q_2$ ,  $Q_3$  If  $Q_4$  does not



equal  $Q_3 + Q_m$  then H must be altered and a fresh trial made  $Q_3$  may be plus, zero, or minus according to the direction in which the water flows

Let E (Fig. 87) be a water main, EF a branch, and GK a pressure column, and let there be a three way cock at G. If no water is being drawn off at F the water rises to a height K, determined by the pressure in the main, whether GK or GF is open, but if water is being drawn off at F the height GK will be less when GF is open. If EF is a house service pipe and GK a pipe rising to the ground level outside the house, then by means of a pressure gauge at K an inspector can tell, without entering the house, whether water is being used in it or not

In a system of bifurcating pipes (Fig. 88) such as that used for the water supply of a town, the pressure heads sufficient to force the



water to the required levels it various points, L, K, I, having been determined, the gradients corresponding to imaginary pressure columns at these points can be drawn, and the required discharges In Inc. to being known, the diameters of the various pipes

can be calculated Suppose the system to be at work, then if the consumption in a branch FG is increased, the pressure head at F will be lowered and the branch FH will not leable to obtain its

estimated supply, unless its conditions are similar to those of FG. The lowering of the pressure at F causes an increased discharge in LF, and a lowering at L, and thus more water is drawn in from the reservoir, but not to the same amount as the increase taken by FG. Thus any excessive consumption tends to partially remedy itself, firstly by preventing water being forced to high levels in its neighbourhood, and secondly, by drawing more water into the main. (Cf. chap vii art 6).

4. Bends.—For bends in small pipes Weisbach found the loss

4 Bends.—For bends in small pipes Weisbach found the loss of head to be z, 127. For a bend of 90° he found z, to be as follows.

The 1 2 3 4 5 6 7 8 9 10

The 13 14 16 21 29 44 66 98 141 198

Where R is the ridius of the bend and rithat of the pipe For angles other thin 90 the loss of head does not increase so fast as the length of the bend According to the above figures, the loss of head decreases as the radius of the bend increases, and this view has generally been accepted. But recent experiments made at Detroit with large pipes by Williams, Hubbell, and Fenkell show that, with large pipes at least, the resistance for a bend of 90 decreases as the ridius of the bend decreases, provided it does not fall below 2 or 2 diameters of the pipe. The relative resistances seem to be somewhat as follows with a new iron pipe 30 inches in diameter —

(1)	(2)	(3)	(4)	(5)
R_dius of 90 Curve	Length of Curve.	Relative Loss of Head due to rea at ance in a length of 1 foot of p pe	Total Relative Loss of Head in bend of 90	Loss of Head in same length of straight p pe.
Feet.	Feet.			
4	63	7-0	44	63
6	94	4.8	45	94
10	15 7	4 3	68	15.7
15	23.6	4.0	94	236
25	393	31	122	39 3
40	62 8	23	144	628
60	94-2	2-0	188	94-2
straight.	1	10		

<sup>1</sup> Transactions of the American Society of Civil Engineers, vol xlvii

The resistance per foot run of pipe decreases, though not very rapidly, as the radius of the bend increases, but owing to the greater length of bend the total resistance increases with the radius of the bend

The results of the experiments are not as exact as could be desired It was found that the straight lengths of pipes, adopted as standards for comparison with the bends, came themselves to some extent under the influence of abnormal velocity distribution due to bends upstream of them The velocities were all measured by Pitot tubes and somewhat complex apparatus, and it is not certain that the results are quite accurate (chap vin arts 14 and 15), but any errors of this kind must have affected all observations in very much the same manner, so that the relative results are hardly affected The diameters of the pipes were not measured at as many points as desirable The figures in the above table are not quotations, but have been arrived at from figures given in the paper They are only intended to be approximations, but having regard to the great differences among the figures in column 3, and to their regularity, the view of the experimenters, that their proposition is true beyond a doubt, must be upheld Some preliminary experiments made with 12 inch and 16 inch pipes gave similar results When the radius of curvature becomes very small the law no longer holds good. This is perhaps because contraction occurs (Cf chap vii art 1)

It is also proved in the paper under reference that when it is desired to connect two straight portions, AL, LD (I ig 89), of a pipe by a 90° curve, a small curve CF

C B is cheaper, because, although the line Pto 59

F is longer than ALGD, the cost of ly ing pipes is much less per foot run on the strught than on curves

In a cross section a few feet down stream of the termination of a 90 degree curve of 10 feet radius in a D 30 inch pije the miximum velocity was found with low velocities to le in the centre of the pipe, but it moved

when the maximum velocity was 3 5 feet per second to a distance from the edge of the pipe equal to about 20 of the diameter further increase of 30 per cent in the velocity fuled to shift it further With curves of 15 feet and 10 feet ridius its position was about the same

5 Relative Velocities in Cross Section—The velocities at different points in the cross section of a pipe have been observed chiefly by means of the Pitot tube (chap viii art 14) Bazin, discussing some observations made by Darcy and some by himself on pipes, finds some previously proposed formulæ to be unsuitable for general application, and arrives at two empirical equations—

$$V_{\tau}-v=V\sqrt{b}\left\{21\left(\frac{r}{E}\right)^{4}+27\left(\frac{r}{E}\right)^{3}\left(1-110\frac{r}{P}\right)^{2}\right\}$$
 (68)  
 $V_{\tau}-v=295V\sqrt{b}\left\{1-\sqrt{1-095\left(\frac{r}{E}\right)^{3}}\right\}$  (69)

where  $V_{\bullet}$  is the central velocity, V the mean velocity, i the velocity at radius t, R the radius of the pipe, and  $b=\frac{RS}{P^2}$ . Either

of these equations gives a velocity curve which nearly agrees with the observed velocities, and both give r=74E as the distance from the centre where the velocity of the witer is equal to V. In a 30 inch pipe the form of the velocity curve has been found by Williams, Hubbell, and Fenkell to be very nearly a semi-ellipse. Regarding the ratio of V to the central velocity  $V_\alpha$ , the various experiments made show somewhat conflicting results, and are not sufficiently rehable and numerous to enable the ratio to be fixed with confidence. The general tendency is for the ratio to increase with V and also with the diameter of the pipe. The following table has been compiled. The figures must be taken as showing probable and approximate values only, but are likely

Kind of Pipe	Da eter	Mean Velocit es i Feet per Secon!								
Kind of Pipe	of P pe in inches.	-8	10	2.5	3.5	3	8	14	6° 5	
Brass	11		_						84	
Brass seamless	11 2	70	-3	77	79	80				
Cast won	3.5	, 1		80	કા	82	83	84	ļ.	
Cast iron	9.5	l .	80	81	82	83	84	85	ļ	
Cast iron with		1	-							
deposit	9 5	1	81	81	82	82	83	83	1	
-	( 12	ì	83	83	84	85	85	85	!	
New iron coated	16	]	82	83	84	85			ļ	
with coal tar	30	1 75	83	84	85				1	
Cement,	31.5	1		i .	85	86			į	
New iron coated with coal tar,	42	İ	1		86					

to give better results than the adoption of a fixed ratio for all cases. The range of velocities for which the figures are given for any pipe is approximately that for which experiments were made. By means of these ratios it is possible to deduce the probable mean velocity in a pine by an observation at the axis.

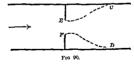
In the Detroit experiments above mentioned it was found that the velocity ratios tended to become irregular with low velocities, and it was suggested, in the discussion on the experiments, that a point of 'critical velocity' (chap 1 art. 15) exists at velocities of about 70 feet, 30 feet, and 14 feet per second for the 30 inch, 16 inch, and 12 inch pipes respectively

### SECTION II - VARIABLE FLOW

6 Abrupt Changes —The losses of head occurring at abrupt changes in small pipes have been found experimentally by Weisbach, and are as below

Abrupt Enlargement (Fig. 4, p. 5)—The loss of head is  $(F_1-\frac{F_2}{2g})^2$  or the head due to the relative velocity, but see remarks  $\frac{2g}{2g}$  in chap in art 18

Abrupt Contraction (Fig. 3, p. 5)—The loss of head (and also for a diaphragm (Fig. 90) or for a contraction with a diaphragm) is chiefly caused by the enlargement from EF to MN, and is to be found as above. To find the velocity at IF divide the elecity



at MN by  $c_r$ . For a draphragm (Fig. 90) the values of  $c_r$  were found to leas follows —

 $\frac{\text{Area }FF}{\text{Area }CD} = 1$  2 3 4 5 6 7 8 9 10  $c_0 = 624$  632 643 659 681 712 755 813 892 100

These may be accepted for the other cases

Filter (I is, 91) — The loss of head is  $-\frac{I^{2}}{2g} \text{ where } \gamma = 946 \text{ sm}^{2} \frac{\theta}{2} + 2.05 \text{ sm} \frac{\theta}{2}$ 

The values of z, are as follows :-

 $\theta = 20^{\circ} 40^{\circ} 60^{\circ} 80^{\circ} 90^{\circ} 100^{\circ} 110^{\circ} 120^{\circ} 130^{\circ}$ z,= 046 ·139 ·364 ·740 ·984 1·260 1·556 1·861 2·158 2·431,

PIPPS



Thus at a right-angled elbow nearly the whole head due to the velocity is lost. When two right-angled elbows closely succeed each other the loss of head is double that in one elbow if the two bends are in opposite directions, but is no greater than that in a

single elbow if the bends are both in one direction. Gate-Valce (Fig. 92) .-

 $\frac{h}{h} \approx 1.0 \quad \frac{7}{8} \quad \frac{3}{4} \quad \frac{5}{8}$  $\frac{a}{A} = 1.0 \cdot 948 \cdot 856 \cdot 740 \cdot 609 \cdot 466$ .315 z, = ·0 ·07 ·26 ·81 2·06 5·52 17.0 Where A is the sectional area of the pipe and a that of the opening.



206 106

					=/				•
	Fig.	-				F10, 93			
	۴ (Fig.								
$\phi =$	5°	10°	15*	20*	25*	30.	33.	40°	45
$\frac{a}{A} =$	•926	·850	772	692	613	•525	458	-385	·315
$z_c =$	.05	-29	.75	1.56	3.10	5.47	9.68	17.3	31.2
$\phi =$	50°	55°	60°	65°	82°				
$\frac{a}{A}$ =	-250	·190	·137	-091	00				

Throttle Value (Fig 94) -



Fra 94

$\phi = 5^{\circ}$	10,	15°	20	25	30°	35°	40°	45°	50"
$z_t = \cdot 24$	52	90	1.54	251	3 91	6 22	108	187	326
$\phi = 55^{\circ}$	60	)°	65°	70°					
$z_t = 58.8$	11	8	256	751					

In the last three cases  $z_{c_t} z_{c_t}$  and  $z_t$  are multiplied by  $\frac{F^2}{2g}$  to give the loss of head

It is not at all certain that the above figures apply correctly to large pipes, and in fact it has been proved that some of them do not apply correctly

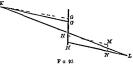
For a gate in a 2 foot pipe z, has been found to be as below.

h D	as observed	by Weisbach a rule given above
12	41 2	43
15	31 35	28
į	22.7	17
1	119	7 92
38	8 63	5 52
5/12	6 3 3	3 77
11/24	4 58	2 87
1/2	3 27	2 06
7/12	1 55	j 111
2/3	77	57
1 0	00	-00

When loss of head due to any of the above causes occurs, the line of hydraulic gradient shows a sudden drop as at GH, H ig  $\mathcal{O}_{Y}$ , its inclination is reduced, and with it the velocity and discharge of the pipe. If the local loss of head did not exist the slope would be KL. The velocity to be used in calculating the loss of head is that due to KG and not KL. If a second cause operates at M the gradient becomes KG, H M, NL, and the loss of head GH is now less than before because the velocity is less. Thus the loss of

head does not increase in proportion to the number of causes operating. But where economy of head is desired, it is necessary to

avoid abrupt changes of all kinds, using tapering 'reducers' where the diameter changes, and curves of fair radius at all bifurcations or changes in direction



It appears that the disturbance of the velocity ratios due to abrupt changes may extend downstream for long distances. Bazin found that the disturbance from the entrance contraction of a 32 inch pipe disappeared at 25 to 50 diameters downstream, but disturbance due to curves has been found to extend to 100 diameters. In the disturbed region the pressures, as indicated by pressure columns, appear to be below normal, or at least to be un reliable. In some important experiments on a 6 foot pipe 1 some of the results are doubtful and probably erroneous, owing to a piezometer being placed just downstream of an abrupt change.

7 Gradual Changes—When a gradual change occurs in the sectional area of a pipe equation 16, page 22, must be used At a point where the diameter of a pipe changes a tapering piece is usually put in If the taper is gradual the loss of head in it from resistances is about the same as in a uniform pipe with the same mean velocity

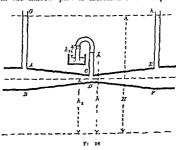
The following are examples of accidental changes in the dia meters of pines —

										_	
(1)	(2)	(3-	-1)	(5-	6)	(7)	(8)	(9)	(10)	(11)	(12)
Length of P pe	cominal Diameter	Act Diam		Velo	cities	V <sub>2</sub> <sup>2</sup> V z <sup>2</sup> or h.	↓ √1 1 <sup>2</sup> +1 2 <sup>2</sup>	c	Loss of Head from Resist ances or A or v <sup>2</sup> L c <sup>2</sup> L	Actual Fattin Gradient or k	Percent age of figure in column 7 to figure in column 10.
	Ins	Ins.			Peet.	Feet	Feet.		FeeL	Feet.	_
100	12		115		4 73	- 099	4 38	113	609	708	16-2
		1	1 .	ľ				128	-0354	0302	214
25	30	297	301	1 4 0	3.93	+ 0082	3 97				1
25	30	297	30}	1.0	983	+ 00051	-993	113	-00312	00251	163

<sup>1</sup> Transactions of the American Society of Civil Engineers vol. xxvl.

The figures in column 11 are obtained from those in columns 7 and 10 If the flow were uniform the figures in columns 10 and 11 would be the same, and the ratio of these figures to one another shows the error caused by assuming the pipe to be uniform the fall h is observed, and V found from h and C, the value of V found will be erroneous in the ratio (neglecting the small variation in C) of Ih to Ih, that is, in the first of the cases shown, by about 8 per cent of the smaller figure If h and I are observed (V being found, say, by measuring Q in a tank) and C is deduced the error in C will be similar to the above If h is not observed, but deduced from known values of V and C, then the percentage error is as shown in column 12 The second and third cases show the same pipe with very different velocities, and it will be noticed that the percentage of error does not vary very greatly In the first case quoted the variation of the diameter from the nominal diameter is perhaps excessive and hardly likely to occur in practice With longer lengths of pipe the percentage of error will, of course be small, but sometimes observations are made on short lengths, and it is clear that in such cases great error may arise, if the diameter is assumed to be uniform

When the diameter of a pipe is reduced (Fig 96) the velocity head in the narrow part is increased and the pressure head



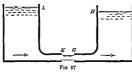
reduced. The insertion of a portion like ACF in a pipe causes very little loss of head if the tapers are in the case is similar to that of a compound tube (ch.). If CD is

small enough, the pressure there will full below the atmospheric pressure P, and if holes are bored in the pipe at this section no water will flow out, but air will enter The pressures on the control surfaces ACDB and CDFE balance one another, and the water has no more tendency to push the pipe forward than it has ın a uniform pipe

With the arrangement shown in Fig 97, the orifices being made to correspond as exactly as possible, the water flows with very little waste into the second reservoir, and the head GH is slightly less than KL

The pressure in the

net KG is P., and it makes no practical dif ference whether this portion is enclosed by a pipe or not, so long as the head KL is kept the same



If at CD (Fig 96) another pipe is introduced, pumping can be effected through it, as with the case of a cylindrical or compound tube

When the hydraulic gradient of a pipe is so flat that the fall between two pressure columns would be too small to be properly observed, the 'Venturi Meter' (Fig 96) is adopted It consists of two tapering lengths of pipe with three pressure columns the diameters, velocities, and sectional areas at AB and CD are D, v, A and d, V, a, then (chap 11)

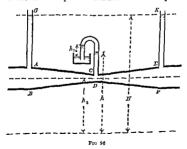
$$\begin{split} \frac{\mathcal{V}^*}{2g} + h &= \frac{v^*}{2g} + H \\ \text{Also} \qquad & \frac{\mathcal{V}^*}{2g} = \frac{\mathcal{A}^*}{a^*} \frac{v^*}{2g} \\ \text{Therefore} \qquad & \frac{v^*}{2g} \left(\frac{\mathcal{A}^*}{a^*} - 1\right) = H - h \\ & v^* = \frac{2ga^*}{\mathcal{A}^* - a^*} (H - h) \\ & v = \frac{a}{\sqrt{\mathcal{A}^* - a^*}} \sqrt{2g(H - h)} \end{split}$$

To allow for loss of head in the tube a co-efficient c must be used, and

$$Q = c \frac{Aa}{\sqrt{A^2 - a^2}} \sqrt{2g(H - h)}$$
 (70)

The figures in column 11 are obtained from those in columns 7 and 10 If the flow were uniform the figures in columns 10 and 11 would be the same, and the ratio of these figures to one another shows the error caused by assuming the pipe to be uniform the fall h is observed, and V found from h and C, the value of V found will be erroneous in the ratio (neglecting the small variation in C) of ./h to ./h'. that is, in the first of the cases shown, by about 8 per cent of the smaller figure If h and V are observed (V being found, say, by measuring Q in a tank) and C is deduced, the error in C will be similar to the above If h is not observed, but deduced from known values of V and C, then the percentage error is as shown in column 12 The second and third cases show the same pipe with very different velocities, and it will be noticed that the percentage of error does not vary very greatly In the first case quoted the variation of the diameter from the nominal diameter is perhaps excessive and hardly likely to occur in practice With longer lengths of pipe the percentage of error will, of course, be small, but sometimes observations are made on short lengths, and it is clear that in such cases great error may arise, if the diameter is assumed to be uniform

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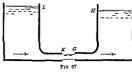


reduced The insertion of a portion like ACE in a pipe causes very little loss of head if the tapers are gradual The case is similar to that of a compound tube (chap in art 17) If CD is PIPES 135

small enough, the pressure there will full below the atmospheric pressure  $P_{\rm el}$  and if holes are bored in the pipe at this section no nater will flow out, but air will enter. The pressures on the conical surfaces ACDB and CDFE balance one another, and the water has no more tendency to push the pipe forward than it has in a uniform pipe

With the arrangement shown in Fig 97, the orifices being made to correspond as exactly as possible, the water flows with very little waste into the second reservoir, and the head GH is slightly less than KL

The pressure in the jet KG is  $P_{es}$  and it makes no practical difference whether this portion is enclosed by a pipe or not, so long as the head KL is kept the same



If at CD (Fig 96) another pipe is introduced, pumping can be effected through it, as with the case of a cylindrical or compound tube

When the hydraulic gradient of a pipe is so flat that the fall between two pressure columns would be too small to be properly observed, the 'Venturi Meter' (Fig 96) is adopted It consists of two tapering lengths of pipe with three pressure columns. If the diameters, velocities, and sectional areas at AB and CD are D, t, A and d, V, d, then (chap in )

Also 
$$\frac{f^2}{2g} + h = \frac{\mathfrak{t}^2}{2g} + H$$

$$\frac{f^2}{2g} = \frac{d^2 \mathfrak{v}^4}{a^4} \frac{\mathfrak{v}^4}{2g}$$
Therefore 
$$\frac{\mathfrak{t}^4}{2g} \left(\frac{d^4}{a^4} - 1\right) = H - h$$

$$\mathfrak{t}^4 = \frac{2ga^4}{d^4 - a^4} (H - h)$$

$$\mathfrak{t} = \frac{a}{\sqrt{4^4 - a^4}} \sqrt{2g(H - h)}$$

To allow for loss of head in the tube a co-efficient  $\epsilon$  must be used, and

$$Q = c \frac{An}{\sqrt{A^t - a^t}} \sqrt{2\eta(H - h)}$$
 (70)

The tops of the pressure columns at G and K will be practically at the same level, and one or other of them may be used. If the pressure at CD is less than the atmospheric pressure, the height  $h_1$  measures the difference and this height must be subtracted from  $h_2$ . In experiments made by Herschel with  $d\approx 77$  square feet, a=086 square feet, and pressures at CD less than atmospheric, c usually ranged from 96 to 101. With A=57.8 square feet and a=7.07 square feet, c varied from 95 to 99, its value being higher as the velocity was lower. The highest velocity at CD was 34.5 feet per second

### SECTION III -- CO EFFICIENTS

8 General Information —The values of the co efficient C for pipes are not well known An iron pipe unprotected by an inside coating of coal tar or asphalt generally becomes in time corroded and incrusted, but occasionally it is not so Much depends on the character of the water Incrustation may occur in a coated pipe if the coating is imperfect or damaged Severe incrustation in reduce the discharge to almost any extent, say by 30 per cent in large pipes, and by still more in smaller ones, where not only is the roughness increased but the diameter greatly reduced Definite or efficients cannot be given for incrusted pipes, but only for new and clean pipes In a wooden pipe the co efficients may be reduced by organic growth, but on the other hand the wood in some cases has become smoother with use

Besides the causes given in chapter in (arts 9 and 11) for discrepancies in C, it must be added that even if the pipe is uniform the diameter is often wrongly stated, the manufacturer s size being accepted. It has been shown above that a slight difference in D has a great effect. Errors in the measurement of Q, D, and S may be in either direction (those in S and D, especially of S, being greatest with low values of these quantities), but error arising from unsuspected or unreported incrustation, or losses of head from beinds or other causes all tend to give low values of C. Hence generally C as reported is likely to be too low and to be worst determined when S is small

9 Values of Co efficients — Darcy obtained a set of co efficients which vary from 93 to 113, as the hydraulic radius varies from 042 foot to 10 foot. Smith framed a much more extensive set, making C increase with both R and S. Fannings co efficients follow a similar law, his values, however, sometimes agreeing with Smith's and sometimes falling short of them by some 10 per cent

Smith's values are probably the more reliable, because of the greater attention which he gives to the subject and the care with which he eliminated faulty or doubtful experiments, and this is, very likely, why his figures are higher. Fanning's co-efficients apply to cast-iron pipes, Smith's to well made cast iron pipes or riveted sheet-iron or steel, all supposed to be coated, joints smooth, and curves of fair radius. The following statement gives an abstract of the co-efficients!—

		Hydraulic	Gradients.		[
Hydraulie Radius.	1 10	100	1 1000	10 000	Remarks
Feet.		149 136	137 133	133 128	Smith. Fanning
U		143	135	131	Mean
-25	124 115	116 110	104 104	100	Smith, Fanning
	120	113	104	100	Mean
10	107	101	96		Smith. Fanning
-	107	101	96		Mean

Recently Tutton has investigated an immense number of pipe experiments, including nearly all considered before. He adopts the formula V=C/R'S where C, is constant for any one pipe. The following are some of his figures—

Kind of Pipe	C <sub>r</sub>		y
New cast-iron (C L) or tarred pipe,	126 to 158	66	51
Wood stave pipe,	129 to 155	66	51
Wrought iron riveted pipe (W I),	127 to 165	62	55
Asphalt-coated pipe,	139 to 188	62	55
Tuberculated pipe,	31 to 80	66	55

<sup>&</sup>lt;sup>1</sup> Fanning gives his co efficients in another form and not for the equation  $I = C \sqrt{I \cdot S}$ , but they have now been reduced to the above form

2 Journal of the Association of Engineering Societies, vol XXIII.

The tops of the pressure columns at G and K will be practically at the same level and one or other of them may be used If the pressure at CD is less than the atmospheric pressure, the height  $h_1$  measures the difference, and this height must be subtracted from h. In experiments made by Herschel with A=77 square feet, a=086 square feet, and pressures at CD less than atmospheric, c usually ranged from 96 to 101. With A=57.8 square feet and a=7.07 square feet, c varied from 95 to 99, its value being higher as the velocity was lower. The highest velocity at CD was 345 feet pre second

### SECTION III -- CO EFFICIENTS

8 General Information —The values of the coefficient C for pipes are not well known. An iron pipe unprotected by an inside coating of coal tar or asphalt generally becomes in time corroded and incrusted, but occasionally it is not so. Much depends on the character of the water. Incrustation may occur in a coated pipe if the coating is imperfect or damaged. Severe incrustation may reduce the discharge to almost any extent, say by 30 per cent in large pipes, and by still more in smaller ones, where not only is the roughness increased but the diameter greatly reduced Definite or efficients cannot be given for incrusted pipes, but only for new and clean pipes. In a wooden pipe the coefficients may be reduced by organic growth, but on the other hand the wood in some cases has become smoother with use.

Besides the causes given in chapter in (arts 9 and 11) for discrepancies in C, it must be added that even if the pipe is uniform the diameter is often wrongly stated the manufacturers size being accepted. It has been shown above that a slight difference in D has a great effect. Errors in the measurement of Q, D, and S may be in either direction (those in S and D, especially of S, being greatest with low values of these quantities), but error arising from unsuspected or unreported incrustation, or losses of head from bends or other causes, all tend to give low values of C. Hence generally C as reported is likely to be too low and to be worst determined when S is small

9 Values of Co efficients — Darcy obtained a set of co efficients which vary from 93 to 113, as the hydraulic radius varies from 042 foot to 10 foot Smith framed a much more extensive set, making C increase with both R and S Fannings co efficients follow a similar law, his values, however, sometimes agreeing with Smith's and sometimes falling short of them by some 10 per cent

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great range of diameters and slopes, but no doubt many of them are inaccurate and some perhaps worthless. On examining the diagrams of them it is seen that in many cases other indices of S would fit the results. This, combined with the preceding remarks, seems sufficient to show that the figures in the above table derived from his formula should be considered only in their general and mean aspects, and must be taken generally as being low

The largest pipes considered by Tutton were 4 feet in druncter Some recent co-efficients for a 6 feet W I pipe are some 20 per cent less than Smith's and Framing's, while those for a 5 feet 1 in C I pipe are 4 and 9 per cent in excess. From these and Tutton's figures it is reviouslibe to conclude that C is lower for W I pipe thin for C I, and this may be due to the rivet beads. For asphalicated pipes Tutton's formula would give results some 10 per cent higher than for W I. For wood pipes the experiments have so far been few, but have included drimeters of 6 feet. The co-efficients seem to be about the same as for C I pipes. The general conclusion is that, though the whole subject is in a highly unsatisfactory state, Smith's co-efficients—or Fanning's for the small pipes, which Smith did not consider—are fairly reliable for clean C I or wood or coated pipes, and that for W I pipes 5, 10, or 15 per cent. should be deducted, the deduction being smaller as D is greater Detailed values of Smith's and Fanning's co efficients are given in tables xiv and xxiv.

Kutter's co-efficients (table xxix  $d \approx q$ ) are not very suitable for pipes, C remaining unaltered when S is increased above  $\frac{1}{1000}$ . They agree generally, when N=011, with Smith's, but give too low velocities for small pipes and too high velocities for large pipes with smill slopes (Cf chap 11 art. 13)

For small tin and zinc pipes Fanning's co-efficients are fairly correct. For 24 inch hose they are fairly correct when the hose is of linen and unlined, but they should be increased by some 25 per cent when the hose is of rubber or lined with rubber.

#### Examples

Explanation —The problem to be solved may be either to find the discharge in a pipe for which all the data are known or when the discharge and one of the quantities D or S are known to find the other. In the first case the solution is direct, in the others (since R and C vary with D and S) indirect. The methods to be adopted will be clear from the following examples

Blot es

Tutton's formulæ and co efficients have been accepted by one recent writer, but on examination they lead to somewhat curious results. When reduced to the Chézy formula, Tutton's co efficients for iron pipes come out as follows.—

	1	(		l			
Hy iraulic Radius	Kind of P pe	Tutton	s Co eff cients (C <sub>f</sub> )	1 10	10   100   100		
	<u></u>			Co eff	le ent C is	n Cl ézy f	orn ula
leet	CI	158	Highest	156	151	148	145
Į.	w i	165	values				104
10 {	Mean			152	141	132	12.
1	W I	126 127	Lowest values				11.
	Mean			118	111	104	90
	M I	158 165	Highest values	124 125	121	118 99	116
٠, ١	Mean		1	125	116	109	102
2υ {	WI	126 127	Lowest, values	99 96	96 85	94 76	93 1 S
Į (	Mean			98	91	85	81
ſ	C I W I	158 165	Highest values	107 113	104 99	102 89	100 79
- 1	Mean		1	110	102	96	90
10 {	WI	126 127	Lowest values	85 86	83 76	81 68	80 61
- [	Mean			86	80	75	71

Taking the highest values, it seems that in going from a steep to a flat slope I' decreases very much faster with a smooth W I pipe than with a smooth C I pipe This, though unlikely, is conceivable But if both pipes are roughened (roughening is the only apparent cause for lower values of C<sub>i</sub>), a similar law holds good, and I' decreases fister for the rough W I pipe than for the rough C-I pipe This is highly improbable Again for tuber culated pipe, which seems to include both kinds, I', if cilculated, would decrease slowly For asphalt it decreases rapidly For coal taired and galvanised pipe Tutton makes I'vary as S'', that is, C increases as S decreases, a result different from any hitherto accepted The results considered by Tutton cover in each case a

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great range of diameters and slopes, but no doubt many of them are insecurite and some perhaps worthless. On examining the diagrams of them it is seen that in many cases other indices of S would fit the results. This, combined with the preceding remarks, seems sufficient to show that the figures in the above table derived from his formula should be considered only in their general and mean aspects, and must be taken generally as being low

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For small tin and zine pipes Fanning's co-efficients are fairly correct. For 24-inch hose they are fairly correct when the hose is of linen and unlined, but they should be increased by some 25 per cent when the hose is of rubber or lined with rubber.

### EXAMPLES

Explanation —The problem to be solved may be either to find the discharge in a pipe for which all the data are known or when the discharge and one of the quantities D or S are known, to find the other. In the first case the solution is direct, in the others (since R and C vary with D and S) indirect. The methods to be adopted will be clear from the following examples

One advantage of the system of tables here adopted as compared to some others, is that V always enters as a factor. It is a distinct advantage, in designing that the value of V, and not only of Q, should constantly come to notice

Example 1 —Using Smith's co efficients, find the discharge of a  $W\_I$  pipe whose diameter is 3 feet and slope 1 in 1000

From table xxiv, C is about 123 5 and V about 34 Smith's co efficient for this value of V is 130, so that V will be about 36 and C about 130 From table xxiii  $\sqrt{R} = 866$  From table xxiii  $\sqrt{R} = 866$  From table xxiii V = 3 56, which agrees nearly with the value assumed, and confirms the co efficient 130 From table xxiii A = 7 07 Then Q = 7 07  $\times$  3 56 = 25 17 c ft per second Since the pipe is W I a deduction should be made As the pipe is rather large deduct 10 per cent, making Q = 22 65 c ft per second

Example 2 —Using Smith's co efficients, design a pipe to carry 20 c ft per second, the fall being 10 ft in 5000

Assume D=2 ft From table xxIII A=3 142 sq ft and  $\sqrt{R}=707$  Also  $V=\frac{20}{3.14}=6$  37 ft per second From table xxI

C=129 From table xxvii  $C\sqrt{R}=912$  This value does not appear in table xxvii , look out 182 4, which gives (for  $S=\frac{1}{160}$ ) V=8 16, V is 4 08, which is too low, that is, the assumed

diameter was too small Let D=2.5 ft From table xxiii A=4.91 and  $\sqrt{R}=791$ 

Also  $V=\frac{20}{491}=407$  ft per second From table xxv C=128 From table xxvi  $C\sqrt{R}=101$  From table xxvii V=452 ft per second which is too high The diameter 25 ft is thus slightly in excess of what is required To find the actual discharge, C (for V=45) is 1295,  $C\sqrt{R}$  is 1024, V is 458, and Q is  $458\times491=2249$  c ft per second

Since  $\left(\frac{2}{2}\frac{4}{6}\right)^{\frac{1}{2}} = \left(\frac{14}{15}\right)^{\frac{1}{2}} = \frac{12}{15}$  nearly, a 2 ft 4 in pipe would

be too small

Example 3—A 1½ ft C I pipe has to carry a discharge of 18 c ft per second. What will the gradient be Famings coefficient to be used. From table xxiii. A=1.77. Then V=18=10.2 ft per second. From table xxiii. C=117 and C=10.2 per second. From table xxiii. C=117 and C=10.2 per second. From table xxiii. C=117 and C=10.2 per second. From table xxiii.

 $\sqrt{R}$ = 612 From table xxv1  $C\sqrt{R}$ =71 6 and 71 6 x 1414=10 23 Therefore S = 020 is correct.

Example 4 -A pipe 2 in in diameter and 20 ft long connects two reservoirs, the head being I ft and the pipe projecting into the upper reservoir Find the discharge, using Fanning's coefficients

The pipe being short, the loss of head at entrance must be allowed for This (art 1) is  $z_a=1.93 \frac{V^a}{2a}$  Suppose V to be 4 ft per second Then from table 1  $\frac{V^2}{2\sigma}$  = 25 and  $z_e$  19 48 This loss occurs in the length of, say, 4 ft, so that  $L{=}19\,6$  ft and  $S = \frac{1.0 - 48}{10.6} = 027$  From table xxiv S = 040 is the slope which gives V=40, so that V has been assumed too high

Let V be 3 5 ft per second Then  $\frac{V^2}{2g} = 19$ , and  $\tau_a$  is 37, and  $S = \frac{10 - 37}{196} = 032$  Table xxx does not give this slope exactly, but evidently C is about 97 From table xxiii JR is 204 In table xxv1 look out 408 Then  $C\sqrt{I}$  is  $\frac{39.6}{9}$  = 19.8 The slope S= 032 is steeper than those in the tables Therefore calculate  $\sqrt{S}$ , which is 18, and  $C\sqrt{RS}$ , which is 198 × 18, or 356 ft per second, which is near enough

Example 5 -An open stream discharging 16 c ft per second 15 passed under a road through a syphon or tunnel of smooth plastered brickwork of section 2 ft x2 ft, which first descends 10 ft vertically, then travels 80 ft horizontally, and again rises 10 ft vertically, the bends being right-angled and sharp What is the loss of head in the tunnel?

Here  $V=\frac{16}{4}=4$  ft per second There are 4 elbows of 90° each That at the entrance to the tunnel is opposite in direction to the second Here the total loss of head from the elbows is  $4 \times 984 \times \frac{V^2}{2a} = 984 \text{ ft}$ 

To find the approximate loss of head from friction let Fannings co efficients be used Then R= 5 C=117, S= 0024 The fall in 100 ft is 24 ft The total loss of head is thus 98+ 24=1 22 ft

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_		XXIII —V	LUES OF	A AND	R FOR CIPCULAR PIPES
Di	ameter (D)	Sectional Area (A).	Hydrauli Radius (A	c √E	Remarks
<u> </u>		Area (A).  S Square Feet 00136 00307	Feet   Olive   Feet   Olive   100		

PIPFS

## TABLES XXIV. AND XXV —CO-FFFICIENTS FOR PIPES CORFF SPONDING TO GIVEN DIAMETERS AND VELOCITIES (Art 9)

The small figures in table xxis show, nearly, the slopes which give the velocities entered in the heading, and they can be used to show the approximate slopes when the co efficients in table xxv are used

XXIV -Fanning's Co-efficients

Dis	Velocities in Fret per Second.											
meter (Pipe	1	5	1	:	3	4	6	10	15	~0		
nches		-								!		
1	43	51	76	019	93	94	371	100	102	10:		
- ₹	50	75	79	88	93	96	98	101	103	10-		
1	73	77	81	1032	94	112 94	213	102	104	103		
,, ]		81	-0043	100	-045	1083	180	47		1		
11	77		86	90	94	-0.º	1*0	102	104	10:		
2	85	88	90	-020	96	1040	101	104	106	100		
3	89	92	93	96	98	100	102	105	106	106		
4	93	93	95	97	100	102	103	143 106	108	108		
6	94	95	1	0019 100	102	1019	1039 106	107 108	109	111		
- 1		l	97	0032	100"0	-012	10%	0.0				
B Feet.	96	97	99	102	101	105	107	110	112	113		
1	98	100	102	105	106	108	110	114	115	110		
15	i '	104	106	109	°200°	113	112	117	118	1		
2		109	111	114	0019 11G	10034	118	12I	122			
3			1	1000x3	10014	-00°4	10051	-014				
1		117	118	121	123	124	127	128	129			
4		127	128	129	131	132	135	135	136			
5		134	135	136	137	137	138	142	142			
6		137	137	137	140	00067 141	143	147	147			
7		141		00014	1000032	147	148	0031 151	le1			
			143	143	146	100045	100097	100 4	- 1			
8		149	150	151	151	152	155	158	158			

# Table XXVI — Continued — Values of $C \swarrow R$ for various Values of C and $\swarrow R$

For a value of C lower than 90 look out double the value and halve the result

For a value of C over 140 look out half the value and double the result

of <i>C</i>	559	5-7							
	í — —		595	612	609	646	652	677	70~
	503	519	53 6		56 6	58 1	59 6		
91	50 9	52 5	54 2		57 2				
92	51 4	531	547	563					
93	520	53 7	55 3	57 9					
94	525	542	55 9	576	59 1				
95	53 1	548	56 5	58 1	598				
96	53 7	55 4	57 1	58 8	60 4				
97	54 2	56 0	577	59 4	61 0				
98	548	56 5	58 3	60 0	61 6				
99	553	57 1	58 9	60 6	623				
100	55 9	577	59 5	61 2	62 9				707
101	56 5	58 3	60 1	618	63.5	65 3	66 9		71 4
102	570	58 9	60 7	62 4	64 2	65 9	67.5		721
103	576	59 5	61 3	63 0	648	66 5	68 2	69 7	728
104	58 1	60 0	61 9	63 6	65 4	67.2	68 8	70 4	73 3
105	58 7	60 6	62.5	64 3	66 0	67 8	69 5	71 1	74.9
106 107	593	61 2	63 1 63 7	64 9	66 7	68 5	702	72 4	757
107	59 8 60 4	617	64 3	66 1	673	69 1	708	73 1	76 4
108	60 9	62 9	649	667	68 6	70 4	72 2	73 8	771
110	615	63 5	65 5	67 3	69 2	711	728	74 5	778
111	62 1	641	66 1	67 9	698	1 717	73 5	732	780
112	62 6	64.6	66 6	68 5	70 4	72 4	741	758	792
114	63 7	G. 8	67.8	698	717	73 6	75.5	77.2	80 6
116	648	66 9	69 0	710	73 0	74 9	768	785	820
118	66 0	68 1	70 2	72 2	74 2	762	761	799	83 4
120	67 1	69 2	714	73 4	75.5	77.5	79 4	81.2	848
22	68 2	704	726	747	76 7	788	808	826	863
24	693	715	738	759	780	801	82 1	839	877
26	704	72 7	750	771	793	814	83 4	853	89 1
28	716	739	762	783	80 5	827	847	86 7	90 5
30	727	750	774	796	818	840	86 1	880	919
32	738	762	785	808	830	853	874	89 4	933
34	74 9	77.3	79 7	82 0	843	866	88 7	90 7	947
36	760	78 5	80 9	83 2	85 5	87 9	90 0	921	96 2 97 6
38 40	77 1	79 6 80 8	82 1	84 5 85 7	86 S 88 1	89 1 90 4	91 4 92 7	93 4	970

Table XXVI — Continued — Values of C 
ightharpoonup R for various Values of C and ightharpoonup R

For a value of C lower than 100 look out double the value and halve the result.

For a value of C over 160 look out half the value and double the result

Values				alues of 🎶	r.		
oft	-36	~64	~91	817	241	-866	-901
100	73 6	764	79 1	817	84 1	86 6	90 1
101	743	77-2	799	82 5	84.9	87.5	910
102	751	77.9	80 7	83.3	85 8	88 3	919
103	75.8	787	81.5	84.2	86 6	89 2	92 8
104	76.5	795	823	850	87.5	901	93 7
105	77.3	80.2	83 1	85.8	88.3	909	94 6
106	780	81 0	83.8	866	891	918	95.5
107	788	817	84 6	87 4	90.0	927	96 4
108	795	825	85 4	88 2	908	935	97.3
109	80-2	83 3	86-2	891	917	944	98 2
110	810	840	87.0	899	92 5	953	99 1
111	817	84.8	87.8	907	93 4	96 1	1000
112	82 4	856	88.6	915	942	970	1009
113	83 2	863	894	923	95 0	979	1018
114	83 9	871	90 2	93 1	959	987	102 7
115	84 6	879	910	940	96 7	996	1036
116	85 4	886	918	948	976	100 4	1045
118	868	90-2	933	96 4	99 2	102 1	106 3
120	883	917	94 9	980	100 9	103 9	108 1
122	898	932	965	99 7	1026	105 6	1099
124	913	947	98 1	101 3	104 2	1073	1117
126	927	963	996	102 9	105 9	1090	1135
128	94 2	978	101 2	104 5	107 6	1108	1153
130	95 7	993	1028	106 2	109 3	1125	1171
132	97 2	1008	1044	1078	1110	1142	1189
134	98 6	1024	106 0	109 4	1127	1159	120 7
136 138	100 0	1039	107.5	111 1 112 7	1143	1177	122 5 124 3
140	1016	10a 4	109 1	114 3	1177	121 2	126 1
142	104 5	106 9 108 4	1107	1160	1194	122 9	127 9
144	105 9	1100	1139	1176	121 1	124 7	129 7
146	107 4	11115	1155	1192	122 7	126 4	131 5
148	108 9	11130	1170	120 9	124 4	1281	133 3
150	1104	1146	1186	122 5	1261	129 8	135 1
152	1118	1161	120 2	124 1	127 8	131 6	136 9
154	113 3	1176	121 8	1257	129 4	133 3	138 7
156	114 8	1191	123 3	1274	131 1	135 0	1405
158	1163	120 7	124 9	129 1	132 8	1367	142 3
160	117 7	122 2	126.5	130 7	1345	138 5	144 1

# Table XXVI — Continued — Values of $C \ \ \ /R$ for various Values of C and $\ \ \ \ /R$

For a value of G lower than 100 look out double the value and halve the result

For a value of C over 160 look out half the value and double the result

Values		Values of √P											
of C	93.	95"	1.00	1-061	1 118	1 1 3	1*.						
100	93 5	967	100 0	106 1	111 8	117 3	122						
101	94 4	97 7	101 0	107 1	1129	1185	123						
102	95 4	986	102 0	108 2	1140	1196	124						
103	963	996	1030	1093	1151	1208	126						
104	97 2	100 6	104 0	110 3	116 2	121 9	127						
105	98 2	101 6	105 0	1114	1173	123 1	128						
106	99 1	102 6	106 0	1124	1185	124 3	131						
107	100 1	103 5	107 0	1135	1196	125 5	132						
108	100 9	104 4	108 0	114 5	120 7	126 6	133						
109	1018	105 4	109 0	115 6	1218	127 8 129 0	134						
110	1028	106 3	1100	1167 1178	122 9 124 0	130 2	135						
111	103 7	107 3	111 0			130 2	137						
112	104 7	108 3	1120	118 8 119 9	125 1 126 2	132 5	138						
113	105 6	109 2 110 2	113 0 114 0	120 9	127 3	133 6	139						
114	106 5	11112	1150	122 0	128 4	134 8	140						
115	107 5 108 4	112 1	1160	123 0	129 6	1360	142						
116 118	1103 4	1140	1180	125 1	131 8	138 3	144						
120	112 2	1160	1200	127 3	134 1	1407	147						
122	114 1	117 9	1220	129 4	136 3	143 0	149						
124	1159	1198	124 0	131 5	138 5	145 3	151						
126	1178	121 7	126 0	133 6	1407	1476	154						
128	1196	123 7	128 0	135 7	143 0	150 0	156 8						
130	121 5	125 6	130 0	137 8	145 2	1523	159						
132	123 8	127 6	132 0	1400	147 5	1547	161 0						
134	125 2	129 5	1340	142 1	1497	157 0	164 0						
136	127 1	131 5	1360	1442	1520	159 4	168 9						
138	129 0	133 4	138 0	1463	154 2	161 7	168 9						
140	130 9	135 3	1400	148 5	156 5	1642	1739						
142	1328	137-2	1420	150 6	1597	166 5 168 8	1764						
144	134 6	139 1	144 0	152 7	160 9 163 I	171 1	178 8						
146	136 5	141 0	1460	154 8 156 9	1654	173 5	151 7						
148	138 3	143 0	148 0 150 0	159 0	167.6	1758	1837						
150	1402 1420	144 9 146 9	1500	161 2	169 9	178 2	186 1						
152	143 9	1488	154 0	163 3	1721	180 3	188 5						
154	145 8	150 8	1560	165 4	174 4	1829	191 0						
156 158	147 7	152 7	158 0	167.5	1766	1852	1934						
160	149 6	154 7	160 0	169 7	178 8	187 6	146.0						

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### TABLE XXVII -VALUES OF S AND JS

## (For steep slopes not included in Table XXVIII )

To find  $\sqrt{S}$  for a steeper slope, look out a slope 4 times as flat and multiply  $\sqrt{S}$  by 2 Thus, for 1 in 50,  $\sqrt{S}$  is  $07071 \times 2 = 14142$ 

Slope 1 in	Fall per Pont or S	√S	Slope Lin	Fall per Foot or S	√S
100	-010	1	230	004348	-06594
105	-0095238	09759	240	004167	66455
110	1009091	095346	250	004000	06325
115	-008696	093250	260	003847	06202
120	-008333	091287	270	003704	-06086
125	008	-089442	280	003571	05976
130	007692	08771	290	003448	-05872
135	-007407	09607	300	-003333	05774
140	007143	08452	310	003226	05680
145	-006897	-08305	320	003125	05590
150	006667	-08165	330	-003030	0ა505
15s	-006452	08032	340	002941	05423
160	100625	-07906	350	002857	05345
165	006061	-07785	360	-06278	05271
170	-005882	-07670	370	002703	05199
175	005714	07559	380	002632	05130
150	003556	*07454	390	002564	05064
185	-005403	-07352	400	0025	05
190	00ა263	07255	420	002381	04880
195	-005128	·07161	440	*002273	04767
200	-005	07071	460	002174	-04663
210	004762	06901	480	000083	04564
220	004545	06742	500	002	04472

Note to table xxxxx —This table shows values of V for given values of  $C\sqrt{R}$  and  $\sqrt{S}$ 

The first line of the heading shows  $\frac{1}{S^2}$ , the third line  $\sqrt{S}$ . The figures in brackets show the amount by which  $\frac{1}{S}$  must be altered to alter  $\sqrt{S}$  and l by 1 per cent. Thus for  $S = \frac{1}{2}\frac{1}{2}$  the slopes  $\frac{1}{2}\frac{1}{2}$ , and  $\frac{1}{2}\frac{1}{2}$  for event more or less than in the table. For  $C\sqrt{R} = 103$ , V is 2.32 and 2.23 feet per second.

TABLE XXVIII (See note on preceding page)

Values of	500 (10) 104472	550 (11) 04264	600 (12) 04083	6.0 (13) 0392	700 (14) 0378	(15	) (	100 16) 3536	900 (18) -03333
100	4 47	4 26	4 08					54	8 33
102	4 56	4 35	4 17	4 00					3 40
104	4 65	4 44	4 25	4 08				68	3 47
106	4 74	4 54	4 83	4 16					8 53
108	4 83	4 61	4 41	4 24				82	3 60
110	4 92	4 69	4 49	4 31				89	3 67
112	5 01	4 78	4 57	4 39				96	3 70
114	5 10	4 86	4 66	4 47				03	3 80
116	5 19	4 95	4 74	4 55				10	3 87 3 93
118 120	5 28 5 37	5 03	4 82	4 63				17 24	4 00
123	5 37	5 12 5 25	4 90 5 02	4 71	4 5				4 10
126	5 68	5 37	5 15	4 82					4 20
129	5 77	5 50	5 27	5 06	4 76				4 30
132	5 90	5 63	5 89	5 18	4 99				4 40
135	6 04	5 76	5 51	5 30	5 10				4 50
138	6 17	5 88	5 64	5 41	5 22				4 60
141	631	6 01	5 76	5 53	5 33				4 70
144	6 44	6 14	5 88	5 65	5 44	5 20			4 80
147	6 57	6 26	6 00	5 77	5 56	6 37			4 90
150	671	6 40	6 13	5 88	5 67	5 48	5 5	9A	5 00
153	6 84	6 52	6 25	6 00	4 78	5 59	5 1		5 10
156	6 98	6 65	6 37	6 12	5 90	5 70			6 20
160	7 16	6 82	6 53	6 28	6 05	5 84		6	33 5 17
164	7 33	6 99	6 70	6 43	6 20	5 99		(0)	J 60
168	7 51	7 16	6 86	6 59	6 35	6 14	1		7 73
172 176	7 69 7 87	7 33	7 02	6 75	6 50	643			# 87
180	8 05	7 68	7 35	7 06	6 80	6 57	100		2 00
185	8 27	7 89	7 55	7 26	6 99	6 76	- G 5	iΤ	6 17
190	8 50	8 10	7 76	7 45	7 18	6 94	67	3	6 83
195	8 72	8 32	7 96	7 65	6 37	7 12	69		6 60
200	8 94	0.53	8 17	7 84	7 56	7 30	7 0		6 67
205	8 17	8 74	8 37	8 04	7 75	7 49	7.2		6.83
210	9 39	8 95	8 57	8 24	7 94	7 67	7 4		7 00 7
215	9 62	9 17	8 78	8 43	8 13	7 85	7 60		7 33
220	984	9 38	8 98	8 63	8 32	8 03	7 76		7 50
225	10 1	9 59	9 19	8 82	8 51	8 22	8 13		7 67
230 235	10 3 10 5	9 81	9 89	9 02	8 69 8 88	8 58	8 31		7 83
240	10 7	10 2	9 80	9 41	9 07	8 77	8 49		8 00
246	11 0	10 5	10 0	9 65	9 80	8 98	8 70	11	8 20
252	11 3	10.8	10 3	9 88	9 53	9 20	8 91		8 40
258	11 5	110	10 5	10 1	9 75	9 42	9 12		8 00
264	11.8	11 3	108	10 4	9 98	964	9 34		03.8
270	121	11 5	110	10 6	10 2	9 86	9 55		9 00
276	123	11.8	11 3	108	10 4	10 1	9 76	+ 7	9 40
282	126	120	11.5	11 1	10.7	10 3 10 5	10 2		100
288	12 9 13 2	12 8 ' 12 5	11 8 12 0	11 3 11 5	10 9 11 1	10 5	10 4		68
294 800	13 4	12.8	12 3	11 8	11 3	11 0	10 6	10	0 0
ا ۵۰۰۰	.0 2	-20							

TABLE XXVIII -Continued.

Talmes	300	2 100	1 707	1 200	1,400	1500	1 000	1 500	2000
1 61	(1%)	(-1)	(24)	(2)	(24)	(30)	(32)	(7)	(39 41)
CVT	-01165	403(15	40"817	454	₹°₹\$	402.42	100-00	1,3,4	0>19
		_							
1	3 16	3 02	2.67	2 77	247	2 58	2 00	2 35	2 21
100	3-23	3 (08	2.25	2 83		2-63	2 55	2 40	2 28
	3 20			289	2 73	2 68	2-00	2 45	2 33
104	2 25	3 14	3.00	291	2 78 2 83	274	265	250	2 37
103	3 42	3-20	3 12	300	2 89	2 79	2 70	2 65	2.42
liio	3 48	3 72	3 18	345	201	261	2 76	2 69	2 46
1112	374	321	323	311	2-00	2 60	2 80	261	2 61
116	2.00	344	329	3 16	305	201	2 85	2 69	2 55
iii	3 67	3 40	2 35	3 22	S 10	3.00	200	2 73	2 59
118	8 77	3 56	8 41	327	3 15	3.05	9.95	2 78	2 61
120	3 73	3 62	3 46	8 57	3 21	3 10	2.00	2 83	2 68
123	3 50	3 71	2 55	3 41	3.21	3 18	3.03	290	2.75
126	7.98	3 60	3.0	3 50	3 37	8.45	3 15	2 97	2 82
129	4-09	3 60	371	3 38	3 45	3 33	3 23	3-01	2.68
132	4 17	349	3 81	3-66	8 53	3 41	3 20	3 11	2-95
1135	4:27	4-07	840	8 74	3-01	3 49	3 38	3 18	3-02
108	4 76	4 16	3 29	3 83	3-69	3 76	3 15	3 25	8-09
141	4 46	4.25	4:07	4.91	4 77	3 61	3 53	3 32	3 15
144	4 55	4 34	4 16	4 (0)	3.85	3 72	3-60	3 32	3 22
117	4 65	4 43	421	1.08	3-113	3 80	3 68	3 47	3 20
150	4 74	4 52	4 23	4 16	401	3 87	3 75	251	3 35
163	4 81	4.61	4 42	4:21	4 00	3-95	3 83	3 61 3 68	8 40
156	4-93	4 70	4 50	4 33	1 17	4-03	4-00	3 77	3 68
100	5.06	4.83	4 62	4 44	4-23	4 13 1	4 10	3 87	3 67
164	5 19	4-95	4 73	4 55	4 49	4 31	4 20	3 96	8 76
168 172	6 81	5-07	4.85	4 77	4 60	4 44	4 30	4.05	3 85
176	5 55	5 19 5 81	616	488	4 70	4 54	4 40	4 15	3 74
150	6 6 3	6 43	6-20	4-99	4 81	4 61	4 50	4 21	4.03
185	85	6 58	5 21	6 13	4 95	4 74	4 63	4 36	4 14 1
190	6-01	5 73	5 49	5-27	5-03	4 91	4 75	4 48	4 25
195	6 17	5 88	5 63	6 41	5 21	5-01	4 88	4 60	4 86
200	6 32	6-03	5 77	5 55	5 85	5 16	5-00	4 71	4 47
205	6 48	6 18	5 93	5 69	5 48	5.29	5 13	4 83	4 58
210	G C4	6 33	C 06	5 83	6 G1	5 42	5 25	4 95	4 70
215	6.80	6 48	6-21	5-96	6 75	5 55	5 38	5 07	4 81
220	6.96	6-63	6 35	6 10	5 88	5 68	5 50	5 19 5 20	5 03
225	7 11	G 78	6.50	6 21	6 02	6 81 6 94	5 75	5 42	5 14
230	7 27	6 91	6 64	6 38	6 15 6 28	6 07	5 88	5 54	5 26
235	7 43	7.00	6.78	6 53	6 42	6 20	6 00	5 86	5 37
240 246	7 59	7 24	6.93 7.10	6 82	6 58	6 35	6 15	6 80	5 50
252	7.97	7 60	7-29	6 99	6 74	6 61	6 30	5 94	5 64
258	8 16	7 78	7 45	7 16	6 90	6 66	6 45	6 08	5 77
264	8 35	7 96	7 62	7 32	7 06	6 82	6 60	6 22	5 90
270	8 54	8 14	7 79	7 49	7 22	6 97	6 75	6 36	6 04
276	8 73	8 32	7 97	7 66	7 39	7 13	6 90	6 51	6 17
282	8 92	8 50	8 14	7 82	7 55	7 28	7 05	6 65	6 44
288	9 11	8 68	8 32	7 99	7 80	7 44	7 20	6 93	6 57
294	9 30	8 86	8 49	8 16 8 32	7 96 8 02	7 59 7 75	7 50	7 07	671
300	9 49	9 05	8 66	8 32	100-	1 " "	1	۱ ۰۰ ۱	
1	1	1	1	1	1				

TABLE XXVIII -- Continued.

				_							
Value of CVR	2 °06 (43 45 '0°13	(47 49	9) (53 6	5) (59 6	1) (65	67) (	600 1 ~3) 1667	4 C (79 01:	81) (89	500 91) 491	5 000 (%) 10°°) 01414
100	2 18							14		49	1 41
102	2 18					8   1	70			52	1 44
104	2 22						78			55	1 47
106	2 20					5   1	77			58	1 50
108	2 80					18   1	80			61	1-53
110	2 35						83			64	1 56
112	2 39						87	17		57	1 58
114	2 43						90			70	1 61
116	2 47		2 23				93	18		73	1 64
118	2 52	2 41	2 27				97	18		6	1 67
120	2 56		2 31	2 19			00	19		79 j	1 70
123	2 62						05	14		33	1 74
126	2 69	2 57	2 43				10	19		38	1 78
129	2 75	2 68					15	20		2	1 82
132	2 82	2 69					20	20		7	1 87
135	2 88	2 76					25	21		1	191
138	2 94	2 82	2 66				30 J	2 1		16	1 95
141	8 01	2 88	2 72	2 58			35	2 2			1 99
144	3 07	2 94	2 77	2 68			40	2 2			2 04
147	3 13	3 00	2 83	2 68			45	2 82			2 08
150	3 20	3 06	2 89	2 74	26		50 J	2 37			2 12
153	3 26	8 12	2 95	2 79		2	55	2 42			2 16 2 21
156	3 33	3 18	3 00	2 85	2 7.			2 47			2 21 2 26
160	8 41	3 27	3 08	2 92	2 79		37	2 53			2 32
164	3 50	8 35	3 16	3 00	2 80		8	2 59			2 38
168	3 58	3 43	8 23	3 07	2 93			2 66			2 43
172	3 67	3 51 3 59	3 31	3 14	3 00		7	2 72 2 78	2 57		2 49
176			3 39	3 21 2 29	3 07		3		2 68		2 55
180 185	3 84	3 67	3 47	2 29	3 13	3 0	0	2 85 2 93	2 70		2 62
190	4 05	3 88	3 66	3 47	3 31	3 1		3 00	2 83		2 (3
195	4 16	3 98	3 75	3 56	3 50	3 2		3 08	2 91		2 76
200	4 26	4 08	3 85	3 65	3 48	3 3		3 16	2 98		283
205	4 37	4 18	8 95	8 74	3 57	34		3 24	2 00		2 00
210	4 48	4 29	4 04	3 84	3 66	3 5		3 32	3 13		2 97
215	4 58	4 39	4 14	3 93	3 74	3 5		3 40	3 21	2	101
220	4 69	4 49	4 24	4 02	3 83	8 6		3 48	3 28	1 8	
225	4 80	4 59	4 33	4 11	3 92	3 7	51	3 58	3 86		18
230	4 90	4 69	4 43	4 20	4 00	3 8		3 64	3 43		25
235	5 01	4 80	4 52	4 29	4 09	3 9	3   3	3 72	8 50	3	
240	5 12	4 90	4 62	4 38	4 19	4 0		3 79	3 58	3	
246	5 25	5 02	4 74	4 49	4 28	4 10		89	8 67	3	48
252	5 37	5 14	4 85	4 60	4 39	4 20		3 99	8 76	3	56
258	5 50	5 27	4 97	471	4 49	4 30		1 08	3 85	3	65
264	5 63	6 29	5 08	4 82	4 60	4 40			8 71		1 28
270	5 76	5 51	6 20	4 93	4 70	4 50			4 03		56
276	5 88	5 63	5 31	5 04	4 81	4 60			4 12		0.)
232	6 01	5 76	5 43 5 51	5 15	4 91	4 70	4		4 20		67
298	6 11	5 88 6 00		5 26	5 01	1 80	1 4		1 38		16
214 300	6 27	6 12	5 66 5 78	5 37	5 12 6 22	8 00	1 4	74	4 47	14	
300	040	712	7 10	240	ندن ن	0 00	1 -	"		1	

TABLE XXVIII -Continued

Values of	5 500 (103 112)	6 000	6 500 (1°8 13°)	7 000	7 500	8 000	8 500	9 000	10 000
CVF	-01349	101001	01240	01195	01155	01118	01085	01054	0100
_	<del>                                     </del>	<u>'</u>	<u>'</u>			<del> </del>	\ <del></del>		
100	1 35	1 29 1 32	1 24	1 20	1 16	1 12	1 00	1 05	1 00
102 104	1 38	1 32	1 47 1 29	1 22 1 24	1 18 1 20	1 14	1 11	1 08	1 02
106	1 43	1 37	1 32	1 24	1 22	1 19	1 15	1 12	1 06
108	1 46	1 39	1 34	1 29	1 25	1 21	1 17	1 14	1 08
110	1 48	1 42	1 36	1 32	1 27	1 23	1 19	1 16	1 10
112 114	1 51	145	1 39	1 34 1 36	1 29 1 32	1 25 1 27	1 22	1 18	1 12
116	1 57	1 56	1 44	1 36 1 39	1 32	1 30	1 26	1 22	1 16
118	1 59	1 52	1 46	1 41	1 36	1 32	1 28	1 24	1 18
120	1 62	1 55	1 49	1 43	1 39	1 34	1 30	1 27	1 20
123 126	1 66	1 59	1 53	1 47	1 42	1 38	1 31	1 30	1 23 1 26
120	1 74	1 63	1 56	1 51	1 46	1 41	1 40	1 36	1 20
132	1 78	1 70	1 64	1 58	1 53	1 48	1 43	1 39	1 32
135	1 83	1 74	1 66	1 61	1 56	1 51	1 47	1 42	1 35
128	1 86	1 78	1 71	1 65	1 59	1 54 1 58	1 50	1 45	1 38
144	1 94	1 82	1 75 1 79	1 69 1 72	1 63 1 66	1 58 1 61	1 53 1 56	1 52	1 44
147	1 98	1 90	1 82	1 76	i 70	1 64	i co	1 56	1 47
150	2 02	1 94	1 86	1 79	1 73	1 68	1 63	1 58	1 50
153 156	2 06 2 11	1.98 2.01	1 90	1 83	1 77	1 71	1 66 1 69	1 61 1 64	1 53
160	2 16	2 07	1 93	1 87 1 91	1 80	1 79	1 74	1 69	1 60
164	2.21	2 12	2 03	1 96	1 89	1 83	1 78	1 78	1 64
168	2 27	2 17	2 08	2 01	1 94	1 88	1 82	1 77	1 68
172 176	2 32 2 37	2 22	2 13 2 18	2.06	1 99 2 03	1 92	1 87 1 91	1 81 1 86	1 72 1 76
180	2 43	2 27 2 32	2 23	2 10 2 15	2 08	2 01	1 95	1 90	1 80
185	2 50	2 39	2 30	2 21	214	2 07	2 01	1 95	1 85
190	2 56	2 45	2 36	2 27	2 20	2 12	2 06	2 00	1 90
195 200	2 63	2 52 2 58	2 42 2 48	2 33	2 25 2 31	2 18 2 24	2 12 2 17	2 06 2 11	1 95 2 00
205	2 77	2 65	2 54	2 45	2 37	2 29	2 22	2 16	2 05
210	2 83	2 71	2 60	2 51	2 43	2 35	2 28 2 33	2 21	2 10
215 220	2 90	2 78	2 67 2 73	2 57	2 48 2 54	2 40 2 46	2 23 2 29	2 27 2 32	2 15
225	2 04	2 84 2 91	2 73 2 79	2 63 2 69	2 60	2 52	2 44	2 37	2 20 2 25
230	3 10	2 97	2 85	2 75	2 66	2 57	2 50	2 42	2 30 1
235	8 27	3 03	2 91	2 81	2 72	2 63	2 55	2 48	2 35
246	8 24	3 10 3 18	2 98	2 87 5 94	2 77 2 84	2 68 2 75	2 60 2 67	2 53 2 59	2 40 2 46
252	3 40	8 25	3 13	3 01	2 91	2 82	2 74	2 66	2 52
258	3 48	8 83	3 20	3 08	2 98	2 88	2 80	2 72	2 58
264 270	8 56	3 41	3 27	3 16	3 05	2 95 3 02	2 86 2 93	2 78 2 85	2 64 2 70
276	3 64 3 72	3 48	3 35 8 42	3 23	3 12	3 02	3 00	2 91	2 76
282	8 80	3 64	8 50	3 87	3 26	3 15	3.06	2 97	2 82
288	3 89	3 72	3 57	3 44	3 33	3 22	8 13	3 04	2 82 2 88 2 94
294 800	3 97	3 80	3 65	3 51	3 40	3 29 3 35	3 19 3 26	3 16	8-00
300	1 3 03	- 01	0 12	333	0 11	1 - 20	1 20		

### CHAPTER VI

### OPEN CHANNELS-UNIFORM FLOW

[For preliminary information see chapter it articles 8 16 and 22 24]

## Section I - OPEN CHANNELS IN GENERAL

1 General Remarks -- Uniform flow can take place only in a uniform channel Strictly speaking, a uniform channel is one which has a uniform bed slope, and all its cross sections equal and similar, but if the cross sections, though differing somewhat in form, as in



Fig 98, are of equal areas and equal wet borders, the channel is to all intents and purposes uniform, provided the form of the section changes gradually term 'uniform channel' will be used in this extended sense 1 Breaches of uni-

formity in a channel may be frequent, and the reaches in which the flow is variable may be of great length. The flow in a unit form channel is thus by no means everywhere uniform are for convenience treated of in chap vii, but flow round a bend may be uniform Thus a uniform stream need not be assumed to It will be seen hereafter (chap vii art 16) that nearly everything which is true for uniform flow is true, with some modifications, for variable flow

The mean depth D (Fig 99) of a stream is the sectional area A divided by the surface width W



Since A = DW = RB, therefore the hydraulic radius is less than the mean depth in the same ratio as the surface

width is less than the border

will often assist in forming an idea of the hydraulic radius greater the width of a stream in proportion to its depth, and the

1 If R varies in the opposite manner to S the flow may be uniform in a variable channel, but this is very rare

fewer the undulations in the border, the more nearly will the surface-width approach to the border and the hydraulic radius to the mean depth. If the depth of water in a channel alters, the hydraulic ridius alters in the same manner. When the water-level rises A increases faster than W, and R therefore increases, but  $\frac{W}{B}$  decreases (unless the side-slopes are flat), so that R increases less rapidly than D. For small changes of water level R and D both change at about the same rate

2 Laws of Variation of Velocity and Discharge —For orifices, werrs, and pipes it was possible to describe in a few words the general laws according to which the velocities and discharges vary, but for open stream it is not so One law is simple, and that is, that for any channel whitever V and Q are nearly as  $\sqrt{S}$  To double V or Q it is necessary to quadruple S. For other factors it is necessary to consider the shape of the cross section

For a stream of 'shallow section,' that is, one in which H' greatly exceeds D, a change in W has hardly any effect on R or on V, while Q is directly as W Also R is very nearly as D For depths not very small C is approximately as  $D^{\frac{1}{2}}$ , so that V is as Di In this case, if D is doubled, V is increased in the ratio 1 59 On comparing velocities, taken from tables, for channels from 8 to 300 feet wide with sides vertical, or 1 to 1, and with various velocities, the actual ratio is found to vary from 1 52 to 173 If the sides are steep A is nearly as D, and Q therefore as Di or thereabouts For a stream of 'medium section'-that is, one in which W is 2 to 6 times D-with vertical sides A is as D. and for moderate changes of water level and depths not very small V is nearly as  $D^{\frac{1}{2}}$ , so that Q is as  $D^{\frac{1}{2}}$  Both these kinds of section are extremely common A flattening of the side slopes may make Q vary as  $\tilde{D}^{\circ}$  If a stream has vertical sides and a depth far exceeding its width-a rare case-the effects of W and D are reversed For a triangular section-used for small drains-R is as D, A as D, C probally as D, and Q as D3

For other kinds of section no definite laws can be framed, but the effect of D is nearly always greater than that of W, so that D is the most important factor in the discharge, especially if the side slopes are flat, and S is always the least important factor

supes are nat, and 31 saways the least important factor in If two streams have equal discharges, and have one factor in the discharge equal, the approximate relation between the other two fretors can be found I et two streams of shallow section have equal slopes, and let one be twice as deep as the other. The

latter must be (2)5 or 3 2 times as wide as the first This law is nearly the same as for werrs When two reaches of a canal have different bed slopes, but equal and similar cross sections, the depth of water is, of course, less in the reach of steeper slope If the discharge is approximately as S1D, the depths in the two reaches will be inversely as the fourth roots of the slopes The velocities are inversely as the depths, and are, therefore, as the fourth roots of the slopes A change of 40 per cent in the slope will cause a change of only about 10 per cent in the velocity, and a change of the same proportion, but of opposite kind, in the depth of water When the changes in the two factors are relatively small they are inversely as the indices in the formulæ Suppose a stream of shallow section with depth D and slope S gives a certain discharge Q Let D be increased by a small amount  $\frac{D}{n}$  Then the compensatory change in S will be  $\frac{3S}{n}$ 

This principle may be applied in designing a channel to carry a given discharge, whenever for any reason it becomes necessary to

make a slight change in the value first assumed for any factor The discharging power of a stream can be increased by in creasing the depth of water, the width or the slope, the last being often effected by cutting off bends The efficiencies of these processes are in the order named In any channel having sloping sides both V and Q are more increased by raising the surface level than by deepening the bed by the same amount It follows that embanking a river is more effective than deepening it for in creasing its discharging power and enabling it to carry off floods

It is in fact the most effective plan that can be devised In clearing out the head reaches of Indian mundation canalsso called because they flow only for a few months, when the rivers are swollen-it used to be the custom to place the bed rather high, at the off take, in order to obtain a good slope Of late years it has been the custom to lower the bed giving a flatter slope but a greater depth of water The velocity is about the same in both cases, the increase in depth making up for the decrease in slope, but the lowered bed of course gives a greatly augmented discharge On the other hand, the lowered bed must cause the introduction of water more heavily charged with silt. Moreover, the ratio of

depth to velocity in the canal is greater than before, and this (chip it art 22) tends to cause mere used deposit Under the old system of high beds the heads of the carris silted more or less It has been impossible to find out whether more silt has actually deposited since the introduction of the low level system, because, owing to changes in the course of the river, the same head channel is seld in cleared for several years in succession, and also because the quantity of silt deposited depends on other factors, such as the position of the head, a canal taken off from the highly silt liden main stream silting more than one taken from a side channel Ol viously the tendency of the low hed is to silt more than the high one, but the worst that can happen is its silting up till it assumes the level of the high one. This takes time, and while it is going on an increased discharge is obtained

#### SECTION II - SPECIAL FORMS OF CHANNEL

3 Section of 'Best Form.'-A stream is of the 'best form' when for a given sectional area the border is a minimum, and the hydraulic rudius, therefore, a maximum. The velocity and dis charge are greater than in any other stream of the same sectional area, slope, and roughness. The form which complies with this condition is a semicircle whose diameter coincides with the line of water surface This form is used in concrete channels but not often in others, because of the difficulty of constructing curved surfaces Of rectilineal figures the best form is half a regular polygon. The greater the number of sides the better, but in practice the form of section is usually restricted to that having a bed level across and two sides vertical or sloping The best form for vertical sides is the half square (Fig. 100), and for sloping sides the semi hexagon (Fig. 101). If the angle of the side slopes is fixed (as it generally is) at some angle other than 60°,



the best form is that in which the bed and sides are all tangents to a semicircle (Fig. 102) The bed width is  $D(\sqrt{n^2+1}-n)$  where n is the ratio of the side slopes. In every channel of the best form the hydraulic radius is half the depth of water, and if the section is rectilineal, the surface width is equal to the sum of the two slopes, so that the border is the sum of the surface and bed widths

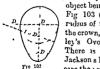
The following statement shows the sectional areas of various channels of the best form All the channels have the same central depth D, the same hydraulic radius  $\frac{D}{a}$  and therefore the same velocity

Description of Cross Section	Sectional Area	Ratio of Sectional Area to that of the In scribed Semicircle
Semicircle, Half square, Sem hexagon, Trapezoid, side slopes ½ to 1, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	1 57 D <sup>2</sup> 2 D <sup>2</sup> 1 732D <sup>2</sup> 1 736D <sup>2</sup> 1 818D <sup>2</sup> 2 106D <sup>2</sup> 2 472D <sup>2</sup> 3 334D <sup>2</sup>	1 00 I 27 I 10 I 11 I 16 I 34 I 57 2 12

A channel of the best form is not usually the cheapest If made of ron, wood, or masonry the cost will probably be reduced by somewhat increasing the width and reducing the depth, thereby enabling the sides to be made lighter, though the length of border is slightly increased In an excavate! channel, where the water surface is to be at the ground level, the best form will give the immuming quantity of work and will be the cheapest if the material exeavated is rock, but if it is earth an increase of with and decrease of depth will reduce the lift of the earth, and therefore the cost It has water surface is not to be at the ground level the cheapest form may differ greatly from the best form

If it is desired simply to deliver a stream of water of given discharge with as high a velocity as possible, the best form is suitable. If the object is to obtain high silt-supporting power, so that the channel may not silt or may seour and charge itself, the question of ratio of depth to velocity must be taken into account, and even when the object is to discourage the growth of weeds the question of depth comes in

If the depth of water in a channel fluctuates, the section can, of course, be of the best form for only one water level Scuers are often made of oval sections in order that the stream may be of the best form, or nearly so, when the water level is low, the



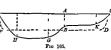
object being to prevent deposits In
Fig 103 (Metropolitan Oood) the
radius of the invert is balf that of
the crown, and in Fig 104 (Hawkes
ley's Oyoid) nearly three-fifths
There is also a form known as
Jackson's Peg top Section In each

Fra 104

Fro 100 case the velocity with the sewer one third full is about three fourths of the velocity when it is two thirds full.

4 Irregular Sections —The cross section of a stream may be called 'irregular' when the border contains undulations or saliences of such a character as to divide the section into well

marked divisions (Fig. 105) In this case the water in each division has a velocity of its own, and in order to calculate the discharge of the whole stream by the use of the



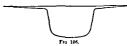
formula  $\tilde{P} = U \sqrt{LS}$ , it is necessary to consider each division separately, finding its hydraulic radius from its area and border. The length AB is not included in the border of either division, since if there is any friction along it, it accelerates the motion in one division and retards it in the other. If  $A_1$ ,  $A_2$  are the sectional areas, and  $b_1$ ,  $B_1$ , the hydraulic radiu,

 $Q_1 = C_1 A_1 \sqrt{R_1} S$   $Q_2 = C_2 A_2 \sqrt{I_2 S}$ 

The discharge of the whole channel calculated from the equation  $Q=CA\sqrt{LS}$ , equals  $Q_1+Q_2$  only when  $R_1=R_2$ , otherwise it is less The more  $R_1$  and  $R_2$  differ, the more Q differs from  $Q_1 + Q_2$ , and for given values of R1 and R2 the difference is greatest when A = A, If either A, or A, is relatively very small, the difference between Q and  $Q_1 + Q_2$  will be small It may happen that  $R_1$  and L. differ greatly with low supplies, and not much with high supplies If without altering either the length of the border or the sectional area of the stream the border be changed to CDLI, the section is no longer irregular, and the equation  $V=\ell\sqrt{L}S$  is the proper one to use There are thus two cross sections with equal values of R and different mean velocities, that is, different values of C Even in a regular section the same principle holds good The discharge is the sum of the discharges of a number of parts and may be affected by a change in the form of the border alone (See also art 13)

An instance of an irregular section occurs when a stream over

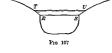
flows its banks (Fig 106) As the overflow occurs the border of the whole stream may increase far more rapidly than the sec



tional area, and Q, if calculated as a whole, would diminish with rise of the water-level. The velocity and discharge of the main

body and of the overflow must be considered separately, and both will increase as the water level rises Similarly, if there we longitudinal grooves or ruts in the bed of a stream, such, for instance, as those caused by longitudinal battens, the water in the grooves has a separate velocity of its own and the velocity of the main body cannot be reduced indefinitely by increasing the number and depth of the grooves, although the border can be increased in this manner to any extent If the river is winding, the spill water, which flows straight, may have a slope greater than that in the river channel, but its velocity may still be very low, especially if the country is covered with crops or regetation Some of the spill water, however, disappears by absorption, and it is clear that in every case it takes off some of the discharge of the river Thus the embanking of a river, so as to shut off spills, must necessarily, to start with, raise the flood level Whether scour of the channel subsequently reduces the level is another matter

5 Channels of Constant Velocity or Discharge —Let A be the area, B the border, and W the surface width of any stream



whose water level is RS (Fig. 107), and let the water level rise to TU, the increase in depth being a small quantity d and the increase in the surface width being 2u. Then if the slopes RT, SU be made such that

RT, SU be made such that  $\frac{(W+w)d}{2\sqrt{d}+w} = \frac{d}{L}$ , the border will have increased in the same ratio is the area, and L will be unaftered. By using the new values of A and B, corresponding to the rused surface, the process can be continued, but the slope becomes rapidly flatter. If the surface falls below LS, R is no longer constant, but decreases. It is impossible to design a section such that R will remain constant is the depth decreases to zero. And even within the limits in which R is constant, the mean velocity is not constant. The channel is irregular, and the velocity, both in the m in body of water and in the minor ones, increases as the water level rise. The investigations which have at times been made to find the equation to the curve of the border when R is constant are useful only as mathematical exercises.

The relocity as the water level rises is nearly constant in a very deep, narrow channel with vertical sides, and it may be kept quite constant by making the sides overhang—as in a sewer running nearly full—but the process is speedily terminated by the meeting of the two sides

To keep the discharge constant for different water levels is still more difficult, but would be of great practical use, especially in irrigation distributaries. It could be effected by making the sides overhang, but they would have to project almost horizontally and would very soon meet, thus giving only a small range of depth. Any form of section adopted for giving either constant clocity or constant discharge must be continuous along the channel from its head for a great distance. If of short length the slope or hydraulic gradient in it would be hable to vary greatly, and with it the velocity. (Cf chap in art 14)

6 Circular Sections —A channel of circular section is an open channel when it is not running full. In such a channel when the hydraulic radius, and therefore the velocity, is a maximum when the angle subtended by the dry portion of the border is 103°, or the depth is 81 of the full depth. If the depth is further increased I. decreases, but at first the increase of area more than compensates for this, and the discharge goes on increasing. When the angle above mentioned is about 52°, or the depth is 95 of the full depth, the expression ACAR is a maximum, and Q is then about 5 per cent more than when the chunnel is flowing full

## SECTION III - RELATIVE VELOCITIES IN CROSS SECTION

7 General Laws—Except near abrupt changes the water at every point of a cross section of a stream has its chief velocity parallel to the axis of the stream and in the direction of flow, and the velocity varies gradually from point to point. Although the velocity at any point in a cross section is affected to some extent by its distance from every part of the border, it depends

chiefly on its distance from that part of the border which is near to it. Those portions of the border which are remote from the point have a small, often an inappreciable effect. In



Fig 108,

Fig. 108 the velocity at A is less than at B because of the effect of the neighbouring side. At all points between C and D the

velocities are nearly equal because both sides are remote Given the cross section of a stream, the forms of the velocity curves are known in a general way but not with accuracy. In other words, their equations are not known

The law that the velocity is greatest at points furthest from the border is subject to one important exception. The maximum velocity in any vertical plane parallel to the axis of the stream is generally at a point somewhat below the surface and not at the surface. If D is the depth of water and  $D_{\rm st}$  the depth of the

point of maximum velocity, the ratio  $\frac{D_m}{D}$  in a stream of shallow section at points not near the sides may have any value from zero to 30, and if the side slopes are not steep the same ratio may be maintained right across the channel. When the sides

are very steep or vertical the ruto  $\frac{D_D}{D}$  close to the side is about 50 or 60, and it decreases towards the centre of the stream, attaining its normal value in a shallow section at a distance from the side equal to about 2D or 25D, and thereafter remains constant or nearly so

The depression of the maximum velocity has been sometimes attributed to the resistance of the air, but this theory is now quite discredited. Air resistance could cause only a very minute depression, and it cannot account for the variation of the depression at different parts of a cross section. It is true that wind acting on waves and ripples may produce some effect. The water level in the Red Sea at Suez is raised during certain seasons of the year when the wind blows steadily up the Red Sea. On the Mississippi, with depths ranging from 45 to 110 feet, an upstream wind was found to reduce the surface velocity and

unstream wind was found to reduce the surface velocity and increase the ratio  $\frac{D_m}{\mathcal{D}}$ . A downstream wind produced opposite effects, but even with a downstream wind the maximum velocity was below the surface, and the same thing has been observed elsewhere. Wind acting on ripples is a different thing to simple air resistance. The depression is attributed by Thomson to the eddles which rise from the bed to the surface. The water of which the eddies are composed is slow moving, and though the eddies retard the velocity at all points which they traverse, they have most effect at the surface, because they spread out and recumulate there. This explanation seems to be the true one at least as regards the central portions of a stream. When no

depression exists there, it is because the eddies are weak relatively to the other factors The increased depression of the maximum velocity near the sides when these are steep or vertical is clearly connected with certain currents which circulate transversely in a stream Near the side there is an upward current (Fig. 108), at least in the upper portion of the section, and there is a surface current from the side outwards It is this current which causes floating matter to accumulate in mid stream At a lower level there must be an inward current which brings quick moving water towards the sides, while the slow moving water near the surface travels outwards and reduces the surface velocity at all points which it reaches

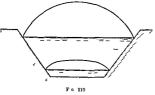
As to the cause of the currents, Stearns, who has investigated the subject.1 considers that they are due to eddies produced at the sides The eddies from the side tend on the average to move at right angles to it, but they also tend

to move chiefly in the direction of the least resistance, that is, towards the surface

8 Horizontal Velocity Curves -A horizontal 'mean velocity curve' is one whose ordinates are the mean velocities on different verticals extending from surface to bed The general forms of these curves for a rectangular section are shown in Fig 109 for two water When the section is shallow



the velocities on different verticals, at a distance from the side



exceeding 2D or 3D, become near ly equal shows channel with sloving sides The length in which the velo city is practically constant is some what greater than before, and

the curves in this portion are nearly as before, but the part in

<sup>1</sup> Transactions of the American Society of Civil Engineers, vol XIL

which the velocity varies is longer, both actually and relatively to the whole width If the bed is not level across (Fig 105, p 159) the velocity is greater where the depth is greater. If there are, at a distance from the sides, divisions of considerable width and constant depth, as HG and BK, the velocity in each such division is nearly constant. The rough rule for a channel of shallon section considered as a whole, that V is approximately as D3 where D is the mean depth, probably applies to any two divisions such as those under consideration and to the same division for different water levels But if a division is of small width its velocity is affected by those adjoining it Thus the velocity curve is one which tones down the irregularities of the bed On the South American rivers with depths of 9 to 73 feet, gradually increasing from the bank to the centre of the stream, Rovy found the velocity to vary as Dn where n is greater than unity. This may he the law in very deep rivers, but Revy's observations were not numerous, and in most of them the flow was unsteady owing to tidal influences Where the change of depth is small the variation of Di is not very different from that of D The form of the velocity curves in a channel of irregular sections changes, as it does in regular channels, with the water level Irregularities which have a marked effect at low water may have no perceptible effect at high water

The reture of the horizontal mean velocity curve depends on the shape of the cross section, and not on its size. From observations made by Bazin on small artificial channels lined with plaster, plank, or gravel, with widths of about 65 feet, and depths up to 15 feet, and observations made by Cunningham on the Ganges Canal in an earthen channel about 170 feet wide and 5 feet deep, and in a masonry channel 85 feet wide, with depths of 2 feet to 35 feet, it is also proved that if the velocity is altered by altering the surface slope (and in the case of Bazin's channels by altering the roughness), the velocities on different verticals all alter mabout the same proportion. It is probable, considering the complications arising from eddies and trunsverse currents, that the actual size of the channel has some effect, but it is negligible, at least in streams of shallow section, and under the conditions which occur in practice

Let U be the mean velocity on the central vertical, and I that in the whole cross section Let  $\frac{I}{I'} = a$ . The values of the co-

efficient a are as follows -

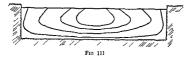
These co efficients are applicable to rectangular and trapezoidal channels, but may not be very accurate for the latter when the ratio of the mean width to the depth is small, especially if the side slopes are flat. In other cases they are probably correct to within 1 or 2 per cent for the deeper sections, and to within 5 per cent for shallower sections. The co-efficients have been found chiefly from the observations above mentioned. Bazin did not work out this particular co-efficient, but his figures enable it to be found. In any particular channel, the co-efficient increases as the water level falls.

The co-efficient a was determined in the observations on the Solani aqueduct in the Roorkee experiments. In the aqueduct there is a central wall which divides the canal into two channels, each 85 feet wide. The aqueduct is 932 feet long, and the observations were made in the middle, that is, only 466 feet from the upper end. Upstream of the aqueduct the canal consists of one undivided channel, and the greatest velocities are in the centre. Owing to this fact the inviminm velocities at the observation sites in the aqueduct at times of high supply are not in the centres of the channels, but nearer the central wall. The velocities observed to determine a were, however, made in the centres of the channels, and the resulting values of a were therefore too high. The depth varied from 4 to 10 feet, and the ratio of width to depth therefore from 21 to 85. The values of a were nearly constant at 95.0 9.6 For the lower depths the co-efficient agrees with that in the above table. For the higher depths it was overestimated for the reason just given. (See chap ii art. 21). The co-efficients are strictly applicable only when the bed, as

The coefficients are strictly applicable only when the bed, as seen in cross section, is a straight and horizontal line, but practically they are applicable whenever the central depth is the mean depth (not counting the sections over the side slopes), and does not differ much from the others. If there is a shallow in the centre the co-efficient may exceed 10, and may increase greatly at low water. For some particular sections somewhat hollow in the centre the co-efficient may not vary as the water level changes. The above refers to horizontal mean velocity curves. The

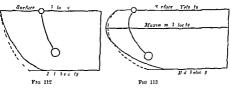
The above refers to horizontal mean velocity curves The properties of horizontal curves at particular levels, for instance at the surface, mid-depth, or bed, are, generally speaking, similar to the above In the central portions of the stream the curves are

probably all parallel projections of one another. Near to vertical or very steep sides, owing to the greater depression of the line of maximum velocity, the mid depth velocity curve, and to some extent the bed velocity curve, become more protuberant and the surface curve less so. Fig. 111 shows the distribution of velocities



found by Bazin in a channel 6 feet wide and 1 5 feet deep, lined with coarse gravel Each line passes through points where the velocities are equal

9 Vertical Velocity Curves —The general forms of the curves are shown in Figs 112 and 113 1 Many attempts have been made



to find the equations to the curves and it is sometimes said that the curve is a parabola with a horizontal axis corresponding to the line of maximum velocity. This is improbable. The transverse curve is certainly not a parabola. The bed of a channel retards the flow in the same manner as the side retards it and the velocity probably decreases very rapidly close to the led just as it does close to a vertical or steep bank. Except near the led almost any geometric curve can be made to fit the velocity curve. The equation to the curve is not nearly of so much practical importance as the ratios of the different velocities to one another. If these are known, the observation of surface velocities and less the led velocities and mean velocities to be recertained. A slight difference in the ratios may make a great difference in the equation. I can the information regarding the ratios is very imperfect, and

The floats and dotted lines are referre I to in clap sit

until it is improved it is useless to discuss the equation. When the depths on adjoining verticals are not equal, the curves are probably of a highly complex nature, since each must influence those near it.

Let U, Um, U, and U, be the surface, maximum, mean and bed velocities on any vertical not near a steep side of a channel, then the ratios which are of most practical importance are those of Dm to D, and of U to each of the other velocities The results as to these ratios furnished by experiments show great discrepancies The fact seems to be that the ratios are easily disturbed A change in depth, roughness, or surface slope may cause the eddies to rise in greater or less proportion, and so alter the ratios The quantity of silt or drift perhaps affects them, since some of the work of the eddies is expended in lifting or moving the materials Wind may affect the surface velocities and un steadiness in the flow may affect the ratios The depth Dm is seldom accurately observed This is because the velocities above and below the line of Um differ very slightly from Um, and also because the velocities are not generally observed at close intervals A greater defect is in the observation of bed velocities They are seldom observed really close to the bed When so observed a rapid decrease of velocity has been noticed

Generally the different ratios roughly follow one another When the eddies reach the surface in greater proportion the ratio

 $\frac{D_m}{D}$  increases At the same time  $U_m$  is diminished and  $U_*$  is increased, because more quickly moving water takes the place of that which rises. Thus the different velocities tend to become equal and the ratios to approach unity  $\frac{D_m}{D}$  and  $\frac{U}{U_*}$ . On examin

mg the results of experiments no clear connection between these ratios and the quantities U and D is apparent, but by considering the two separate elements on which, for any given depth, U depends, namely N and S, some more definite, though not very satisfactory results are obtained. The following table contains in abstract of the results of some of the chief observations. Each group consists generally of several series, each series having a separate value of D and U, and sometimes of N or S. The table is a mere abstract, and is intended to show only what experiments have been considered and their general results. On the Mississippi and Irrawaddy and Ganges Canal the observations were made with

# Abstract of Results of Observations on Verticals not near the Sides of the Channels

Serial \umber	Channel	Observer	Depti Velo	Rough	ness and ertical	R	atios
Senal			D	N	v	D n	$\frac{L}{L_n}$
		Division I —	GREAT	RIVE	ers		
1	Mississippi	Humphreys and Abbott	76	027	35	38	98
2	,,	1	79	027	21	13	94
3	"	"	65	031	53	27	97
4	1 ::	! "	27	025	47	28	97
4 5 6	Irrawaddy	Gordon	50	*-*	5 4	03	95
ñ	, ,		29	i .	18	zero	93
7	Parana de las	Revy	50		24	zero	83
١.,	Palmas	100.3	00	1		2010	"
8	La Plata	,,	24	ı	13	zero	69
	Div	ision IIOr	DINAR	y Str	FAUS		
9	Saone	Leveille	14	028	1 2 2	15	1 90
10	Garonne	Baumgarten	11	0275	50	10	90
11	Seine	Emmery	9	026	25	05	89
12	Rhine	International	7	030	71	zero	80
1	Kinne	Commission	١ ′	000	١,,	20.0	1 00 1
13	Branch of Rhine		5	0275	3.5	zero	87
14	Ganges Canal	Cunningham	9	025	35	12	98
15	ounges Cultur	Ounmeduam	6.5	013	4.2	19	93
	Dı	vision III —	SMALL	STRF	MS		
16	Artificial Channels	Bazin	13	020	59	05	84
17	**	,, !	11	015	66	zero	89
18		,,	1	012	65	zero	91
19			9	010	91	zero	92

the double float, and the ratio  $\frac{U}{U_m}$  was thus seriously vitinted (chap

one art 9), the values of U obtained being too high. On the Ganges Canal U was, however, observed separately by means of rod floats, and by making certain corrections for the length of rod used, corrected values of U have been found and used. In Revy's observations the flow was unsteady

By considering the figures of each separate series in Javisions

n and ni it is quite clear that the ratio  $\frac{U}{U_m}$  increases as N decreases. This result had projously been found by Bazin for his small channels. It also seems probable that the ratio generally increases with the depth. In division 1 the figures are unreliable, as above explained, but to some extent they confirm the above laws. From a consideration of the various results the following table has been prepared, but the figures given are only probable and approximate. The only law that seems to be well established is that of change of the ratio with change of N, the rest being somewhat doubtful. The figures are, however, an advance on the present rough rule that the ratio is '85 to 90' The blanks in the table may be filled in according to judgment.

The ratio  $\frac{U}{U_s}$  may be designated eta

Probable Ratios of Mean to Surface Velocities  $\begin{pmatrix} \beta \text{ of } U \\ U \end{pmatrix}$  on Verticals not near the Sides of a Channel.

and rough channels the ratio has been found to be as low as 60

Depth on		Values of A									
Vertical.	030	10° 5	00.00	*0**25	-0^0	-01 5	015	013	01		
Feet				_							
чO	1 1	1 1			83	86	٥8	89	91		
1 10	1			l i	84	87	89	90	91		
1.25	1				85	87	89	-91	91		
1 50	1	}			87	88	90	91	9:		
2 00	1 .	1 8	87								
3 00	1 1	1 1	88			1	- 1	·			
5.0	85	87	89			1 1	1	93			
70			90			1		- 1			
100	86	l so l	90				1	-92			
13.0	*-	91	89				- 1				
18 0	89	92	88	'	89	١ '	90 .	-91			
23.0	1 00	93	-50	1 '	, ,,	1					
28 0	1	95		1		l j					

After the preparation of the above table for depths up to 18 feet the author's attention was drawn to an extensive and careful series of observations made with current-meters by Marr on the Mississippi. The results worked up and abstracted are as follows—

<sup>1</sup> Report on Current meter Observations in the Mississippi near Burlington

### Abstract of Results of Observations on Verticals not near the Sides of the Channels

\umber roup	Cl annel	Observer	Deptl Velo	Rough n	Ratios		
Serial \umb	Granner	Ouserver	D	N	ı	$\frac{D_n}{D}$	$\frac{1}{t_m}$
ļ ļ		Division I —	FREAT	Rive	RS		
1	Mississibbi	Humphreys and Abbott	76	027	3 5	38	98
2	,,	۱ "	79	027	21	13	94
3	,,	,,	65	031	53	27	97
5	,,	,,	27	025	47	28	97
5	Irrawaddy	Gordon	50		54	03	95
6 (	,,	,,	29		18	zero	93
7	Parana de las Palmas	Revy	50		24	Zero	83
8	La Plata	_ ,,	24		13	zero	69

### DIVISION II -ORDINARY STPEAMS

I	g	Saone	Leveille	14	028	22	15	90
	10	Garonne	Baumgarten	11	0275	50	10	90
	11	Seine	Lmmery	9	026	25	0.5	89
	12	Rhine	International	7	030	71	zero	85
		(	Commission	[ ]				
	13	Branch of Rhine	Defontaine	5	0275	3.5	zero	57
	14	Ganges Canal	Cunningham	9	025	35	12	45
١	15			6.5	013	42	19	93

### DIVISION III -SMALL STREAMS

i							
16	Artificial Channels	Bazın	1 3	020	59	05	54
17 18	,,	,,	11	015 012	66	zero	S9 91
10	,,	"	Îg	010	ğΪ	zero	92

the double float, and the ratio  $U_{\rm ps}$  was thus seriously vitrated (chap  $U_{\rm ps}$ 

viii art 9), the values of U obtained being too high. On the Ganges Canal U was, however, observed separately by means of rod floats, and by making certain corrections for the length of rod used, corrected values of U have been found and used. In Prevs observations the flow was unsteady

By considering the figures of each separate series in livisions

11 and 111 it is quite clear that the ratio  $\frac{U}{U_n}$  increases as N decreases. This result had previously been found by Barin for his small channels. It also seems probable that the ratio generally increases with the depth. In division 1 the figures are unreliable, as above explained, but to some extent they confirm the above laws. From a consideration of the various results the following table has been prepared, but the figures given are only probable and approximate. The only law that seems to be well established is that of change of the ratio with change of N, the rest being somewhat doubtful. The figures are, however, an advance on the present rough rule that the ratio is '85 to 90'. The blanks in the table may be filled in according to judgment. In some small and rough channels the ratio has been found to be as low as 60. The ratio  $\frac{U}{II}$  may be designated  $\beta$ 

Probable Ratios of Mean to Suppace Velocities  $\left(\beta$  or  $U \atop U \atop V \right)$  on Verticals not near the Sides of a Channel

Depth on				1.	lues of	۸	_		
VerticaL	030	-0~5	-0~0	10725	-0^0	-01-5	015	013	-010
Feet. 90 1 10 1 25 1 50 2 00 3 00			87 88		83 84 85 87	86 87 87 88	88 89 89 90	\$9 90 91 91	91 91 91 92
5-0 7 0 10 0 13 0 18 0 23 0 28 0	86 89	87 91 92 93 95	89 90 90 89 88		89		90	93 92 91	

After the preparation of the above table for depths up to 18 feet the author's attention was drawn to an extensive and careful series of observations made with current-meters by Marr on the Mississippi 1 The results, worked up and abstracted, are as follows—

<sup>1</sup> Report on Current meter Observations in the Mississippi near Burlington

ABSTRACT OF RESULTS OF ODSERVATIONS ON VERTICALS

NOT NEAR THE SIDES OF THE CHANNELS

Ser al Number	Cl annel	Observer	Deptl Velo	Rought Cty on V	ess and ert cal	R	at os					
Ser al	G. daniel	CDScIVE!	D	N	t	D.	I I A					
	Division I —Great Rivers											
1	Mississippi	Humphreys and Abbott	76	027	3 5	38	J8					
2	,,		79	027	21	13	04					
3	1	"	65	031	53	27	97					
1 4	"	"	27	025	47	28	97					
l â	Irrawaddy	Gordon "	50	020	54	03	95					
3 4 5 6	111 a waddy	Gordon	29	1	18	,	93					
1 7	Parana de las	D.,"	50		24	zero	83					
1	Palmas	Revy	50		24	zero	} "					
8	La Plata	.,	24	<u> </u>	13	zero	69					
	Div	ision II —Or	DINAR	y Stri	EAMS							
9	Saone	Leveille	14	028	22	1 15	00					
10	Garonne	Baumgarten	11	0275	50	10	90					
11	Seine	Emmery	ĝ	026	25	05	89					
12	Rhine	International	7	030	71	zero	80					
( "		Commission	•				' i					
13	Branch of Rhine		5	0275	3.5	zero	87					
14	Ganges Canal	Cunningham	9 .	025	35	12	38					
15	,,	٠ ١	65	013	42	19	J3					
	·		لتت									
_	Dr	vision III —S	MALL	STRE	MS							
16	Artificial Channels	Bazin	13	020	59	05	84					
17	,,	,,	11	015	66	zero	89					
18	",		i l	012	6.5	zero	91					
iš.	] " ]	"	- g	010	91	zero	92					
	1 " f	"	- 1		/		- 1					
	' '.											

the double float, and the ratio  $\frac{U}{U_m}$  was thus seriously vitrated (chap viii art 9), the values of U obtained being too high. On the Ganges Canal U was, however, observed separately by means of rod floats, and by making certain corrections for the length of rod used, corrected values of U have been found and used. In Revy's observations the flow was unsteady

By considering the figures of each separate series in harmons

11 and 111 it is quite clear that the ratio  $\frac{U}{U}$  increases as N decreases. This result had previously been found by Bazin for his small channels. It also seems probable that the ratio generally increases with the depth. In division 1 the figures are unreliable, as above explained, but to some extent they confirm the above laws. From a consideration of the various results the following table has been prepared, but the figures given are only probable and approximate. The only law that seems to be well established is that of change of the ratio with change of N, the rest being somewhat doubtful. The figures are, however, an advance on the present rough rule that the ratio is  $^48$  to  $^{90}$ . The blanks in the table may be filled in according to judgment. In some small and rough channels the ratio has been found to be as low as  $^60$ . The ratio  $^{11}{IL}$  may be designated  $\beta$ 

Probable Ratios of Mean to Suppace Velocities ( $\beta$  of U) on Vepticals not near the Sides of a Channel.

Depth on	1	Values of A							
Vertical.	630	-0^-5	0.0	· 25	1070	-01-5	015	013	010
Feet,	1-	$\overline{}$	_	-					
90	1 :				83	86	86	89	91
1 10	1			l i	S4	87	89	90	91
1.25	1 !	!!			85	87	59	-91	91
1 00	1				87	88	90	91	92
2 00	1 1	i i	8-	i 1		i i		1	
3 00	!		88	lì					
5-0	8.5	87	89					93	
70	1		90			1		1	
100	86	89	90	1 1		) )		92	
13-0		91	89						
18 0	89	92	88		89	1	90	91	
23 0	1 "	93	1 1	1 1		ነ ነ		1	1
28 0	1	95	ì	1 '	1	l i		) 1	

After the preparation of the above table for depths up to 18 feet the author's attention was drawn to an extensive and careful series of observations made with current-meters by Marr on the Mississippi<sup>1</sup> The results, worked up and abstracted, are as follows—

<sup>1</sup> Report on Current meter Observations in the Mississippi, near Burlington

Depth=11 2	Feet 13 2	Feet. 20 4	Feet. 21 6	Feet. 27 6
V = 20	26	19	2 2	2 2
$U-U_{\bullet} = 89$	91	93	93	945
$D_m - D \approx 09$	09	26	21	-09

The values of N and S are not stated, but N is judged to have been about 0275, and the above table has been accordingly extended to depths of 28 feet. The velocities were not observed near enough to the bed to enable  $U_{\bullet}$  to be found

When the maximum velocity is at the surface the ratio  $U_{\infty}$  is the same as  $\frac{U}{U}$ . Otherwise it is 1 to 3 per cent lower

No law for the variation of  $\frac{D_m}{D}$  can be traced, except that in small streams the ratio is greater the rougher the channel. The ratio never exceeds 20 except on the Mississippi. On the Irrawadds, with not dissimilar depths and velocities, it is very small or zero. The difference may possibly be due to differences in N and S. It appears that in very deep givers all the ratios are more sensitive.

The ratio  $\frac{U_*}{U_n}$  or  $\frac{U_*}{U_*}$  generally follows the ratio  $\frac{L}{U_n}$ . In the detailed series of division in of the table on page 168 both ratios attain maximum and minimum values together. Values ranging from 58 to 63 have been found for the ratio on the lower Rhine, Meuse, Oder, Worth, and Messel. It is probable that in nearly all experiments the ratios found are too high lecause the velocities are hardly ever observed close to the led and also because of the rapid decrease of velocity near the led on the Slone the current-meter was placed as near to the led as possible, and the ratio comes out very low. The following table shows such probable values of this ratio as it has been possible to arrive at ...

``	60 6-3	+0=3	0.0	7015	1010
Depth=	Fert. 5 to 18		Feet. 1 to 1 5	l to I	1772
l,l.	50 to 3		50 to "	10	C5

When the various ratios are known the vertical velocity curve

can be drawn. The curves are, of course, sharper the less the depth of water. The depth at which the velocity is equal to the mean velocity on the vertical varies somewhat, being generally deeper as  $D_n$  is deeper. It has been found to vary from 55D to 67D. On the average it is at about 60D or 625D. The middepth velocity is greater than the mean, but generally by only 1 or 2 per cent. On the Mississippi it was found to remain constant while U was constant, even though U, was increased or decreased by wind, a compensating change occurring near the bed. The mean velocity can be found approximately by an observation at 50 or 625 of the full depth. It can be found very nearly, as has been shown by Cunningham, by observing the velocities at 21 and 79 of the full depth and taking the mean of the two

10 Central Surface Velocity Co-efficients - Sometimes the mean velocity I' in a cross section is inferred from an observation in the centre of a stream. If U is the velocity on the central vertical V=aU Sometimes  $U_a$  the central surface velocity, is observed and multiplied by a co efficient δ It is clear that δ must be ax B It has been seen that a depends on the shape of the section, and is practically independent of the size, roughness, and slope, while B. at least in streams of shallow section, seems to depend on these three factors. In a given stream of shallow section and fairly level bed a decreases as D increases, but  $\beta$ increases Hence & does not in ordinary cases show any very great fluctuation On the Ganges Canal, with earthen channels 190 to 60 feet wide, and masonry channels 85 feet wide, and with depths of water from 2 to 11 feet, 8 varied from 84 to 89 Neither a nor B varied much With widths of 10 to 20 feet, and depths of 1 to 3 feet, a was somewhat reduced, and & was also less, its values being 81 to 85 At one site, where there was a shallow in the middle, a rose at low water to 1 07 and 8 to 95 Ordinarily 81s seldom below 80

Bazin found for small channels the values of a coefficient  $\Delta$ , giving the ratio of  $U_n$  to V. Its values do not differ very much from those of  $\delta$ . Bazin, however, assumed that  $\Delta$  depended only on N and R, and on this assumption he worked out values of the coefficient for values of R, extending up to 20 feet or far beyond the limits of his experiments. It has been the custom to use these coefficients as values of  $\delta$ , that is, to use them for obtaining V from  $U_v$ . This in itself would not cause any very large error, but the values of the coefficients, when applied to channels of slopes, sizes, and roughnesses, differing greatly from those used by Bazin,

are entirely wrong Neither  $\delta$  nor  $\Delta$  can depend only on R and N, but must depend on the values of  $\alpha$  and  $\beta$ 

Other general expressions for  $\delta$  have been proposed by Prony and others, but they, in common with those of Bazin, are almost useless as general formulæ

# SECTION IV -CO EFFICIENTS

11 Bazın's and Kutters Co efficients - Setting aside obsolete and discarded figures, the first important set of co efficients for open channels is that obtained by Darcy and Bazin from experi ments on artificial channels, whose width did not exceed 6 56 feet in masonry and wood and 21 feet in earth Bazin from these experiments, framed tables of C (connecting them by an empirical formula and extending them far outside the range of the experi ments) for four classes of channel, namely, earth, rubble musonry, ashlar or brickwork, and smooth cemented surfaces It has been found that these co efficients, though correct enough for small channels, often fail for others More recently two Swiss engineers, Ganguillet and Kutter, went thoroughly into the subject, and after investigating the results of the principal observations, and making some themselves, arrived at various sets of co-efficients for channels of different degrees of roughness, the roughness being defined by a 'rugosity co efficient' N The following statement shows some selected values of Bazin's and Lutter's co efficients The last three columns will be referred to below -

	c	Baz n s o-ettic ents		Kutter Channe	Autter's Co efficients for Channels I aving a Slope of I in 5000			Barin 4 New Co efficients.		
Ily dra lic Radius (I)	Cement etc	Rubble Masonry	Earth	Cement Plaster etc	Farthen Chan els in Good Order	Earti en Channel in Bad Order	Ce nent	Ileg lar Cl annels.	Very Ro ! Cha nels	
				1 = 1010	λ = ·0°0	\= <b>1030</b>	y= 109	y=2 01	y 31	
5 10 20 40 60 100	135 141 144 146 147 147	72 87 99 106 110 112	36 48 62 76 84 91	132 152 170 185 193 201	57 69 82 94 101 105	35 43 53 63 69 76	136 142 146 140 151 152	50 50 77 89 97	31 49 61 69 7J	

It will be seen that C always increases with L and that the increase is less rapid as L becomes greater, and that as I increases

C becomes less affected by the degree of roughness Also that, with change of R, Kutter's coefficient varies more than Bazin's for smooth channels, and less than Bazin's for rough channels

Bazin's co efficients are independent of S, but Kutter's depend to some extent on S, as will appear from the following statement —

Value of P	Kutter's Co efficients for different Slopes										
	N-	-010	A.	= -030							
	Slope 1 in 10 000	Slope 1 in 1000 and Steeper Slopes	Slope 1 in 10 000	Slope 1 in 1000 and Steeper Slopes.							
	126	138	33	36							
10	148	156	42	45							
20	168	172	52	54							
40	186	185	64	63							
6.0	195	191	70	68							
10 0	206	197	78	74							

When R is about 3.2 C is independent of S. It increases or decreases with S according as R is below or above 3.2, but varies only slightly for a great change of S, the variation being greatest when S is between 1 in 2500 and 1 in 5000. For slopes steeper than 1 in 1000 the variation is negligible. For all values of N the variation of C with S is very similar in relative amount.

Kutter's co efficients for flat slopes are based on the Vississippi observations of Humphreys and Abbott The fall here was so small (sometimes 02 foot per mile) that the deduced slopes are absolutely unreliable This is the opinion of Bazin and also of Smith There is really no proper evidence that C increases as S decreases Bazin, who has recently reviewed the whole question and considered all the best known experiments, has arrived at a new set of co efficients, some of whose general values are given in the last three columns of the first of the above tables As before he makes C independent of S, and his different sets of co-efficients correspond to certain values of y which is analogous to Kutter's A' The rate at which C varies with change of L conforms more nearly than before to that of hutters co-efficients Buzin in his discussion includes some results which are known to be wrong, such as those obtained on the Irrawaddy (art. 9) and in the Soluni aqueduct, Ganges Canal (chap. vii art. 5), but the rejection of these would not al preciably alter his foures.

The experimental values of  $\mathcal C$  when plotted form a mass of irregularly placed dots and Bazni's co-efficients seem to suit them as well as Kutter's, while the law of their variation is more simple. It has, however, been seen that for pipes  $\mathcal C$  undoubtedly increases with  $\mathcal S$ , and it is unlikely that a different law holds good for small open channels. It is quite likely that  $\mathcal C$  always increases with  $\mathcal S$ , but that for large values of  $\mathcal R$  the increase is negligible

Engineers have now become familiar with Kutter's values of N, and it is desirable to continue their use. It is possible to expund Bazin's new sets of co efficients so as to give values corresponding to all Kutter's values of N, but it seems undesirable to do this, having regard to the doubt as to what the real law is Complete sets of both Kutter's and Bazin's co efficients are given in tables xxix to xhi

The empirical formulæ connecting the different values of the co efficients are as follows —

Bazin's original co efficients

$$C = \frac{1}{\sqrt{a(1+\frac{\beta}{R})}}$$

Kutter's co efficients

$$C = \frac{41.6 + \frac{1.811}{N} + \frac{00281}{S}}{\sqrt{R + N} \left(41.6 + \frac{00281}{S}\right)} \sqrt{R}$$

Bazin's new co efficients

$$C = \frac{157 \text{ G}}{1 + \sqrt{R}}$$

The quantities  $\alpha$ ,  $\beta$ , N and  $\gamma$  are all constants depending on the nature of the channel

12 Rugosity Co-efficients — The kinds of materials for which various values of N have been generally accepted are as follows Unless otherwise stuted all are supposed to be in good order. If in bad order the next higher value of N may be used, if extra smooth, the next lower

00) Timber planed and perfectly

continuous

Olo Timber planed Glazed and Cement an l

enamelic l plater
materials

Plaster and Pipes of iron, cement cement, or with one terra cotta. thurd of well joined sand and in best order

> New brick. work

012 Timber unplaned and perfectly con tipnous -013

-011

Unglazed stoneware and earth enware

Good brack

work and ashlar Rough faced

brickwork

Well-dressed

-015 Wooden frames covered with canvas Wood en troughs with battens inside, } in apart

017 Finegravelwell

tammed

cement

Coarse

imn. stonework Rubble in Tuberculated Brickwork. iron

Foul and

slightly tu

berculated

stonework and ashlar in

inferior con ditton

'020 Coarse gravel well rammed Wooden troughs with battens inside. 2 ins apart

rubble laid dry Rubble in inferior condition

For earthen channels the following are the general values -

Channels in very good order .017 ക്ക good order .. 0225 order above the average .. -025 average order 0275 order below the average .. 1030 bad order 4035 very bad order .,

A channel in very good order is free from irregularities, lumps, hollows, snags, or other obstructions, weeds and overhanging growth A channel having all the above irregularities (or even a few of them in excess) would be in very bid order. If a channel is choked by weeds, N may rise even higher than '035. The channels are all supposed to be free from bends In the l'unjah canals, when the channel has been worn very smooth and even, The experimental values of C when plotted form a mass of irregularly placed dots and Bazin's co-efficients seem to suit them as well as Kutters, while the law of their variation is more simple It has, however, been seen that for pipes C undoubtedly increases with S, and it is unlikely that a different law holds good for small open channels. It is quite likely that C always increases with S, but that for large values of R the increase is negligible

Engineers have now become familiar with Kutter's values of N and it is desirable to continue their use. It is possible to expand Bazin's new sets of co efficients so as to give values corresponding to all Kutter's values of N, but it seems undesirable to do this, having regard to the doubt as to what the real law is. Complete sets of both Kutter's and Bazin's co efficients are given in tables exix to this

The empirical formule connecting the different values of the co efficients are as follows —

Bazın's original co-efficients

$$C = \frac{1}{\sqrt{a\left(1 + \frac{\beta}{L}\right)}}$$

Kutter's co efficients

$$C = \frac{41.6 + \frac{1.811}{N} + \frac{00281}{S}}{\sqrt{R + N(41.6 + \frac{00281}{S})}} \sqrt{R}$$

Bazin's new co efficients

$$C = \frac{157 \text{ G}}{1 + \sqrt{\gamma}}$$

The quantities a,  $\beta$ , N and  $\gamma$  are all constants depending on the nature of the channel

12 Rugosity Co efficients—The kinds of materials for which various values of N have been generally accepted are as follows Unless otherwise stated all are supposed to be in good order. If in bad order the next higher value of N may be used, if extra smooth, the next lower

-009 Timber planed an l perfectly continuous

old Timber planed Glazed and Cement and enamelle | plaster materials

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	en ent	con il, ir
	with ra	terracetti,
	thir 1 of	w # 1 1 ft 1
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Lore with nechanicle the following are the general values.

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4117 Class late very profest t 67 14 weel aler 4027 alerales ti average RYSIBUS A ISS 111 11171 entertal without rays イバソト 1-11-11 10 \*\*\*\* 101 111

A claumel in very good or fer in free frees irres illenties I may a fellown, angre, or other elaten tien weels as I overlarging growth A channel laving all the above less danities for even a lewel them in excess, we dille in very 1 ferter. If a charrel last kelly weeks, he may rice even higher than tie. He changels are all any poor I to Infree free bereite. In the Lurish entals, when the chart I has been wern very or eth at bever,

N has sometimes been found to be as low as 016 There are of course channels requiring values of N intermediate to the above. and the proper value to be adopted, in any given case, is a matter of experience and judgment The deposits which occur in brick sewers increase the roughness somewhat The deposit of silt in an earthen channel frequently reduces the roughness

The kinds of channels corresponding to Bazin's y are as

follows -

109 Cement, planed wood

290 Planks, bricks, cut stone

833 Rubble masonry

1 54 Earth if very regular, stone revetments 2 35 Ordinary earth

3 17 Exceptionally rough (beds covered with boulders, sides with grass, etc )

13 Remarks -Besides the causes of discrepancies among the values of C mentioned in chapter is (arts 9 and 11) there are others. On the Mississippi and Irrawaddy V was obtained by the double float which gives erroneous results (chap viii art 9) The results of over a hundred discharges observed near the head of a large canal in India, when arranged into groups according to the depth of silt in the canal, show the average value of N to be 025 when there is little or no silt, but 013 when the depth of silt is from 5 foot unwards. Silt generally deposits in a wedge, the depth being greatest near the head of the canal It is therefore probable that the want of uniformity of the flow gale a some what enhanced value to C, and consequently too low a value to N This would, however, account only partially for the low value of N, and it is probable that its correct value is not more than 016 in the silted channel The above values are the average ones In individual discharges N varies enormously For one particular depth of silt it varies from 009 to 030 These varia tions may be accounted for partly by real variations in the rough ness of the channel, which often becomes very irregular when scouring is going on actively, partly by errors in the observations of the individual surface slopes and partly by variations in the degree of the variability of the flow

For two channels equal as regards roughness of surface and value of L, N is less when the profile of the section is semicircular or curved than when it is angular. In Ikirin's experiments on small channels C is 5 to 9 per cent less for a rectangular section, even though the depth was only 12 to ' of the width, than for a

semicircular channel The difference is probably due to the effect of the eddies produced at the sides (art 7) The co efficients in the tables may be taken to be for average sections, the section being neither a segment of a circle nor a rectangle (See also art 4)

For smooth channels of small hydraulic radius Kutter's co efficients give results which are too low | For iron or very smooth masonry conduits of diameters less than a foot, if N is taken to be 011. If comes out much too low For such cases Smith's or Fan ming's pipe co efficients should be used (See also chap v art 9) Similarly for brick sewers, if A' is taken to be 013, V is too low and Buzin's co-efficients may be used These facts point to the greater accuracy of Bazin's co-efficients for small and smooth channels

In earthen channels N seems to be particularly low when the ratio of width to depth is great. On the river Ravi at Sidhnai the value of N, deduced from a long series of observations, is often 008 or 010, and never very much higher The bed is often silted, but not always The flow is practically uniform, and the slope observations were checked with a view to discovering any error The river is straight, very regular, about 800 feet wide, and 6 feet to 10 feet deep. The case was specially investigated, and it seems to be proved that N at this site is not above 010 It is possible that the low value is due to the small effect of eddies from the sides, as compared with narrower streams and to the regularity of the flow Generally streams as wide as the Ravi are irregular 1

#### SECTION V -- MOVEMENT OF SOLIDS BY A STREAM

14 Formulæ and their Application -The observations made by Kennedy, and referred to in chap ii (art 22), were made in India on the Bari Doab Canal and its branches, the widths of the channels varying from 8 feet to 91 feet, and the depths of water from 2 3 feet to 7 3 feet The beds of these channels have, in the course of years adjusted themselves by silting or scouring, so that there is a state of permanent regime, each stream carrying its full charge of silt, and the charges in all being equal It was found that the relation between D and V in any channel was nearly given by the equation

 $V = 84D^{64}$ (71)

Put in a general form, this equation is  $V=cD^{-1}$ 

> 1 See also Appendix C 3.5

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The theory advanced in the paper quoted is that the silt supported per square foot of bed is P,D where P, is the charge of silt, and the force of the eddies as V2, so that P1D is as V If the solids consisted only of silt m would be 1, but there is also drift The silt discharge is BDVP,, or is as BV's The drift discharge is supposed to be as BV, and relatively small, and the total solid discharge is thus as a function of V, varying less rapidly than I's, say as Vn On the Burn Doab Canul n was 2 56 For, since De is as V. D is as V1 5, and BDVP as RPV256

Let V, be the bottom velocity and v the drift relocity If it be assumed that  $P_1D$  is as  $V_4^2$ —the ratio  $\frac{V_4}{V_1}$  increasing with  $V_4$ 

and D—the force of the current on the drift is  $(V_t-t)^2$ , and the friction of the drift on the channel as a, and that the depth of the drift may increase with P, then m may come out lower, say less than 1 for silt alone, or 1 for all solids The equation

 $I' = 1.05 D^{3}$ agrees nearly as closely as equation 67 with the observed results

All the above equations are partly empirical, and obviously apply only to cases in which the silt and drift bear some sort of proportion to each other. In theoretical equations of general application silt and drift would have to be considered separately If there is silt and no drift, equation 72 may be of the true form for all cases, m being probably 1 or less If there is drift and no silt, as in a clear stream rolling gravel or boulders, the moving force depends on Va, and D will be absent from the equation or will enter into it only in so far as the ratio  $\frac{P_s}{D}$  may depend on DRegarding equation 71 as a semi empirical worling equationand no more has been claimed for it-applicable to can'd systems and streams carrying silt and fine sand, its practical importance is very great. It is now known that in order to prevent, su, 1 deposit in any reach or branch, I must not be kept constant, lut be altered in the same manner as D. Whether it be altered as De or Di does not, for moderate changes, make very much differ The exact figures will in time le letter known designing a channel the proper relation of depth to velocity can he arranged for, or, at least, one quantity or the other kept in the ascendant according as scouring or silting is the evil to le guarde l against

The old idea was that an increase in I, even if accompanie ! ! v an increase in D, gave increased silt transporting power. In a stream of shallow section this is probably correct for I' mere ises as In

that is, as fast as required by equation 71, and faster than required by equation 73. In a stream of deep section a decrease in D gives increased sill-transporting power. If the discharge is fixed, a change in D or W must be met by a change of the opposite kind in the other quantity. In this case widening or narrowing the channel may be proper according to circumstances. In a deep section widening will decrease the depth of water, and may also increase the velocity, and it will thus give increased sociuming power. In a shellow section narrowing will increase the velocity more than it increases  $D^1$ . In a medium section it is a matter of exact calculation to find out whether widening or narrowing will improve matters

If the water entering a card has a higher silt-charge than can be carried in the canal some of it must deposit. Suppose an increased discharge to be run, and that this gives a higher silt-carrying power and a smaller rate of deposit per cubic foot of discharge, it does not follow that the deposit will be less because the quantity of silt entering the canal is now greater than before, Owing to want of knowledge regarding the proportions of silt and drift, and to want of exectness in the formule, reliable calculations regarding proportions deposited cannot be made

Assuming equation 71 to be correct, Kennedy has determined the following 'critical velocities,' or velocities below which silting will occur in channels supplied with turbid water, such as that of the Indian rivers, and has also published diagrams giving details D=1 2 3 4 5 6 7 8 9 10 V=94 1 30 1 70 2 04 2 35 2 64 2 92 3 18 3 43 3 67 15 Remarks—The channels in which the observations above

referred to were made have all, as stated, assumed nearly rect angular cross sections, the sides having become vertical (Fig. 114) by the deposit on them of finer silt, but the equations probably apply approximately to any channel if D is the mean depth from

side to side, and I' the mean velocity in the whole section

If the ratio of I' to Ir, say I' to I'', differs in different parts of a cross section, there is a tendency towards deposit in the parts where the ratio is least, or to seour where it is greater. There is of course, a tendency for the silt-charge to adjust itself to the circumstances of each part of the stream, that is to become less where the above ratio is less, but the irregular movements of the stream cause a transference of water transversely as well as vertically, and this tends to qualise the silt-charge. In a charred with not very steep side slopes the angles at V. A (Fig. 115)

frequently silt up-the velocity there being relatively low-and the sides become steep or vertical Sometimes, even when the sides are vertical, fine silt adheres to them, and the channel contracts, even though there may be no deposit in the bed the bed is level across there frequently occurs a shouling near the





sides, or a scour in the middle, and a marked rounding off at the lower angles The section thus tends to assume the form shown in Fig 116 When the bed is of sand, as in the Bari Doab Canal channels, it remains nearly level, because the sand at the sides rolls towards the centre

It is clearly impossible to answer, in a general manner, questions such as whether the embanking of a river, or confining it by training walls, will cause its bed to rise or to scour, whether silt will deposit on flooded land, whether the minor arm of a stream will tend to silt and become obliterated Everything depends on the charge of silt originally carried, on the hardness of the channels, and on the relations between D and I'

On some Indian canals the bed when the water is shut off, forms a suc cession of steps, each about 1 foot or less in height, and 20 to 30 feet aj art From one step to the next the bed slopes upwards This condition seems to occur when the material is sandy and scour is going on. The sand seems to I e rolled up the long slope, and to fall over the step

Some rivers in the northern hemisphere which flow in a southerly direct tion have a tendency to shift their clannels westwards. This is especially n ticeable in some of the Indian rivers. The revolution of the earth has been ascribed as a cause As the water approaches the e quator its velicity of rotation about the earth's axis increases. In latitude 30° a stream flow ing south at 2 miles an hour has its velocity of rotation increase I in one hour from about 1300 feet per second to 1300 37 feet per sec mil or ly 37 feet per second This is not a large amount in an hour, an I tle i ressure due to it must be a negligible quantity

#### Examples 1

Explanation -The explanation given under examples in Chapter applies also to open channels. If only one factor, say &, is fixed an infinite number of channels can be designed to carry a given discharge, but usually other factors are determined by practical considerations the ratio of the side slopes, sas, by the nature of the soil, and the ratio of H' to D, say, by the velocity

When these I xamples were worked out Bazin's new coleff cients 121 not come to notice They can be used in the same way as hutter s

desirable or the solid moving power required. If V must not fall below a certain minimum this can be arranged by keeping L large enough, or if this cannot be done, by altering S, N, or Q. If V is not to exceed a certain maximum R can be kept down, or S can be reduced to any extent by placing falls in the channel

Example 1 —Find the discharge of a stream with vertical sides and 15 ft wide when D=5.5 ft, N=017, and S=1 in 5225

From table xlin A=75 and  $\sqrt{R}=1.74$  From table xxxv  $C\sqrt{R}=183$  From table xxviii a slope of  $xd\pi\sigma$  gives V=2.59, and the percentage to be deducted is  $\frac{1}{10}c^{-2}=2.2$ , making V=2.53 Then  $Q=75\times2.53=189.8$  c ft per second

Example 2—Design a channel with side slopes 1 to 1 to dis charge 1000 c ft per second, S being the analysis of Successive trials, the bed width being 40 ft. It is clear that a depth of 7 13 ft gives the requisite discharge

	1st trial	nd trial.	3rd trial,
Bel width,	40	40	40
Depth,	7.5	7 25	70
A from table xlv	3563	342 6	329
/R from table xlv,	2 41	2 38	2 34
C √P from table xxxvii ,	216	212	208
from table xxviii	3 0ა	3 00	2 94
Q = AV	1087	1028	967

Example 3—In the preceding example let I' be limited to 2.5 ft per second. Find the minimum bed width

A must be 400 From table vxvii  $\ell$  /L is 176, and this in table vxvii gives  $\sqrt{R} = 2.08$  From table xlv a bed width of 80 ft and depth 4.75 ft gives practically the required values of A and  $\ell$ /P

Example 4—A channel 20 ft, wide with side slopes 4 to 1 and depth 5 ft has to discharge 240 c ft per second V being 025 Find S

From table aliv I=112.5 and I=1.90 Then  $I=\frac{-10}{11...5}=2.13$  ft per second Assume S to be  $\frac{1}{10.05}$  Then table xxviii gives  $C_1I_1=151$ , which corresponds in table xxxviii to I=2.0

Therefore S has been assumed too low Assume it to be  $_{1555}$  then  $C\sqrt{L}=142$  and  $_{1}/P=1$  92. To be exact  $_{1}/S$  must be

increased in the ratio  $\frac{192}{190}$ , or by 1 per cent nearly, that is,  $S = \frac{1}{1111}$ 

Example 5 — Keeping Q the same, alter D and S in the list case so as to give the necessary ratio of V to D to prevent silting according to the rules of art 14

The statement given below shows that if D is reduced to 3.25 ft S will be as before (1 in 4410), but W must be increased to 40 ft If W is left unaltered D can be 4.75, but S must be increased to about 1 in 3572. In a short channel, or one containing falls, it would be easiest to increase S, but otherwise it would be necessary to widen

Depth of water, 50 45 40 35 30 Velocity according to above rule, 235 220 201 187 170 Mean width of channel to make Q=240 c ft per second, Bed width of channel to nearest foot, Mr from table with , 187 185 179 173 161

 $\sqrt{R}$  from table viv., 187 185 179 173 164  $C\sqrt{L}$  from table vivin, 137 135 129 123 111 S (from table vivin) to give I' 3380 3764 4000 1320 4000 as above, 1 in

Example 6 —In a channel I is found to be i8 sq it,  $\sqrt{L}$  is 1 if it, Q is known to be 100 c ft per second, and S is  $_{110}^{1}$  G and N

V is  $^{10}_{18} = 208$  ft per second From table xxiII, if  $S = ^{1}_{000}$ ,  $C\sqrt{h} = 114$  An addition of 61 to 3000 decreases V by 1 per cent, an addition of 100 decreases V by 16 per cent, and  $C\sqrt{h}$  must be increased by 16 per cent, that is, it is 115.8 Hen  $C = \frac{115.8}{14} = 82.7$ , which (table xxxiI) corresponds very nearly to

λ = 020 Example 7 —In a channel with vertical sides, 70 ft wide and 5 ft deep, the central surface velocity is 3 ft per second, K' is 025 What is V'?

From the table on page 169  $\beta$  is 89. I rom the table on page 165  $\alpha$  is 915. Then  $V=3\times 59\times 915=2.72$  ft. per second

#### TABLES OF KUTTER'S AND BAZIN'S CO-EFFICIENTS

These are given to three figures, and the engineer who uses them will be fortunate if the actuals come out so as to agree with the third figure or even come near it. To add a fourth figure is useless, and it would render the tables bulky and less convenient. The values of C. The have been obtained from the four figure values of C, and the figures in excess of three struck off

As N increases the difference in C becomes less in proportion to the change in N. Hence it is not necessary to give C for N=0.395

TABLE XXIX.—KUTTER'S CO-EFFICIENTS (N= 009)

	TABLE A VIA.—KUTTER'S CO-EFFICIFVTS (N = 000)											
√r	I in	000	1 in 1	2 000	1 in 1	000	1 in	5 000	110	• 500	1 (n	1 000
	c	C√F	с	C√E	с	c√r	С	c <sub>v</sub> r	c	c.r	С	c, r
4	93 4		98 9	39 5		422		45 C	119	47 7	123	49 1
45	101	45 6	107	48	113	510		547	127	57	130	58 5
5	108	54 2	114	56 S		60 1		64 2		66 6		68 2
55	115	633	120	66 2		69 6		73 9		76 a		78 1
G	121	72 7	126	708		794		84	145	867		88 4
65	127	82 5	132	85 S		89 5		94-2		97	152	98 8,
7	133	92 7	137	95 1	143	100	150	105	154	108	136	109
S	142	114	147	117	152	122	158	126	162	129	164	131
9	151	136	1.55	140	160	144	165	149	168	15t	170	153
1	159	159	163	163	167	167	171	171	174	174	175	175
11	166	183	169	186	173	190	177	194	179	197	180	198
12	173	207	175	210	178	214	181	218	183	220	184	122
13	178	232	180	235	183	238	185	241	187	243	188	244
14	154	257	185	2ა9	187	262	189	265	190	267	191	267
15	188	283	190	285	191	287	193	289	193	290	194	291
16	193	309	194	310	19a	118	196	313	196	314	197	314
17	197	335	197	336	198	336	198	337	199	338	199	338
18	, 201	362	201	362	201	362	201	362	201	362	201	362
19	204	388	204	358	20°	387	203	386	203	386	203	386
2	208	415	207	414	206	413	20a	411	205	410	205	409
22	211	443	210	440	209	438	207	436	207	434	206	433
22	214	470	212	467	211	464	209	460	208	459	208	457
23	216	497	215	494	213	490	211	4Sə	210	483	209	481
24	219	525	217	520	215	516	213	510	211	507	211	506
2.5	221	553	219	547	217	541	214	535	213	532	212	529
26	293	581	221	574	218	568	215	э60	214	506	213	554
27	226	600	223	601	220	594	217	585	215	581	214	578
28	228	637	224	629	221	620	218	610	216	605	215	602
29	229	665	226	656	223	646	219	635	217	630	216	626
3	231	694	228	683	224	673	220	660	218	654	217	650
!	1	1	I	1			l			· i		

TABLE XXX --KUTTER'S CO EFFICIENTS (N= 01)

√r	1 m	000 00	1 111 1	15 OCO	1 in	10 000	1 in	5 000	1 in	2 500	1 is	1 000
_	С	C√F	c	C√R	c	c√r	c	C√R	c	C <sub>V</sub> R	c	C√R
4	81	32 4	85 7	34 3	91 4	36 6	99	39 6	104	41.	107	42 7
45	87 9	396	926	413	98.3	44 3	106	47 6	110	49 -		51 i
а	94 4	47 2	99 1	496	105	52 4	112	56	117	58 2		79 7
5ა	100	55 2	105	57 S	111	608	118	64 7	122	67	120	68 6
G	106	63 6	111	66 3	116	69 6		73 7	127	761		77 7
65	111	72 3	115	75 3	121	78 7	128	82 9	131	85 4	134	87
7	116	81 4		84 5	126	88	132	923	136	94 9	138	96 C
8	126	100	130	104	134	107	140	112	143	114	145	116
9	134	120	137	124	141	127	146	132	149	134	151	136
1	141	141	144	144	148	148	152	152	155	155	156	156
11	148	162	150	166	154	169	157	173	159	175	161	177
12	154	184	156	187	159	190	162	194	164	196	165	198
13	159	207	161	209	163	212	166	216	167	217	168	219
14	164	230	166	232	167	234	109	237	171	239	171	240
15	169	253	170	255	171	257	173		174	260	174	261
16	173	277	174	278	175	250	176		176	282	177	282
17	177	301	178	302	178	302	178		179	304	179	304
18	181	325	181	325	181	300 [	181			326	181 [	326
19	184	350	•						i		33	347
2	187	375					•				35	10.0
21	190	400					-				6	391
22	193	425							•		8	413
23		450 [										435
24		476										477
25	201	501										479 501
26				-		-				506	194	501
27							. '	r 30 1 1		2.44. 1	1741	1
28										-		. 1
29												

Terly XXXI -Kutter's Corfficients (N=011)

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	115	nno	1 (0)	5,000	i fa i	10.000	112	\$ 0.03	110	2,500	1 12	1 000
<b>,</b> /T	-	_	_					<u> </u>			_	
	١٢	C, 1	٢	C, I	С	CVT	r	CVT	c	CVT	c	CVT
			_		_	-				_	_	1
4	71.1	25.	753	371	50 3	32 1	57.1	34 4	913	36 .	261	37 C
45	77.4	31-	816	36 4	50 C	30	931	42	97 :	435	100	451
3	577	41 (	57 4	437	55.		99	49 %	103	1 51 -	106	32.5
-5	85 8	45 4	920	51.1	97.9		104	57 7	105	59 .	111	COS
-6 i	26	*64	94	55 5	103	617	100	654		1 177	] 115	69 1
65	25 2	612	103	664	105	(3 4	113	737	117	761	119	77.6
7	104	724	107	75 1	112	75.2	115	823	121	817	123	86-2,
**	112	82 :	115	923	120	757	125	99 4	125	102	130	104
-9	12+	105	123	110	127	114	131	118	134	120	136	122
1	126	126	120	123	133	121	137	137	139	ำาว	140	140
11	133	146	135	142	135	152	142	1.0	144	1.8	145	159
1-2	138	166	141	169	143	172	146	17.5	145	177	149	178
1-1	144	157	145	159	147	192	130	103	151	197	152	198
14	145	2)8	1.0	210	151	212	153	215	174	216	155	(217)
15	1.3	229	134	231	1-3	233	156	235	157	236	158	237
1.0	177	251	153 101	274	162	211	159	255	160	256	160	276
17	161	273	164	276	102	296	162	275 296	162	276	164	276
1.9	164		167	118	167	319	167	317	165	296	166	296   316
1-9	165	318	176	310	169	339	169	317	167 168	316	168	336
21	174	364	173	303	172	361	171	358	170	357	170	336
22	176	358	175	355	174	382	172	379	172	378	171	376
23	179	411	177	408	176	401	174	400	173	398	172	397
24	isi	435	170	431	178	426	176	421	175	419	174	417
23	154	459	182	454	179	448	177	442	176	439	175	437
2 G	186	483	183	477	181	471	178	464	177	460	176	458
27	158	507	185	500	183	193	180	485	178	481	177	478
28	190	531	187	523	184	515	181	506	179	502	178	498
23	101	551	188	547	185	537	182	528	180	522	179	519
3	193	580	190	570	187	560	183	549	181	543	180	539
			l	1								

# TABLE XXXII.—BAZIN'S AND KUTTER'S CO-EFFICIENTS.

[	Bazin	Kutter N= 012
√R	γ= 109	1 in 20,000   1 in 15,000   1 in 10,000   1 in 5,000   1 in 2,500   1 in 1,000
}	c  c/1	C CVR C CVR C CVR C CVR C CVR C CVI
	104 104	
4		1
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.6		İ
5 5 6 7 8 9		1
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13	. "	
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1.6	••	j i
18	:	
2		
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23	٠. ا	
25		
24 25 26 27		· ·
28	152 440	177 514 174 505 171 497 168 487 166 482 165 479
3	152 456 152 472	179 536 176 527 173 518 169 507 167 501 166 498
31	152 487	{
33	152   503     153   519	Bazin's co-efficients for higher values of $\sqrt{R}$ .
35	153 535 153 550	/R=50 70 80
3 G 3 7	153 566	C=154 155 155
38	153 592 153 598	}
4	153 614	



Table XXXIV —Kutter's Co-ffficients ( $N \approx 015$ )

√R	1 in 2	000	1 in 1	15 000	l in l	10 000	1 in	5 000	1 111	2 500	1 in	1 000
·	c	C~P	c	C√R	С	C√R	c	c√1	С	c√r	C	$c_{\checkmark}r$
4 5 6 7 8 9 1 1 1 1 2 1 3 1 4 1 5	46 8 55 5 63 4 70 4 77 1 83 1 85 6 93 6	38 49 3 61 7 74 8 88 6 103	49 4 58 3 66 1 73 79 4 85 4 90 6 95 5	29 2 39 7 51 2 63 7 70 8 90 6 105	69 4 76 2 82 5 88 1 93 1 97 7	21 1 30 8 41 7 53 4 66 79 3 93 1 107	96 1 100	82 4 96 1 110	60 68-9 76-4 82-8 88-6 93-6 97-9 102 105 109 111 114	45 9 58 70 9 84 2 97 9 112 126 141 156 171	78 3 84 6 90 1 94 9 99 1 103 106 109 112 114	24 8 35 4 47 9 59 2 72 1 85 4 99 1 113 127 142 157 172
16	114	182	115	183	115	184	116	185	116	186	117	187
17	117	199	118	200	118 120	201	118	201	119	202 217		202
19	123	234	123	234	123	233		233		233		232
20	126	2,2	126	251	125	250		249	124	248	124	248
21	120	270	128	260	127	267	126	265		254		263
22									27	2e0 [	127	279 [
23 24												
24			•					•				
25				•								
26 27							•	,				
28	, .									:		
28		421)	143)	•					:			
3	147	440	144	<del>1</del> - ۱	í	٠,	- 1	٠.,		٠,	٠,٠	١,



Table XXXVI.—Kutter's Co-efficients (N= 020)

111111111111111111111111111111111111111	1 1 1 2	1 1 1 1	1		Ľ	
		:	•	1   3	_ _	/n :
				32	С	l in :
				12 8	41	000
		Ξ.	•	s  33 G	c	1 m
				13 4	C√R	15,000
				35 7	c	1 m 1
				143	C√R	10,000
				38.7	c	1 18
			•	15 <u>5</u>	C√R	5,000
	:			40 6	c	1 in
				162	CVR	2,500
		٠.		41 9		1 in
				16.8	c√1	1,000

TABLE XXXVII.-BAZIN'S AND KUTTER'S CO-EFFICIENTS

	14	zin 1 54					kı	aller	N= 0	225				
4/E	7*	1 54	1 in	20 000	1 in	15,000	1 in	10 000	1 in	5,000	1 bi	570	1 in	1,000
_	с	CVI	c	C√E.	С	cvr	С	c√r	c	c√r	С	c√r	c	CVI.
·	ι	ı,	l —			Ι, .	[-		ι.	١			Ι.	
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TABLE XXXVIII, -BAZIN'S AND KUTTER'S CO EFFICIENTS

]	Ba	zin 23.,					I	Lutter	N=	02, 🗸				
√ <i>I</i> .	γ=	2 3.3	1 in	20,000	1 m	15,000	1 m	10,000	1 in	5,000	1 10	2,500	1 in	1 000
	С	C_1	ι	C√R	С	CVR	ι	C.VI.	c	C√R	ι	LVA	c	CVR
_						<b> </b>	-							_
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Bazin's co-efficients for higher values of  $R \begin{cases} \sqrt{R} = 4.5 & 5 & 6 & 7 & 8 \\ C = 103 & 107 & 113 & 118 & 122 \end{cases}$ 

Table XXXIX.—Kutter's Co efficients (N= 0275).

			_	_		_		_				
√E	1 in :	000	1 ln 1	5,000	1 in 1	10,000	l in	5,000	l in	2,500	1 in	1,000
	С	C√R	c	€√R	c	C√E	С	c√r	ι	cvi.	c	c√R
-4 56 -7 -8 9 1-1-1	21-2 25 6 29 8 33 8 37 5 41 44 4 47 5	8 5 12 8 17 9 23 7 36 9 44 4 52 2	22 2 26 7 30 9 34 9 38 6 42 1 45 3 48 4	8 9 13 3 18 5 24 5 30 9 37 9 45 3 53 2	23 4 28 32 3 36 3 39 9 43-2 46 5 49 4	9 4 14 19 4 25 4 31 9 46 5 51 4	25-2 29 9 34-2 38 1 41 7 45 48 50 8	10 1 15 20 5 26 7 33 4 40 5 48 55 9	26 4 31-2 35 5 39 3 42 8 46 49 51 7	10 5 15 6 21 3 27 5 34 3 41 4 49 56 8	27 2 32 36 3 40 2 43 6 46 8 49 6 52 3	10 9 16 21 8 28 1 34 9 42 1 49 6 57 5
	٠.						•					
1.8 1.9 1.2 2.3 4.5 2.6	65 6 67 8 69 8 71 7 73 6 75 4 77 8 80 4	118 129 140 151 162 174 185 197 209	65 G 67 G 69 5 71 3 73 I 74 8 76 3 77 3	118 128 136 150 161 172 183 195 206	63 G 67 5 69 2 70 9 72 4 73 9 70 4 70 7 77 7 78	118 128 138 149 159 170 181 192 203	65 7 3 65 8 70 3 71 6 72 9 74 2 4 76 5	118 128 138 148 158 158 178 188 199	67 7 67 2 68 9 69 9 71 1 72 4 73 6 74 6 75 6	118 128 137 147 157 167 177 187 197	6571 6555 6979 721 7311 759 7684 7791 7918 805	118 128 137 146 156 166 175 205 205 225 235 245 256 266 276
37 38 39 4	<u> </u>	!	!			· .			· .		81 8 92 3 82 9 83 4 84 84 5	286 296 307 317 328 338

TABLE XL -BAZIN'S AND KUTTER'S CO EITICIENTS.

	Ba.	nn					К	utter	N-0	30				
<b>√</b> T	η-	3 1-	1 m	20 000	'i in i	5,000	1 in 1	0 000	1 m	5 000	1 in	2 500	1 in	1 (
	c	C√1	С	c√r	с	C√R	c	C-/ L	C	c√1	c	c√r	С	c
4	17 9	716	19	76	19 8	79	20 9	8 4	22 4	g	23 5	94	24 2	Ī
4 5 6 7 8 9			i											
8														
111														
111111111111122222222223333333333333333														
15														
17														
2 2 1														
2 2 2 3		ĺ												
2 4		- 1												
27														
29		i												
3 1 3 2														
33		:												
36		:		•										
33		i												
4		i	1	- 1	1	1	1							

Bazm's co efficients for higher values of  $R\left\{ \begin{array}{lll} \sqrt{P=1.5} & 5 & 6 & 7 \\ C=92 & 97 & 103 & 108 & 118 \end{array} \right.$ 



### TABLE XLII -BAZIN'S OLD CO EFFICIENTS

These co efficients have been superseded by Bazin's New Co efficients, but are given here because they may be still considered suitable in some cases, or may be required for reference

					<del>-,</del>
P	Very Smooth Channels (Cement)	Smooth Channels (Ashlar or Brickwork)	Rough Channels (R ibble Masonry)	Very Rough Clannels (Earth)	Excessively Rough Channels (Encumbered with Detrit is
β	-0031G 1	00401 23	*00 0 82	*0059* 41	00845 S
25	125	9 <sub>2</sub>	57	26	18 5
2 2	135	110	72	36	25 6
75 (	139	116	81 /	42	30.8
1 1	141	119	87 J	48	34 9
15	143	122	94	56	41 2
25	144	124	98	62	46
25	140	126	101	67	53
3	145	126	104	70	53
35	146 146	127 128	10ə 106	73	58
4 4 5	146	128	100	76 78	93
5	146	128	107	80	62
5.5	146	129	103	82	0-
6 1	147	129	110	84	65
6.5	147	129	110	85	,
7 1	147	129	110	86	67
1 73	147	129	iii	87	
8	147	130	iii	88	69
80	147	130	112	89	
9	147	130	112	90	71
95	147	130	112	90	1
10	147	130	112	11	72
111	147	130	113	92	
12	147	130	113	93	74
13	147	130	113	94	
14	147	130	113 114	95 96	77
15	147 147	130	114	97	11
16	147	130	114	97	
1 17	147	130	114	98	
18 20	147	131	114	98	0
20	149	131	115	100	- 1
30	145	131	iii	102	83
140	148	131	116	103	85
50	148	131	116	104	86
Infinity	145	131	117	108	91
1		1	·		

#### TABLES OF SECTIONAL DATA

#### RECTANGULAR AND TRAPEZOIDAL SECTIONS

For a bed width intermediate to those given it is only necessary, in order to find A, to multiply D by the difference in width and add or subtract the Thus, for bed 43 ft , slope 1 to 1, and depth 3 75 ft , A = 175 8 -3 70 x 2=168 3 \( \sqrt{R} \) changes so slowly that the correct figure can be interpolated by inspection Widths outside the range

idth W and

depth D, look out  $\sqrt{R}$  for

by 2, or for

 $\frac{W}{\Omega}$  and  $\frac{D}{\Omega}$  and multiply by 3 Interpolations can also be made on this For instance, the figures for a bed of 125 feet can be found from those for a 50 feet bed

For side slopes of 4 to 3 and 3 to 4 -A and AR are the same respectively as for a rectangular section and a 4 to 1 section of the same mean width Thus for a channel of bed 21 feet, side slope 4 to 3, and depth 3 feet, the mean width is 25 feet, and A = 75, JR = 1.06 For a bed width of 11 feet, side slopes 3 to 4, and depth 4 feet, the mean width is 14 feet, which is the same as for a channel with bed 12 feet, side slopes 4 to 1, and depth 4 feet A=56 and  $\sqrt{R}=164$  These rul - - A+L

ratio or the sine slopes, and depends

## TABLE XLIII -- SECTIONAL DATA FOR OPEN CHANNELS

## Rectangular Sections

Depth	Bed 1	foot	Bed	2 feet	Bed 3	feet	Red	4 feet	Bed 5	feet.
of Water	A	√P	A	√r	A	√P	A	√r	٨	√R
Peet 575 1 25 575 25 575 25 575 4 25 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	575 1 95 1 75 1 75 2 95 2 95 2 95 2 95 3 95 3 95 3 95 3 95 3 95 3 95 3 95 3	5 53 58 6 61 62 63 64 65 65 76	1 15 2 25 35 45 55 65 75 8	56 66 71 74 78 8 82 83 84 86 87 87 87 88 89	1 5 22 3 75 4 5 2 4 5 2 4 5 2 10 5 5 11 2 12 75 13 5 5 15 15	61 71 77 73 87 9 93 97 99 1 1 01 1 02 1 03 1 04 1 05 1 07	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19	63 74 82 88 93 97 103 105 111 113 114 115 117 119	2 5 3 75 5 6 25 7 5 5 8 75 10 25 12 5 13 75 16 25 17 5 5 12 75 20 21 22 5 75 22 75 22 75	65 76 85 91 1 01 1 05 1 09 1 12 1 14 1 17 1 19 1 21 1 23 1 24 1 25 1 27

TABLE XLIII -Continued (Rectangular)

Depth	Bed (	6 feet	Bed	7 feet	Bet	1 & feet	Bed	10 feet	Bed	12 f et
Water	A	√P	A	√P	A	√R	A	√r	А	√r
5 2 5 5 5 5 75	3	65 78 97 94 1 105 1 1 13 1 117 1 12 1 23 1 23 1 13 1 13 1 13 1 13 1 13	3 5 25 5 25 5 25 5 25 5 25 5 25 5 25 5	66 79 98 98 96 96 113 11 17 121 127 13 13 13 13 14 14 14 14 14 14 14 14 14 14 14 14 14	4 6 6 8 10 12 14 16 16 18 20 22 14 26 30 32 44 45 48	67 8 8 8 8 8 8 1 1 4 1 1 1 15 1 2 1 1 2 1 1 3 1 1 3 1 1 3 1 1 3 1 1 4 1 1 4 1 1 4 1 1 4 1 1 4 1 1 1 4 1 1 1 4 1 1 1 4 1 1 1 4 1 1 1 1 1	7 5	1 71 1 73 1 73 1 74		6 5 5 9 9 9 1 1 1 1 1 1 2 1 2 2 1 3 7 1 4 1 4 5 1 1 2 2 1 5 7 1 1 6 1 1 6 7 1 1 6 7 1 1 6 7 1 1 7 1 7

TABLE ALIH -Continued (Rectangular)

Depth	Bed 1	fret.	Bed	lo fect	Bed 1	9 feet.	Be t	20 feet	Bed *	, feet.
Water	л	,T	A	√E	,	√P	A	√r	А	√r
Feder 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	105 5 14 17 1 1 1 1	6\22 94 140 140 112 118 112 118 114 114 114 115 116 117 117 117 118 118 118 118 118 118 118	8 12 16 2 14 17 2 2 3 4 4 4 4 12 5 6 6 6 5 7 2 5 5 5 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 12 16 2 16 16 16 16 16 16 16 16 16 16 16 16 16	60 83 41 144 127 133 143 143 143 143 143 143 143 143 143	9 13 5 14 15 14 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	1 97 1 9 1 92 1 94	10 15 25 30 35 340 45 55 50 50 55 65 70 55 70 50 95 95 95 95 100 110 1110 1120 1130 1140 1150 1150 1150 1150 1150 1150 115	69 95 147 114 129 147 129 147 129 147 129 147 129 147 147 147 149 149 149 149 149 149 149 149 149 149	12 7 8 8 2 7 31 3 3 3 3 4 3 8 6 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 3 7 6 6 8 8 7 5 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6 7	65 84 96 167 116 117 117 117 117 117 117 117 11

TABLE XLIII -Continued (Rectangular)

								en jace	,	
Depth of	Bed :	0 feet	Bed	3a feet	Bes	1 40 feet	. В	d 50 feet	Ве	d 60 feet
Water	Λ	√P	Λ	√r	А	√1	1	1/1	, A	3/1
7 25 7 5 7 75 8 25 8 25 8 75 9 25 9 25 9 75	30 30 60 67 75 5 90 75 105 112 112 112 112 113 113 113 113	2 37 2 39 2 41 2 43	375 5 5 70 78 8 87 5 3 105 8 87 5 3 105 113 8 122 7 5 166 3 114 8 114 7 5 114 8 114 7 5 114 8 114 7 5 114 8 114 7 5 114 8 114 8 114 7 5 114 8 11	97 1 188 1 34 1 1 48 1 54 1 1 6 1 166 1 166 1 171 1 175 1 175 2 18 2 21 2 21 2 22 2 23 2 24 2 24 2 25 2 25 2 25 2 25 2 25 2 25	80 90 100	11	8 75 100 2 112 1125 1 162 1 162 1 162 1 162 2 162	1 1 1 1 3 1 5 1 5 1 5 1 5 1 5 1 7 7 1 7 1 7 1 7 1	9 90 6 120 4 135 1 150 7 16 7 16 195 5 210 225 6 240 255 270 285 200	1 2 1 37 1 45 1 50 1 65 1 71

TABLE XLIII -Continued (Rectangular)

De <sub>1</sub> th	Bed "	0 feet.	Bed 8	0 feet	Bed 90	feet	Bed 1	00 feet	Bed 12	0 feet
Water	4	√r	4	√R	A	<b>√</b> P	A	√P	A	√ <i>I</i> .
Feet 1 5 25 5 5 7 5 5 5 7 5	70 105 140 157 5 175 210 227 5 245 262 5 280 297 5 315 332 5 367 5 385 402 5		80 120 160 180 220 240 250 280 300 320 340 360 420 440 460 480	VI	90 135 180 202 5 247 5 247 5 270 292 5 315 337 5 360 382 5 427 5 472 5 495 517 5		100 150 205 250 275 300 375 350 375 400 475 450 550 575 600	<b>V</b> 1	120 180 240 270 300 330 360 420 450 480 510 540 570 630 660 690 720	71.
6 25 6 5 75 6 5 77 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	437 5 455 490 5 507 5 525 542 5 560 577 5 630 647 5 663 682 5 700 805 840	:	500 520 540 560 620 640 660 720 740 750 800 840 880 920		562 5 585 5 630 5 675 675 675 720 742 5 765 787 5 810 832 5 877 5 900 945 990 1035 1050		625 650 675 700 725 750 825 850 825 850 925 950 1000 1150 1150 1200		750 780 810 840 870 900 930 1020 1050 1110 1140 11200 1200 1320 1350 1440	

TABLE XLIV —SECTIONAL DATA FOR OPEN CHANNELS

Trapezoidal Sections—Side slopes 1 to 1

Depth	Bed 1	foot	Bel	o feet	Bel	3 feet	Bed	4 feet	Bed	of et
of Water	A	√1	А	VI	t	√E	ı	1	1	V1
Feet 5	63	>4	1 13	GO	1 63	63	2 13	64	2 63	6
75	1 03	63	1 78	69	2 53	73	3 28	76	4 03	77
1	1 5	65	25	77	3 5	82	4.5	8,	55	87
1 25	2 03	73	3 28	83	4 ,3	ss	5 79	92	7 03	95
1.5	2 63	78	4 13	ss	563	94	7 13	95	8 63	1 02
1 75	3 28	52	5 03	92	6 78	99	8 53	1 04	10 25	1 05
2	í	86	6	96	8	1 03	10	1 09	12	1 13
2 25	4 78	89	7 03	1	9 28	1 07	11 53	1 13	13.75	1 17
25	5 63	45	8 13	1 03	10 63	111	13 13	1 17	1 63	1 21
27,	6 53	95	9 28	1 07	12 03	1 15	14 78	1 21	17 **	1 25
3	75	99	10 5	11	13.5	1 18	16 5	1 24	19 5	1 29
3 25	1	l	11 79	1 13	15 03	1-21	18 28	1 27	21 3	1 33
3 7	J		13 13	1 16	16 C3	1 24	20 13	1,30-	23 (3	1 36
3 75	[		14 53	1 18	18 28	1 27	22 03	1 33	25 78	13)
4	1		10	1 21	20	1 29	21	1 36	25	1 12
4 25	- 1		- 1	-	21 78	1 32	26 03	1 39	30.29	14"
45	ļ		l	- 1	23 63	13>	28 13	1 41	32 63	1 47
4 75	1	1	- 1	Į	2, -3	1 37	30 28	1 14	3.03	15
5	-	ļ		İ	27 3	1 39	32.5	1 16	17.5	1 2

TABLE XLIV -Continued (1 to 1)

Depth Bed 6 f		feet.	Bed 7	feet	Bed 8	feet.	Bed 9	feet.	Bed 10	feet.
Water	A	√r	A	√r	A	√r	1	<b>√</b> ₽	A	<b>√</b> r
11-170000000000000000000000000000000000	3 13 4 75 8 29 8 29 12 03 14 03 14 03 15 13 20 25 22 7 13 33 15 22 7 23 34 53 33 9 78 42 5 42 5 42 13 35 10 36 10	666 788 89 97 104 1121 1120 1120 1120 1120 1120 1120	3 63 5 5 5 3 7 5 5 9 5 5 3 16 2 5 5 6 3 13 7 8 16 2 5 2 9 6 3 2 2 5 5 6 3 2 2 5 6 6 3 2 5 6 6 6 7 8 6 6 7 8 6 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8 6 6 7 8	67 79 9 9 1 106 1 123 1 123 1 123 1 136 1 14 1 14 1 14 1 15 1 15 1 15 1 15 1 16 1 16 1 16 1 16	4 13 6 28 8 5 10 78 13 13 15 53 18 20 53 23 13 25 78 28 5 31 23 37 03 44 03 44 03 45 28 55 5 50 13 66 6	67 8 91 1 107 1 14 1 2 1 2 1 2 1 3 1 35 1 43 1 45 1 15 1 163 1 163 1 163 1 171 1 176	4 63 7 03 9 5 12 03 17 28 22 78 25 63 22 78 25 63 31 5 34 53 34 53 40 78 44 28 50 60 51 54 60 61 63 68 28 72	68 81 92 101 109 1128 133 138 142 146 154 154 166 169 172 174 177	5 13 28 10 5 13 19 03 25 13 15 13 28 25 13 15 13 19 03 25 13 15 13 17 18 16 15 15 15 15 15 15 15 15 15 15 15 15 15	68 81 1 93 1 102 1 1 1 23 1 29 1 1 48 1 1 20 1 1 77 1 8 2 1 1 77 1 8 1 8 2 1 1 7 1 1 9 1 1

Table XLIV -Continued (1 to 1)

						(_ '	,		
Depth Be	l 12 feet	Bed 1	l4 feet	Bed	16 feet	Bed	18 feet	Bed	"O feet
Water	√P	A	√P	A	Vr	1	1/1	A	1/3
Test 5 9 9 125 125 125 125 125 125 125 125 125 125	3	10 8 14 5 18 3 22 1 26	69 83 94 1 103 1 12 7 1 133 1 139 1 1 50 1 150 1 150 1 150 1 150 1 150 1 1 1 1		95 95 104 122 1 35 1 41 1 47 1 52 1 1 47 1 1 16 1 17 1 1 18 1 1 19 1 1 18 1 1 19 1 1 19 1 1 19 1 1 19 2 2 05 2 2 08 2 2 15 2 2 15	13 8 18 5 23 3 3 3 3 43 43 1 53 3 5 5 5 6 3 8 6 9 1	8 8 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	15 2 20 5 20 8 31 1 36 5 42 47 5 53 1	5 84 90 1 00 1 1.

TABLE XLIV -Continued (1 to 1)

Depth	Bel 25	feet.	Bel 31	fret.	Bed \$1	feet.	Bed 40	feet.	Bed 4	feet.
Water	A	√r	A	√r	A	√r	А	√r	A	î
유 그 이 하는 한 이 이 이 이 이 이 이 이 이 이 이 이 이 이 이 이 이 이	25 5 38 6 52 58 8 57 2 5 72 5 79 5 100 8 115 3 112 6 137 5 145 6 150 3	97 1173 114 1146 1152 1167 1174 1178 1195 1195 1196 1196 1196 1196 1196 1196	30 5 46 1 62 70 78 1 86 3 94 5 102 8 111 1 128 136 5 145 1 153 8 162 5 171 3 180 1	97 118 134 141 148 154 166 171 176 181 199 203 203	35 5 53 6 72 81 3 90 6 100 109 5 119 123 6 133 3 149 157 5 167 5 187 5 197 5 197 6	18 118 118 118 118 118 118 118 118 118	40 5 61 82 92 5 103 2 113 3 124 5 135 3 146 1 159 1 201 3 201 3 201 5 201 5 201 5 201 5	98 1 19 1 136 1 137 1 157 1 163 1 175 1 185 1 195 1 195 2 04 2 01 2 01 2 01 2 01 2 01 2 01 2 01 2 01	45 5 68 6 92 103 8 1156 5 151 5 151 5 153 6 157 5 158 200 3 212 6 225 250 6 257 5 3	98 119 136 144 151 178 167 176 182 196 201 206 21 218
6 - 25 - 6 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 -	169 175 8 183 6 191 6 199 5 207 5 215 6 223 8 232 240 3	2-09 9-12 9-15 9-19 9-23 9-23 9-25 9-27 9-33 9-36	199 207 216 1 225 3 234 5 243 8 253 1 262 5 272 291 5	2 14 2 17 2 24 2 27 2 33 2 36 2 37 2 38 2 38	238 3 248 6 259 1 269 5 280 290 6 301 3 312 322 8	2 17 2 21 2 24 2 28 2 31 2 34 2 37 2 4 2 43 2 46	258 269 5 281 1 292 8 304 5 316 3 328 1 340 3 )2 364	221 227 231 231 237 244 247 25 252	288 300 8 313 6 326 6 339 5 352 5 365 6 378 8 392 405 3 418 6	01010101010101010101010101010101010101
1 1 11			t	· :	i		500 5	2 55 2 58 2 61 2 63 2 66 2 69 2 74 2 78	432 1 445 0 439 1 472 6 486 3 500 527 6 550 5	2 59 64 67 67 7 7 1 8 3 8 3 8 3 8 3 8 3 8 3 8 3 8 3 8 3 8
11 5 12			Ì				526 1 552	2 83 2 87	583 6 612	2 87 2 92

TABLE XLIV .- Continued (1 to 1)

	<del></del>											
Depth	Bed	50 feet	Bed	60 feet	Bec	1 "0 fee	t	Bed	SO feet	Bec	I 90 fee	et
Water	A	√R	A	√R	A	1	'R	4	1	A	1	/1
Feet 1	51.5	98	60.5	5 99	70	5	99	80	5 99	90		99
15	76 1	1 19	91 1		100		21	121				ยย 21
2	102	1 37		1 38		1:	38	162	1 38	182		30
2 25 2 5	115	1 45					16	182				47
25	128 1 141 3	1 52			178 196		54	203 1				
2 75	154 5	1 65	184 5		214 8		7	244 5		252 :		52
3 25	167 8	171	200 3		232 8		4	265 3				13
3 5	181 1	1 77	216 1	1 78	251 1			28G 1		321 1	ílîs	31
3 75	194 5	1 83	232	1 84	269 5		6	307	1 86	344 5		
4	208	1 88	248	19	288	1 9		328	1 92	368		13
4 25 4 5	221 5 235 1	1 93	264 280 1	1 96	306 5 325 1			349 370 1	1 98	391 5 415 1		
4 75	248 8	2 03	296 3	2 05	343 8			391 3	2 08	438 8	20	
5	262 5	2 07	312 5	21	362 5			412 5	2 13	162 5		
5 25	276 3	2 12	328 8	2 15	381 3	21	6	433 8	2 18	486 3	21	9
5 5	290 1	2 16	345 1	2 18	400 1	2 1 2 2 2 2		455 1	2 22	510 1	2.2	
5 75	304	2 2 2 4	361 5	2 23 2 27	419			476 5 498	2 26 2 31	534	132	3
62	318 332	2 23	378 394 5	2 31	438 457	2 2	2	498 519 5	2 31	558 552	2 3	
65	346 1	2 33	411 1	2 35	476 1	2 3		541 l	2 39	606 I	24	
6 75	360 3	2 36	427 8	2 39	49,3	241	i / s	5628	243	630 3	2.41	
7	374 5	2 39	414 5	2 42	514 5	2 43		584 5	2 47	654)	249	
7 25	388 5	2 43	461 3	2 46	533 8	2 40		6063	2 51	675 8	2 57	
75	$\frac{403}{417}$ 1	2 46 2 49	478 1 495	25	553 1 572 5	2 50		628 1 5-0	2 57	703 1 727 5	2 57	1
7 75	432	2 52	512	2 56	592	26		572	2 62	752	261	ı
8 25	446.5	25,	529	2 59	6115	2 63		594	266	76 5	2 68	1
85	461 I	2 58	546 1	263	631 1	2 66		16 1	2 69	701 1	2.71	
5 73	4758	2 61	563 3	2 66	650 8	27		19 3	2 76	825 9	2 68 2 71 2 75 2 78	
9 _	490 5 503 3	2 64 2 67	580 5 597 8	2 69 2 72	670 5 690 3	2 7 2 73 2 76		G0 5 S2 8		575 3	278	1
9 25 9 5	520 1	27	6151	2 72 2 73	710 1	2 79		051	2 79	900 1	2 91	
9 75	535	2 73	632 5	2 78	730	2 82		27 5	255	927	255	1
10 1	570	2 76	650	2 51	750	2 85		)Oc	2 88	950	3 91	J
10.5	550 1	2 81	685 1	2 86	790 1	291		95 1		000	2 97	
11 ]	610 5	2 SG 2 91	720 5 756 1	2 92	\$30 ± 178	3 02		10 5		101	305	l .
11.5	611 1	2 96	792	3 02	312	3 07	10			152	3 14	
122	012	- 30	• • •			,	í					1

TABLE XLIV .- Continued (1 to 1)

Depth of	Bel 100	feet.	Bed 1*0	feet	Bel 140	) feet.	Be 1 160	feet.
Water	•	√r	4	VΓ		√1	A	Vr.
Feet.	'	\ '	i '	1		1	1	
1	100 5	99	120 5	99	140 5	99	160 5	1 00 1
15	151 1	1 21	181 1	1 21	211 1		241 1	انتا
2	202	1 39	242	1 39	252	14	322	1 56
222	227 5	147	272 5	1 47		1	ı	1 1
1 23. 1	2031	1 55	303 1	1 55	353 1	1 56	403 1	1.1
[ 275 ]	275.9	1 62	333 8	1 62	359 8	1 63	4438	1 63
3	304.5	1 69	364.5	1 69	424 5	17.	494.5	17
3:25	330 3	176	395 3	1 76	460 3	1 77	525 3	1 77
3 75	35G 1 382	1 52	426 1 457	1 82	496 1 532	1 83	566 1 607	1 83
1 4 10	405	194	459	194	568	1 95	648	1 96
4 25	434	1 99	519	, , ,	604	2 01	689	2.02
4.5	460 1	201	550 1	24)7	1 040	2.06	730 1	2.07
4 75	456 3	21	581 3	211	676 3	2 12	771 3	213
1 5	512.5	. 2 15	612.5	2 16	7125	2 17	812 5	218
5:25	538 8	2.2	6138	2 21	748 5	2-23	853 8	223
55	, 56ა 1	2 24	675 1	2 25	795 1	226	895 1	2-25
5 75	391 3	2 29	7665	23	821 5	2 31	930 0	2 32
6	618	2 33	735	2 35	858	2 36	978	2 37 2 42
6-25	G44 5	2 38	769 3	24	894 5	2 41	10:20	2 42
6.5	671 1	2 42	801 1	5 44	931 1	240	1061	2 46
6.75	697 S	2 46	S32 8	2 48	967 8	25	1103	2 51
7-25	724 5	25	864.5	2 52	1005		1145	2 55
1 5	778 1	2 58	896 3 928 1	2 56	1041	2 58	1186	2 59
7-25	805	2 62	960	2.64	1115	2 66	1270	2 68
18	832	2 66	992	2 68	11.2	27	1312	272
823	8.9	2 69	1024	272	1159	274	13.4	276
8.5	856 1	2 73	10.6	2 75	1726	278	1396	279
8 75	9133	2 76	1058	2 79	1263	2 52	1438	2 43
9	940 5	28	1121	2.83	1301	2 95	1481	2 86
9 25	967.8	2 83	1153	2 86	1338	2 59	1523	29
9.5	995 1	2 86	1185	3 89	1375	2 92	1565	2.0"
9 75	1023	29	1118	293	1413	2 96	1605	2 97
10 10 5	1050	2 99	1200	2 96	1450	2 99	1650	307
111	1161	3 05	1315 1381	3 09	1525 1601	3 05	1735 1821	3 13
11.5	1216	3 11	1446	312	1676	3 18	19/6	32
12	12,2	3 17	1512	3.21	1752	3-24	1992	3 27
1	1	1	-01-	1	-,05	1		1 - 3.

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# TABLE XLV.-SECTIONAL DATA FOR OPEN CHANNELS

# Trapezoidal Sections-Side-slopes 1 to 1.

Depth	Bed	1 foot	Bed	2 feet	Bed	3 feet	Bec	l 4 feet	Ве	d 5 feet.
Water	A	√R	A	√R	A	<b>√</b> 1	А	√R	1	√r
Feet 5	75	577	1.25	603	1 75	629	2 25	64	5 27	5 658
75	1 31	652	2 06	707	2 81	741	3 56	763	3 4 3	1 779
1	2	723	3	788	4	828	5	856	6	873
1 25	2 81	787	4 06	856	5 31	901	6 56	933	7 81	956
15	3 75	846	5 25	917	6 75	965	8 25	1	9 75	1 03
1 75	4 81	899	6 56	971	8 31	1 02	10 06	1 06	11 81	1 09
2	6	95	8	1 02	10	1 08	12	1 12	14	1 15
2-25	7 31	996	9 56	1 07	11 81	1 12	14 06	1 17	16 31	12
25	8 75	1 04	11 25	1 11	13 75	1 17	16 25	1 21	18 75	1 25
2 75	10 32	1 08	13 06	1 16	15 81	1 21	18 56	1 26	21 31	1 29
3	12	1 13	15	12	18	1 25	21	13	21	1 33
3 25			17 06	1 24	20 31	1 29	23 56	1 34	26 81	1 37
35			19 25	1 27	22 73	1 33	26 25	1 38	29 75	1 41
3 75			21 56	1 31	25 31	1 36	29 06	141	32 81	1 45
4			24	1 34	28	14	32	1 45	36	1 19
4.25				- 1	30 81	1 43	35 06	1 48	30 31	1 52
45			ļ	- }	33 75	1 47	38 25	1 51		1 55
4 75					36 81	15	41 56	1 54	70 /-	1 59
5	)	)	)	j	40	1 53	45	1 58	50	1 62
- 1	- 1	. 1				- 1	ſ	- 1	- (	

Table XLV -Continued (1 to 1)

Deş tlı	Bed 6	feet	Be l	feet	Be 1 8	feet	Bed 9	feet.	Bed 1	0 feet
Water	A	√1	A	<b>√</b> 1	A	<b>√</b> 1	A	√r	A	√r
Feet 5 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	3-25 5 76 9 06 11-25 13 56 18 56 21-23 36 56 47 25 36 56 67 57 77	662 7811 975 5 1 11 1 17 1 123 1 28 1 32 1 37 1 41 1 48 1 52 1 62 1 69 1 77	3 75 581 8 10 31 12 75 15 31 12 75 75 15 31 12 75 75 15 31 15 31 15 30 75 75 81 75 75 81 75 75 78 78 78 78 78 78 78 78 78 78 78 78 78	667 798 902 989 1 107 1 13 1 19 1 43 1 13 1 31 1 31 1 31 1 31 1 50 1 62 1 63 1 72 1 178 1 18		672 803 911 1 1 108 1 127 1 132 1 147 1 141 1 151 1 161 1 163 1 163 1 175 1 181 1 181 1 183	4 63 10 12 81 18 81 22 33 36 36 37 56 31 66 75 56 31 17 87 88 82 24 31 17 81 82 82 83 11 17 8 8 82 82 83 83 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 82 84 84 82 84 84 84 84 84 84 84 84 84 84 84 84 84	667 795 919 101 116 1123 1238 133 133 1134 1156 164 167 1171 118 118 118 118 118 118 118 118 1	3 25 8 06 11 4 06 11 25 5 5 6 12 5 7 10 6 6 15 25 6 11 2 5 1 12 5 1 1 1 2 5 1 1 1 2 5 1 1 1 1	678 815 926 102 111 172 129 129 129 129 129 129 129 129 129 12

TABLE XLV .- Continued (I to 1)

Depth	Be 1 1	2 feet	Bed 1	feet.	Bed 1	6 feet	Bed 1	S feet.	Bed :	20 feet.
Water	A	√R	A	√ <i>I</i>	1	√r	A	√Γ	ſ	√r
6-25 6-75 7-25 7-25 7-75	146 3	1 9 1 93 1 96 1 99 2 02 2 05 2 07 2 1 2 13	1333 1401 147	1 87 1 91 1 94 1 97 2 03 2 06 2 20 2 21 2 14 2 17 2 19	161 188 6 176 3 184 1 192 200 1 208 3 216 6 225 233 6 242 3	1 83 1 87 1 97 1 94 1 97 1 2 90 1 2 2 90 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	144 151 6 159 3 167 1 75 161 3 161 3 160 6 160 6 175 186 6 187 3 187 1 187  1 89 1 89 1 1 96 2 2 3 66 3 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	15 56 56 56 56 67 56 56 56 56 56 56 56 56 56 56 56 56 56		

Table XLV -Continue ! (1 to 1)

Degu	Bed 25 feet.		Red 2	fret	Bel t.	feet.	Bel (	fret	Brd 4	S feet
of Water	A	<b>1</b> /1	A	, r	٨	<b>~</b> 'F	A	vr.	А	√r
Feet 1	26	-966	31	-970	36	-976	41	-975	46	281
2 7	39.75 51	1 33	47.25 61	131	51 75 74	1 14	62·25 81	1 19 1 36	19 75 94	1 19
225 225 227	61 31 65 75		72.56 N/25	1 41	43.91	1 42 1 49	95-06 106-3	1 43	106 3 118 S	1 44
275 3 325	76 31	1 54	90(0	1.54 1.66	103 8 114 124 3	162	117 6 129 140 6	1 57	131 3 144 156 8	1 38 1 64 1 7
355	91 81 99 75 107 5		105 I 117 3 126 6	177	134 %	175	1523	70 1 77 1 78 1	1618	1 7 1 76 1 81
4-25	116	1 79	136 145 6	151	1.6 166 S	1 81	176	185	196 209 3	1 97
475	132 9	1 53	1 5 3 165 1	191	177 %	1 93 1 97	200 3 212 6	1 95	236 3	1 96 2 01
525	150 158 8 167 8	1 97 1 97 2 03	175 185 1 195 3	2 03 2 07 1 2 07	200 211 3 222 8	2 02 2 06 2 1 2 14	257 6 247 3	2 04   2 08   2 12	2.0 263 8 277 8	2 06   2 1 2 14
2 75 6	176 S	1207	265 6 216	211	234.3	2 14 2 18	263 1	2 16	201 8	2 18
625	195 3 204 8	2 14 2 17	226 6 237 3	2 18 2 21	2079	2-21 2-25	259 I 302 3	2 24 2 28	320 3 334 8	2 26 2 3
6 75 7 25	214 3 224 233 8	2-24	245 1 2-9	2-23 2-23 2-31	281 8 294 306 3	223 232 235	315 6 329 342 6	2 31 2 34 2 37	349 3 364 378 8	
7 73	243 8 253 8	2-27 2-3 2-33	270 1 281 3 292 6	2 34	318 8	2 35 2 38 2 41	3563	2 37 2 41 2 45	3)3 S 408 S	2 41 2 44 2 47
8 23	264 274 4	2 35	304 315 6	2 4 2 43	344	2 44 2 47	399.1	2 48	474 489 4	25
8 75	284 8	2 41	327 3 339 1	2 40	369 8 382 9	25	412 3 426 6	2 o4 2 o7	470 4	2 57
9 9-2⊲ ⊧9-5	306 316 9 327 8	2 46 2 49 2 51	351 363 1 375 3	2 32 2 34 2 37	396 409 4 422 8	2 56 2 59 2 61	441 45ヶ6 4703	26 262 265	486 501 9 517 8	2 62   2 66   2 68
19 75	338 9 350	2 54	387 6 400	2 6 2 62	436 4 450	2 64 2 67	485 1 500	2 68 2 71	ა33 9 ნამ	2 71 2 74 1
10 5 11				1			530 3 561	2 76 2 81	582 8 616	2 79 2 85
11 5 12		İ					593 3 624	2 86 2 91	650 8 684	2 9 2 94

TAPLE XLV -Continued (1 to 1)

					,—-					
Dej th	Bed J	) feet	Belo	0 feet	Bed '	O feet,	Bed 9	191 et	Beta	) feet
Water	A	√P	}_1	VI	A	√r	1	1/2	4	15
Feet 5 25 57 25 77 25 77 25 77 25 77 25 77 25 77 25 77 25 77 25 77 77 77 77 77 77 77 77 77 77 77 77 77	51 22 101 6 117 6 3 145 1 159 173 1 159 173 1 157 3 6 216 6 245 3 250 1 275 250 3 353 1 379 1 447 3 447 5	982	61 92 25 124 140 1 156 3 172 6 189 6 222 3 239 1 239 1 290 3 342 6 360 3 378 1 414 1 443 3 47 6	583	-	087 12 37 146 153 166 167 179 1179 1179 1179 120 160 120 160 120 160 173 173 174 175 175 175 175 175 175 175 175 175 175	}	95' 1 46 1 14 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	91 194 207 6 231 3 251 1 279 327 3 327 3 327 3 327 3 340 1 47, 500 1 52, 3 540 1 601 6 (27 3 (27 3 (27 3) 1 (27 3) 1 (27 3) 1	99 134741 1168 1179 1187 1187 1187 1187 1187 1187 118
8 8 8 8 9 9 9 E E E E E E E E E E E E E	464 0 497 3 514 1 531 1 548 1 548 1 548 1 548 1 548 1 548 1 548 1 548 1 744 1	00000000000000000000000000000000000000	544 563 1 5\2 3 601 6 621 640 6 660 3 680 1 740 3 7\1	24636 27636 27636 2763 2763 2763 2763 2763	624 615 6 617 6 617 3 (S) 1 711 733 1 733 1 737 6 843 3 843 3 951	26367776925978	704 725 1 7 2 3 7 7 6 501 8 5 6 8 5 0 3 8 5 0 3 9 40 3 001 0.3	32222822226	781 810 6 837 3 864 1 891 918 1 915 3 9726 900 900 1111	100010000000000000000000000000000000000

TABLE XLV -Continued (1 to 1)

Dep*h	Bet In	) feet,	B-1 1*	) feet	Bel 14	) feet.	Bel 16	O feet.
Water		,r	A	√r.		√r	,	√r
Pet 1 2 2 7 7 7 2 7 7 7 7 7 7 7 7 7 7 7 7 7	15	\$\times 1 \t	121 221 221 221 221 221 221 221 221 221	\$21.54 1.54 1.52 1.54 1.52 2.55 1.54 2.55 2.55 2.55 2.55 2.55 2.55 2.55 2	141 254 7 7 25 7 7 25 7 7 25 7 7 25 7 7 25 7 7 25 7 25 7 25 7 1 1 25 7 25 7	\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	161 721 750 1 4 750 1 4 750 1 4 750 1 4 750 1 4 750 1 1 750 1	\$4448677714986672884888465588857458886555551488

Table XLVI—Sectional Data for Open Channels.

Truperally Socion—Sided of 12 to 1

D- '7	Bed 1	•	Bed	est.	B-1	8 f≈t.	24	1 ***	r:	
Wat -				٠,٠	4	ι, ε	4	1,7	1	1 . 1
Tres.	~-	+0	1 %	-6	1	₹3	28	161	25	5 -64
-,	1 9	7.0	2 %	-1	ઉત્તર		-~4	-,	4 ~7	1 ==
1	2 -	-4	٠,	79	4 3	~3		~	6.5	~~
12	5-9	~1	4~4	~3	619	۰,	: 34	-03	`-1	4
15	- 4>	٠.	6 57	~	7~7	47	9 ~7	1	10~7	112
1 ~	6 34	-93	<b>149</b>	44	9~4	115	11 ~2	146	15 74	146
2	`	-0.3	1)	114	12	110	14	1 12	16	1 15
2-25	9~4	114	12+19	1119	14 %	1 14	16-3	1 17	1~~4	15
2	11~	1 443	14 37	1 14	16 👡	119	10 ~-	122	21~7	1-25
2-	14 117	1 14	16 🛂	1 19	10 3	123	보다	1-2"	2,40	15
3	16 5	1 15	19 31	1:23	22	1-2	2	1 ~1	25	1 ~1
32		-	<u> 가</u> 和	1-5	210	12	J- ~4	1 ^	5741)	. در د
3.5	- ]		2, **	12	>~7	1 2	€° ~ <del>.</del>	14	-	1 43
- 75	!		200	1 2	24	14	C 44)		-	1 4-
4	- '	-	2	1	55	1 44 4	• •	14- 4		1 1
4-25	-	-	- 1	-	.,-1	145 4	1146)			1 -
4 -	-	-	-		r~7	1 1 4			-	
4 7"		-			(117	1				111
,	-		-	- 7	5	1	-	1-2 6	2-	14.1
	_						_			

Tarlf XLVI -Continued (11 to 1)

Depth	Bed 6 feet Bed 7 feet.		feet.	Bed 8 feet.		Bed 9 feet.		Be l 10 feet		
of Water	1	√r	А	√r	А	√r	A	√P	A	√r
Feb. 575 2557 2557 2557 2557 2557 2557 2557	3 37 5 7 3 9 84 2 37 15 09 12 37 15 09 12 37 15 09 247 84 31 5 34 43 59 43 59 44 59 66 75 72 84 66 75 84 09	66 78 97 1 04 1 17 1 123 1 1 23 1 1 23 1 1 24 1 1 25 1 25 1 2	3 87 6 00 11 00 23 34 26 84 26 84 27 84 28 87 29 84 20 84 20	67 779 89 98 1 066 89 1 122 1 18 1 13 1 13 1 13 1 1 13 1 1 1 1 1 1	4 37 6 84 9 5 12 34 85 9 5 12 34 46 37 5 14 6 37 5 17 5 17 7 5 18 5 10 9 6 6 37 17 7 5 18 9 3 9 5 10 2	67 8 9 99 107 114 126 131 136 146 15 165 165 179 176 178 183 183	4 88 7 539 10 5 13 59 20 34 27 84 11 88 20 34 40 5 40 5 40 5 40 5 40 5 40 5 40 5 40	68 81 108 1108 122 128 128 128 128 128 138 138 148 148 164 164 168 171 170 170 181 181 181 185 192 203 211	5 38 8 34 111 5 11 8 38 92 09 9 34 38 9 32 09 9 34 38 9 38 4 47 5 5 38 8 1 34 107 1 11 124 4 17 1 12 1 1 1 12 1 1 1 1 1 1 1 1 1 1 1	68 81 101 109 1123 123 123 123 1134 1134 1134 1134 11

TABLE XLVI - SECTIONAL DATA FOR OPEN CHANNELS

Trapezoidal Sections-Side slopes 11 to 1

							_	_		
Depth of	Bed	l foot	Bed	2 feet	Bel	3 feet	Bed	4 feet.	Bed	o feet
Water	А	√P	A	√P	A	√E		\sqr	1	√R
Feet	97	ə6	1 33	6	1 88	63	2 38	64	2 87.	64
75	1 59	r5	2 31	71	3 09	73	3 81	76	4 09	77
1	25	74	30	79	45	83	55	85	6.5	\$7
1 23	3 19	81	4 84	86	6 09	9	7 31	93	8 20	9,
15	4 48	87	6 37	93	7 87	97	9 37	1	10 87	1 02
17,	6 34	93	8 09	99	9 84	1 03	11 59	1 06	13 34	1.09
2	8	99	10	1 04	12	1 08	14	1 12	16	1 Io
22)	9 84	1 04	12 09	1 09	14 34	1 14	16 59	1 17	18 84	12
2,	11 87	1 09	14 37	1 14	16 87	1 19	19 37	1.22	21 87	1 25
2 -,	14 09	1 14	16 84	1 19	19 59	1 23	22 34	1 27	25 09	13
3	د 16	1 18	ا 30 19	1 23	22 5	1 28	200	1 31	- / /	131
32,			22 34	1 28	206	1 32	28 81	1 36	32 09	1 39
3 5			20 37	1 32	28 87	1 36	32 37	}		1 43
3 75			28 6	1 36	32 34	14	36 00	1 14	39 84	1
4		1	32	1 39	36	1 14	40	1	**	1 1
4 25			j		39 81	1 48	44 (7)	-	15 31 1	
4 ,	- 1			į	43 87	1 1	49 37	[ ]	, 8_	C1
4 75	- 1	- 1	- 1		48 09	1 -	7251	1	" 1	cı
٦	]	ļ	j	ł	2,	17	7 ,	112	, .	
	- 1	1			- 1		_			

TAPLE XIVI -Continued (11 to 1)

h	Bel 6 feet	Bed 7 feet.	Hed 8 feet		Bed 9 feet.		Bed 10 feet.	
t	t ,r	t vr	,	, P	A	√r	ŧ	√r
31 3 33 34 37 37 43 49 48 5 52 59 57 37 62 34 67 5	5 34 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	7 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	466-3115314584545454545532 466-3115314584545454555 566-3115314585 566-315 566-315 566-31	67 9 87 1112 A 112	4 83 7 50 10 7 11 0 1 10 1 11 0 0 10 0 31 0 21 1 11 92 1 40 0 40 0 40 0 40 0 10 0 10 0 10 0 10	1 23 1 23 1 33 1 34 1 45 1 45 1 45 1 45 1 45 1 45 1 45 1 4	138 934 115 114 54 115 116 116 116 116 116 116 116 116 116	- 68 - 92 - 100 - 1106 - 123 - 134 - 1

TABLE XLVI -Continued (11 to 1)

Depth of Water											
Table	30	Bel 1	9 feet	Bed 1	i feet	Bed 1	S f et	Bed 1	S f vet	Bed ℃	fert.
To   94   82   114   145   125   145   1	Water	A	√P	A	√R	4	√r	A	vr	į	√P
0 1 2 42 32 4 2 17 9 7 10 11 1 2 42 32 7 4 2 17 10 10 1 2 47 337 ( 2 47 2 7 2 7 2 7 2 7 2 7 2 7 2 7 2 7 2	575 2 - 1775 5 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	9 \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\	82 102 111 123 115 123 124 123 142 143 143 143 143 143 143 143 143 143 143	11 34 13 5 19 84 24 37 29 09 34 39 09 44 37 49 94 50 34 66 37 73 39 96 39 97 37 100 3 100 3 1114 8 1120 4 1130 1 1130 1 1130 1 1131 1 1130 1 1131 1 1130 1 1131 1 11	29 94 112 12 12 12 12 12 12 12 12 12 12 12 12	12.54 17.34 27.87 32.99 49.73 50.91 49.73 50.91 60.54 74.77 50.91 1117.03 1117.04 1117	\$3 94 113 121 125 134 146 1316 131 131 132 134 146 1316 1317 133 133 133 133 133 133 133 133 13	19 5 25 1 37 35 00 1 3	9 0 0 14 12 29 11 12 29 11 11 12 29 11 11 12 29 11 11 12 29 11 11 11 11 11 11 11 11 11 11 11 11 11	91 34 76 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	9551523 7 37 34 34 45 45 45 45 46 47 47 47 47 47 47 47 47 47 47 47 47 47

Tarle XLVI -Continued (11 to 1)

Depth	Red 2	freL	Bed 30	) feet.	Bel 8	freL	Bel 4	Bol 40 feet.		fert.
Water	A	,,	(	<b>V</b> 1	4	Vr	А	√r	1	√r
eif.	20 5 5 6 4 7 5 6 7 7 1 1 1 4 8 8 1 2 1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1	1 16 1 32 1 30 1 45	31 7 48 98 66 66 66 66 66 66 66 66 66 66 66 66 66	77 118 1133 114 1175 1175 118 118 1197 1201 1213 1223 1233 1243 1243 1243 1243 124	4 26 7 5 88 76 88 76 88 76 88 76 88 76 88 76 88 76 88 76 88 76 76 88 76	97 1 18 1 34	41 5 63 98 66 97 50 100 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-98 1 18 1 35	46 5 70 88 70 88 109 8 109 8 8 109 8 8 109 8 109 8 109 110 110 110 110 110 110 110 110 110	98
9 9·25 9·5 9·75 10 10·5 11 11·5	346 5 359 6 372-9 356 4 400	2 46 2 48 2 51 2 53 2 56	391 5 405 8 420 4 435 1 450	2 33 2 36 2 36 2 8 2 61	436 5 4 2 1 467 9 453 9 JIO	2 54 2 57 2 6 2 63 2 65	491 5 498 3 51 4 52 5 550 4 621 5 658 4 696	2 58 2 61 2 64 2 66 2 74 2 79 2 84 2 89	502 0 562 0 581 3 600 637 9 676 5 715 9	2 61 2 64 2 66 2 69 2 72 2 77 2 83 2 83 2 93

TABLE XLVI -Continued (11 to 1)

Depth	Bed 50 fe	eet	Bed ro	feet.	Bed	0 feet	Red 80	feet	Bed 90	feet.
Water	A	√r	A	√R	A	√R	A	√R	A	√r
Feet 5 20 75 20 575 20	51 5 5 5 6 1 1 5 5 6 1 1 5 5 6 1 1 5 5 6 1 1 5 6 6 1 1 1 1	98 919 1364 1451 1486 1486 1486 1486 1486 1486 1486 148	61 5 5 6 9 11 12 6 6 12 6 14 2 4 6 14 2 6 14	98 1187 1145 1159 1159 1159 1159 1159 1159 1159	71 5 4 108 4 160 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-	81 5 123 4 166 187 6 209 4 231 3 2-3 5 275 8	888	91 o 4 188 4 1890 1 188 4 1890 1 234 4 8 233 3 338 4 233 3 338 4 400 4 401 3 0 401 4 180 4	√F

TAPLE LVII -SECTIONAL DATA FOR OVAL SEWERS (Art 3)

Metropolitan Oroi l

	Full		Two-third	ls full	One third full.		
D mens ons	A	√R	A	√r	A	√r	
1 0"×1 0 1 2"×1 0" 1 4"×2" 0" 1 6"×2" 3" 1 6"×2" 6" 1 10"×2 9"	1 15 1 16 2 04 2 3 3 19 3 56	54 -58 -62 -66 -69 -73	76 143 134 17 21	56 61 65 69 73 76	28 39 31 C4 79 96	45 49 3 6 59 62	
2 0°×3 0° 2 2°×3 3° 2 4°×3 0° 2 6°×3 9° 2 8°×4 0° 2 10°×4 3°	4 9 5 39 6 25 7 18 8 17 9 22	59 59 59 50 70	3-02 3-55 4-12 4-72 5-38 6-07	79 83 86 88 42 93	1 14 1 33 1 55 1 78 2 02 2 28	64 67 69 72 74 76	
3 0"×4 6" 3 2"×4 9" 3 4"×5 0" 3 6"×5 3" 3 8"×5 6" 3 10"×5 9"	10 31 11 2 12 76 14 07 15 41 16 88	93 -96 -98 1-01 1-03 1-06	6 8 7 58 8 4 9 26 10 16 11 11	97 1 03 1 05 1 08 1 1	2 % 3 16 3 48 3 % 4 17	9 81 83 85 87 89	
4 0" × 6 0" 4 2" × 6 3" 4 4" × 6 6" 4 6" × 6 9" 4 8" × 7 0" 4 10" × 7 3"	18 38 19 94 21 57 23-26 25 01 26 83	1-08 1-1 1-12 1-14 1-16 1-18	12 09 13 12 14 19 15 31 16 46 17 66	1 12 1 15 1 17 1 19 1 21 1 23	4 54 4 93 5 33 5 75 6 19 6 64	91 93 95 96 98 1	
0" × 7 " 2" × 7 9 3 4" × 8 0" 6" × 8 3" 8" × 8 6" 5 10" × 8 9" 6 0" × 9 0"	28 71 30 67 32 67 31 74 36 88 39 08 41 35	1.20 1.21 1.26 1.28 1.3 1.3 1.32	18 9 90 18 21 3 22 86 24 7 25 7 27 21	1-26 1-28 1-3 1-32 1-34 1-36 1-38	7 1 7 58 8 08 8 59 9 12 9 66 10 22	1 02 1 03 1 05 1 07 1 09 1 1 1 11	

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TABLE XLVIII —SECTIONAL DATA FOR OVAL SEWERS (Art 3)

Hawksley's Oronl

Transverse Dru jeter	Fı	ш	Two th	rds full	One th	urd full
Dittietet	A	√P	1	√₽	t	√R
1 0'	1	53	67	56	26	44
1 2"	1 36	57	91	6	35	48
1 4	1 77	61	1 19	64	46	51
1 6	2 24	64	1 51	68	58	54
1 8"	2 77	68	1 87	72	71	57
1 10'	2 35	71	2 25	75	86	6
2 0	3 98	74	2 69	79	1 03	63
2 2	4 67	77	3 14	82	1 21	66
2 4	5 42	8	3 66	85	1 4	68
2 6	6 22	83	4 2	88	1 61	7
2 8	7 08	86	4 77	91	1 83	72
2 10	7 89	89	5 38	94	2 06	74
3 0	8 97	91	6 04	96	2 31	77
3 2	9 98	94	6 73	99	2 58	79
3 4	11 06	96	7 46	1 02	2 55	81
3 6	12 2	98	8 22	1 04	3 15	83
3 8	13 38	1 01	9	1 07	3 45	85
3 10	14 63	1 03	9 87	1 09	3 78	85
4 0	10 93	1 05	10 74	1 11	4 11	89
4 2	17 28	1 07	11 66	1 14	4 46	91
4 4"	18 69	1 09	12 57	1 16	4 82	93
4 6"	20 18	1 12	13 6	1 18	5 20	91
4 8	21 68	1 14	14 ( 2	1 2	5 59	96
4 10'	23 2	1 16	15 65	1 22	6	98
5 0'	24 89	1 18	16 79	1 24	6 42	1
5 2'	26 57	1 2	17 92	1 27	6 %6	1 01
5 4"	28 32	1 21	19 1	1 29	7 31	1 03
5 6"	30 11	1 23	20 26	1 31	7 76	1 04
5 8	31 56	1 25	51 5	1 33	8 24	1 06
5 10"	33 87	1 27	92 84	1 34	8 74	1 07
6 0"	35 81	1 29	21 17	1 36	9 25	1 09

Table XLIA —Sectional Data for Oval Sewifs (Art 3)

Incl. on's Pea top Section

#### Two ti irds full One ti pifu i Full D mens ons √r √r 11 1 A A 0" x 1 1 039 ,2 646 242 11 2' × 1' 9" 57 88 33 47 1 414 νſι 1 4"×2 0" 1 816 1 148 Ğĺ 431 G 6"×2 37 2 337 Ğ3 1 4"3 545 53 8"×2 67 1 793 2555 67 68 65 ьG 10"×2 0 3 491 2115 72 913 59 0" 70 0" x 3 4 174 73 76 2.583 969 62 2"×3 3\* 78 1 136 64 4 574 3 033 4"×3 6" 561 3 016 81 1 310 6"×3 9" 82 6 491 4 034 81 1 113 69 8"×4 0" i 722 7 38) 84 4 993 86 71 10" × 4 8 337 87 5 184 89 1 943 73 3 0"×4 6" 99 5 813 -9:2 2 179 76 9 347 2 427 3 2"×4 9" 93 6 478 10 41 94 78 á 4"×5 0" 11 54 91 7 172 7 912 97 2 602 8 3 š š2 $6" \times 5$ 12 72 97 99 2 967 8" × 5 67 3 13 96 99 8 461 101 324 84 10"×5 3 5 % 15-26 1 01 9 492 1.03 80 0" × 6 0" 10 33 1.06 38-4 87 16 02 1 03 2" × 6 3" 18 03 1.06 11 22 1.08 4 201 89 4" x C 6" 12 13 īi 91 19.5 1 08 4 )43 C" × 6 97 13.05 1 12 4 903 93 21 03 11 8" × 7 0" 22 63 1.12 14 0" 1 14 F 274 91 10"×7 3\* 24-26 1 14 15 09 1 16 5 6.3 96 0" × 7 6" n, 2, 96 1 16 16 14 15 6:0.4 2" x 7 gr 99 27 72 1 15 17:24 1.2 £ 46 4" x 8 Ô 29 54 1 19 18 37 i 20 6 811 L of 7 7 321 6" x h 31 42 21 19 34 1.24 1.02 5"x 5 6" 33 7 77 33 % 1 20 74 ı 26 1 01 10° × 5 9\* 3, 31 21-98 1.25 8-231 140 0" x 9 0" 5 718 147 37 31 23 20 1.3

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# TABLE L —RATIOS OF COMBINED LENGTH OF TWO SIDE SLOPES TO DEPTH OF WATER

Side slope = \( \frac{1}{2} \) to 1 \( \frac{3}{2} \) to 1 \( 1 \) to 1 \( 1 \frac{1}{2} \) to 1 \( 1 \frac{1}{2} \) to 1 \( 2 \frac{1}{2} \) to 1 \( 3 \) to 1 \

These ratios can be used for calculating R for channels outside the range of tables  $x_{111}$   $x_{121}$ 

# Table La—Circular Channels partly full (Art 6)

The Diameter of the Channel is supposed to be 1.

Depth of Water	Angle sub tended by Wet Portion of Border	Relative Values of A	Relative Values of $\sqrt{R}$
Feet 25	120°	196	767
5	180°	5	1
75	240°	804	11
1	360°	1	1

For actual values of A and  $\sqrt{R}$  see table xxiii, page 142.

#### CHAPTER VII

#### OPEN CHANNELS—VARIABLE FLOW

[For preliminary information see chapter it articles 10 to 14 and 17 to 21]

#### SECTION I -BENDS AND ABRUPT CHANGES

1 Bends —The loss of head at a change in direction in an open stream is, as in the case of a pipe, greater for an elbow thin for bend. The formula for loss of head at a bend arrived at by observations on the Mississippi is  $H = \frac{U^2 \sin^4 \theta}{134}$  where  $\theta$  is the angle subtended by the bend. This takes no account of the radius. In a bend of 90° the loss of head by this formula is  $48\frac{U^2}{27}$ . Generally a single bend with ordinary velocities causes little heading up, but if a stream has a long succession of bends their cumulative effect may be considerable. It is practically the same as that of an increase of roughness, and may be allowed for by taking a lower value of the co-efficient C. How far the loss of head at a bend depends on the radius of the bend is not known (Cf chap V art 4)

At a bend there is a 'set of the stream towards the concave bank, the greatest velocity being near that bank, and there is a

raising of the water level there, so that the surface has a transverse slope (Fig 117) There is also a deepening near the concave bank and a shoahing at the opposite one, but this is not all due to the direct action of centrifugal force The high water level at the concave

Fig. 11"

bank, due to centrifugal force, gives a greater pressure and tends to cause a transverse current from the concave towards the convex bank. This tendency is, in the greater part of the cross section, resisted by the centrifugal force. But the water near the bed and sides has a low velocity, the centrifugal force is therefore smaller, and transverse flow occurs. Solid material is thus rolled towards the convex bank, and it recumulates there because the velocity is low. To compensate for the low level current towards the convex bank there are high level.



currents towards the concave bank. The directions of the currents are shown by the arrows on Fig. 117. In Fig. 118 the dotted line shows the direction of the strongest surface current and the arrows the currents near the bed. This explanation is due to Thomson, and has been confirmed 1) him experimentally. When the channel is of masonry or even very hard soil the deepening TVIV cannot occur, but the formed the material for it hears.

the bank RST may still be formed, the material for it being brought down by the stream

As the transverse current and transverse surface slope cannot commence or end abruptly there is a certain length in which they vary. In this length the radius of curvature of the lend and the form of the cross section also tend to vary. This can often be seen in plans of river bends the curvature being less sharp towards the ends. This principle has been adopted in construct ing river training walls and it appears to be sound as tending against any abruptness in the change of section. For training walls to remove burs at the mouth of the Mississippi it has been proposed to construct instead of two walls only one wall having a curve conceive to the stream. The success of this plan would appear to depend on whether the curve is sharp enough to ensure the stream I coping close to the wall and not going off in another direction.

The sectional area of a stream is often less at all end thin in straight reaches, especially when the channel is hard, so that the stream cannot excavate a hollow to compensate for the silt bull, but the surface width is often greatest at bends, and in constructing training walls the width letween the walls is sometimes increased at bends. In the silt elevances of some tortucus canals in India it was once the custom to remove the silt J sJ, the dotted line showing the section of the cleared channel in the straight reaches. To allowance was made for the hollow II is A silt-bank so immoved quickly forms again. Its removal is cuivalent to the digging of a hole or recess in the led

When once a stream has assumed a curved form, be it ever so shipt, the tendency is for the bend to increase. The greater velocity and greater depth near the concave bank react on each other, each inducing the other. The concave bank is worn away, or becoming vertical by erosion near the bed, cracks, falls in, and is washed away. The bend may go on increasing as indicated by the dotted lines in Fig. 119, a deposit of silt occurring at the

convex bank, so that the width of the stream remains tolerably constant Some of the large Indian rivers flowing through alluvial soil sometimes cut away, at bends, hundreds of acres of land, together with the trees. crops, and villages standing thereon Works to check the erosion would cost many times as much as the value of the property to be saved When a bend has formed in a channel previously strught, the stream at the lower end of the bend, by setting against the bank, tends to cause another bend of the opposite kind to the first. Thus the ten dency is for the stream to become tortuous, and while the tortuosity is slight the length, and therefore the slope and velocity, are little affected, but the action may continue until the increase in the length of the stream materially flattens the slope, and the conse quent reduction in velocity causes crosion to cease Or the stream during a flood may find, along the chord of a bend, a direct

F10. 119

and, along the chord of a bend, a direct route, with of course a steeper slope. Scouring a channel along this route it straightens itself, and its action then commences afresh

2 Ohanges of Section—An 'obstruction is anything causing an abrupt decrease of area in a part of the cross section of a stream such as a pier or spur There may or may not be a decrease in the sectional area of the stream as a whole. There is a tendency to scour alongside an obstruction owing to the increased velocity, and downstream of it owing to the eddies. When a spur is constructed for the purpose of deflecting a stream or checking crossion of the bank, the scour near the end of the spur may be very severe, even though their may be very little contraction of the stream as a whole. If the bed is soft the spur may be undermined. Ventinous limin, of the bank with

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protective material is not open to such an attack. Similarly a hole may be formed alongside of and downstream of a bridge pier. The hole may work back to the upstream side of the obstruction though there is little original tendency to scour there

When an obstruction reaches up to the surface, or nearly up to it, there is a heaping up of the water on its upstream side due to the checking of the velocity. In the eddy downstreum of an obstruction the water level is depressed. The changes of water level and velocity are local, that is, they do not necessarily extend across the stream, and they are independent of the effects of any general change—supposing such to occur—in the sectional area of the stream. Their amounts cannot be calculated, but they often have to be recognised. They should be avoided in observing water levels where accuracy is required, as for instance when finding the surface slope. The discharge of a branch will be increased by a spir or obstruction just below it, and decreased by one just above it. On some irrigation canals in India, where the velocity is high and the channel of boulders, the cultivators somotimes run out small spurs below their water course heads in order to obtain more water.

An obstruction causes a 'set of the stream,' that is a strong current, as shown by the arrows in Fig 119, but the distance to which such a current extends depends entirely on its impetus, and is not usually great. If a spur is merely intended to cause slack water or silt deposit on its own side of the stream several shorts spurs will do as well as one long one, but when the object is to cause a stream to set against the opposite bank the spurs may have to be very long

In a short deep recess in the bed or bink of a stream or down stream of in obstruction if it is large enough to cause dead water, there is generally a rapid deposit of silt, but not where strong

eddies occur

When an obstruction causes material reduction of the section of the stream the velocity past it is increased, and the scour may be excessive, both from the high velocity past it and (if there is a subsequent expansion of the stream) the eddies downstream of it. Thus a partly formed dam  $EF(F_{\rm b}=119)$  is, unless the gap is quickly closed, liable to be destroyed by the stream, and so is any structure which reduces the water way. In order to lessen scour of the banks downstream of contracted water ways the claimed is sometimes widened out so as to form a basin in which the eddies exchants themselves.

3 Bifurcations and Junctions—The general effects of these have been stated in chapter it (att 20). In an irrigation distributing constructed in India the velocity was exceptionally high, and it was found that the discharges of some narrow making outlets, taking off from the distributing at right angles, were so small that it became necessary to rebuild them at a smaller angle. On the other hand, it was once the custom to build the heads of the distributants themselves at an angle of 15° with the canal, but they are now built at right angles. The velocity in the canal is 2 or 3 feet per second, and that in the distributary less. A slight fall into the distributary is not objectionable. A skew head is suitable in cases where loss of head is not permissible.

When there is a bend in the main stream importance is some times attached to the set of the stream as affecting the supply in a branch taking off on the concave lank. The velocity in the branch is that due to its slope and to the depth of water in it The advantage possessed by the Iranch as compared with one on the opposite bank is the greater depth of water, owing to velocity of approach This advantage is small except in the case of a sharp bend and a high velocity. A river about 20 feet deep was croding the concave brilk at a bend. An attempt was made to divert it by a straight cut, about a mile long across the bend Owing to the high level of the sub-soil water, the cut could only be dug down to about 2 feet below the water level of the river The slope of the cut was about one and a half times that of the river, but owing to the small depth of water the velocity was low, and the cut or at least its upper part, rapidly silted up. The reason given for its failure was that its head was not so placed as to eatch the set of the stream at the ben I next above This set might have given an inch or two more water and the cut might have taken a few days longer to silt up

Sometimes the deposit of silt in a branch channel is attributed to some peculiarity in its off take, such as the angle of off take or the arrangement of the head <sub>actives</sub>. If these matters have any importance it can only be when they affect the stratum of water drawn upon (thus altering the silt charge or the amount of rolled material broug, bit in), or when they directly affect the gauge reading or depth of water which, in a given channel is the only factor governing the velocity, and, so far as is known, the silt-supporting power. In river diversion works spurs are sometimes used to 'drive

In river diversion works spurs are sometimes used to 'drive the river' down a branch channel A spur may make the current set against the brunch head (art 1), but unless the spur is so long as to greatly contract the water way, the rise of water level will not be great except in cases of very high velocities, and the river will continue to distribute itself according to the discharging capacities of the two branches. It is only by closing or thoroughly obstructing one branch or enlarging the other that the stream can be forced to alter its distribution of discharge

At a junction of one stream with another there are the usual eddles and inequalities in the water level, all depending as before on the sharpness of the angle and on the velocity. When the main stream is not much larger than the tributary, the latter may cause a set of the current against the opposite bank and crode it.

4 Relative Velocities in Gross section—In every case of abrupt contraction in a stream there are (chap in art 21) eddes which extend back to the point where the fall in the surface begins. Upstream of these eddies the distribution of the velocities in the cross section is not affected. In the case of a pier, even a wide one, in the middle of a straight uniform stream, the maximum velocity remains in mid stream till just before the pier is reached. If a plank or gate obstructs the upper portion of a stream from side to side, the surface velocities are affected for only a short distance upstream. A spur or sudden decreace of width causes slack water for only a short distance. In all these cases the state of the flow further upstream, as far as regards the distribution of the velocities is precisely the same as if no obstruction existed. In the case of a were visual evidence is wanting, but by analogy the same law holds good.

# SECTION II -VARIABLE FLOW IN A UNIFORM CHANNEL

(General De cription)

5 Breaks in Uniformity —Variable flow may be caused by a change in slope (Figs 16 and 17, pp 24 and 25) or in roughness (Figs 120 and 121) by a de

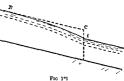
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bouchure into a pond or river (Figs. 122 and 123), by a weir (Figs. 121 and 125) by a change in width (Figs. 126 and 127) or in bed lete! (Figs. 1. and 1.9) Heading.

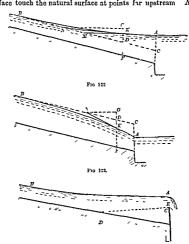
up may be caused by a local contraction or submerged weir

(Fig 130), but the analogous case of a local enlargement has no effect. A change of hydraulic radius seldom occurs without a

change of sectional area, and it need not therefore be considered as a separate case. A bend generally causes some degree of heading up. In each case the line BC is the 'natural water surface' of the upper reach, that is, the surface as it would



have been if no change had occurred The profiles of the watersurface touch the natural surface at points far upstream Above



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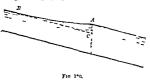
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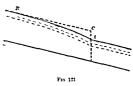
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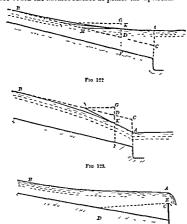
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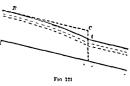
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120 and 121), by a de bouchure into a pond or river (Figs 122 and 123), by a weir (1 igs 121 and 125), by a change in width (1 igs 126 and 127), or in bed level (1 igs 125 and 129). Heading

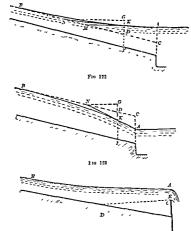
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these points the flow is uniform if the reach extends far enough. In heading up there is a tendency to silt and in drawing down

P C 1°

In the cases shown in Pigs 126 to 130 there are abrupt changes in the sec tional area, falls in the sur face when the area decreases, and perhaps rises where it increases (chap in arts 18 and 19). In Figs 124 and 125 the weir for mula gives the discharge

having reference to the surface above the local full which therefore need not be considered in the other cases there are no abrupt changes in section and therefore no local \_\_\_\_n

changes in level
A change of one
I ind may be com
bined with another
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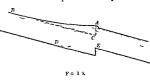
sed for instance the changes of roughness may be accompanied by changes in slope so that the water level in the locer reach is at C and the flow is uniform but any

fow is uniform but any local fulls or rises due to all rupt change of section (I igs 126 to 170) all remain. The rises are generally however negligible, and the fulls are much reduced if the changes are not actually sud len (chap in art 17).

In all cases whatever the upstream level has to accommodate strell to the downstream level. The vater level in the lower reach or nond or on the crost of the full is known or can be accordant. He local fall or rise, if any, must be found and there will be leader to up or drawing down or neither in the reach above according as

the level found is above or below or equal to the natural level in that reach When the variable flow extends upstream to a point where

there is another break in uniform ity the flow in the reach is said to be 'variable through out If the bed of the reach is level or slopes upward (Figs 135 and 136



p 240) the flow must be variable throughout however long the reach may be and the surface convey



upward In a uniform chan nel let CD (Fig. 131) be a 'flume of the same section as the rest of the channel but of smoother ma terral If the flume

Actually it will be CGL GL being a curve of drawing down The height DG will generally be very small and no appreciable change in the velo city will be caused

extended upstream for enough the water surface would be CGH

but if surface slope observations are made a serious error may occur if the upstream point of obser " vation falls at M The slope required is ECDL that actually observed is E M Often a flume has vertical sides and is of a different section to the rest of the channel If the change is made grad F a 131 ually there may possibly be no inter

ference with the straight line of the water surface the smaller

sectional area and hydraulic radius of the flume compensating for its smoother material. But this is not hill ely to be the case exectif if the change of section is abrupt there will be a change in the water level at the entrance of the flume. In the Roorl ee Hydraulic Experiments observations were made in a misonry aqueduct good feet long in the Ganges Canal. The surface slope instead of being observed within the aqueduct, was obtained from points lying far outside it in the either channel and the results of the experiments so far as concerns the relation between slope and velocity in masonry channels were visited.

6 Bifurcations and Junctions —A bifurcation or junction may cause variable flow upstream of it. At a junction let  $O_i$  and  $O_i$  be the discharges of the two tributaries. The flow in the main stream is uniform, and its water level is that corresponding to the discharge  $O_i + O_i$ . If the conditions of the debouchure of either tributary are such as to cause any local fall or rise the amount of this must be estimated and the water level in the tributary just above the junction is then known. There will be heading up or drawing-down or neither in the tributary, according as its natural water level is below or above or equal to that so found. There may be heading up in one tributary and drawing down in the other

At a bifurcation let Q be the discharge of the main stream. The flow in the branches is uniform. Assume discharges  $O_1$  and  $Q_2$ , for them— $Q_1+Q_2$  being equal to  $Q_2$ —and find their water levels. Allow for any local fall or rise, and if the water levels upstream of them are equal the assumed discharges  $O_1$  and  $O_2$  are correct, and the water level found is that of the main stream. If they are not equal to is necessary to after the quantities  $O_1$  and  $O_2$  are and make a second trial. In the main stream there will be heading up or drawing down or neither, according as the water level found is higher or lower than, or equal to its instural water level. If a stream flows out of a reservoir the flow will be uniform down stream of the fall in the surface (chap is at 15) which occurs at the head. If more than two streams meet or separate at one place the discharges  $Q_1$ ,  $Q_2$ , etc., must be considered, and the above processes adopted. The variable flow caused by a junction of bifurcation may be counteracted wholly or partly by any other cause, just as in the other instances of variable flow.

In a paper on the designing of trapezoidal notches at canal fills it has been observed that a distributary usually takes off a short

<sup>1</sup> Transictions Society of I gi sers 15% I jil Irrigitio I raich I yer No -

distance above a fall, and that though the not; in must obviously be able to pass the whole discharge when the distributary is closed, it has to be settled in each case whether the design of the notch should be such as to cause draw when the distributary is open or heading up when it is closed. The question must occur with every distributary, and not only with those taking off above falls. If the canal is designed so as to give uniform flow with the distributary closed, then there must be draw when it is open. If there is uniform flow when the distributary is open, there must be heading up when it is closed. The best arrangement depends on engineering considerations which need not be discussed here

The opening of an escape or branch may cause scouring upstream of it. One method of freeing the upper reach of a canal from silt is to make an escape from a point some distance below its head leading back to the river. If there is a weir across the river the slope of the escape may be great. By opening the escape scour is caused in the canal, but this may cause some deposit in the canal downstream of the escape, unless it can be shut off when the escape is opened.

There were once to be seen in a large canal two gauges, one just above and the other just below the off take of an escape channel. It was stated that the two gauges had been erected in order that, by noting the difference of their readings, the quantity of water passing down the escape could be estimated. Both gauges were carefully read, and copies of the readings sent to various efficials. But when the escape was opened the water level on the upper gauge fell practically as much as that on the lower one. Both gauges always read the same. The assistant in charge put up a temporary gauge half a mile upstream. This also fell when the escape was opened. The proper arrangement in such a case is to have one gauge in the canal below the escape and one in the escape. Again, some irrigators who wanted a new water course were anxious that its off take should be placed just above and not just below the off take of an evisting water course. Practically it made no difference whether it was above or below Theore was no sudden fall in the water level of the canal. If a branch whose discharge is to be g is to be supplied from a channel whose discharge is to be yis to be supplied from a channel whose discharge is to be when its discharge is Q-q and then to design the branch so that it will obtain a discharge g with the water level thus found

7 Effect of Change in the Discharge -An increase or decrease of

the discharge is always accompanied by a rise or fall of the water level throughout every reach except at the points A (Figs 122 and 123), where the stream enters or leaves a river or pond whose water level is not affected by the alteration of discharge. It is clear, however, that for a given change of discharge the changes in the water levels at two distant points may be very different from one mother In changes of slope, roughness, width, or bed level, a change in the discharge causes no change in the character of the flow, that is, there is always heading up or draw, whichever there was at first. In a local contraction there is always heading up and also with a drowned weir if there is no fall in the bed In the other cases (change of bed level, werrs debouchures) there will be heading up if the supply falls low enough, and drawing down if it rises high enough (See also chap iv arts 12, 15, and 17)

At a bifurcation, if the branches are such that the flow in the main stream is uniform with the average discharge, and if the beds of all three channels are at one level, the flow in the main stream will probably be nearly uniform with all discharges. At a junction a similar rule obtains only if the discharges of the tributaries vary in the same proportion

Above a weir or a rise in the bed the water approaches the line DF (Figs 124 and 128) as the discharge is reduced, the tendency to silt increases, supposing the water to be silt laden, and deposit will doubtless occur if the discharge falls low enough A fall in the bed (Fig 129) is converted into a clear 'fall' (Fig 79, p 99) at low supply, and in that case there will probably be scour or 'cutting back' owing to the high velocity

8 Effects of Alterations in a Channel - When a natural or artificial change occurs in a channel, such as deepening, widening, silting, the erection or removal of a structure, or the manipulation of a gate or sluice, the consequent change of water level may exte

the the depth at the head of the channel remains constant, it is surface slope afters, and with it the discharge, or a change m the channel may cause an alteration in the quantity of water lost by exaporation, percolation, or flooding, and so affect the discharge But if the discharge of the channel is unaltered, the effect on the water level and velocity caused by any change in the channel is wholly upstream. The building for instance, of a wer in a stream ordinarily causes little difference to persons further down the stream as long as water is not permanently diverted

In a discussion on some oblique were creeted in the Severn it is implied that the were caused a lowering of the flood level and a deepening upstream. Above the were basins had been made by widening the channel, and the widening might, by itself, have caused some slight reduction in the flood level, but not when a werr was added. It was not contended that the flood discharge at the were was reduced. The water level at D (Fig. 130) would therefore be the same as it was originally, and since there must always be some fall from A to D, the flood level at A must have been raised. No deepening due to the were could occur except close alongside a very oblique weir. (See also chap in at 18)

close alongside a very oblique weir (See also chap iv art 18)
Upstream of a place where changes occur a gauge reading affords no proper indication of the discharge, and a discharge table, if it can be made at all, must be one of double entry, showing the discharge as depending not only on the gauge reading, but on other conditions. If gates or shutters are worked there may be any number of water surfaces corresponding to one discharge. An instance of this has already been given in the case of the flow upstream of an escape. Gauges are sometimes fixed in canals near their heads, and tables are made showing the discharges as depending on the gauge reading. The deposit of sit in the heads alters the discharges, vituates the tables, and destroys the utility of statistics biased on the discharges obtained from them. Gauges ought to be placed below the reaches in which the deposits occur. The deposit of sit changes both the section and the slope, and it is next to impossible to allow for it by merely observing the depth at the gauge.

Sometimes shoals or masses of silt travel down a stream. On the Western Junna Canal there is a gauge at Jhind and unother about twenty miles unstream. When the upper gauge is kept steady that at Jhind sometimes slowly fluctuates in a curious manner, although no water is drawn off in the intervening reaches This has been ascribed to travelling masses of silt, and no other

explanation presents itself

If a channel AB (Fg 119) is drawn from a source whose water level is not affected, and if, near the head of the channel, a branch BC is taken off, the discharge of the channel below B may be very little affected A very slight lowering of the water level at B increases the slope AB, and causes more water to be drawn in The water level in the channel may rise slightly at L (chap is at 20) A case occurred in which an engineer, wishing to

<sup>1</sup> Minutes of Proceedings, Institution of Civil Engineers vol 1x

reduce the supply in an overcharged canal, caused a breach to be made in the bank a short distance below its off take from the new surprised to find, that although a large volume of water passed out of the breach, there was no appreciable diminution of the canal discharge below the breach. In the case of an inrigation distributary which takes out of a canal and has itself a number of water courses taking out of it not far from its head, the discharge of the distributary may partly depend on whether the water courses are open or not (Cf case of branched water man, chap y art, 3)

Let a straight cut be made across a bend in a uniform stream. The slope in the cut is increased and the longitudinal section is as



and the longitudinal section is as in Tig 132. If the discharge is in Rig 132. If the discharge is in altered the water lovel at B is as before, and there is ten dency to scour at A and to sit at B. The bed and water surface tend to assume the positions shown by the dotted

lines, and the probability of this occurring must be considered in making a cut If it is desired to keep the water lovel at A the same as before, the cut AB must be made smaller than the original channel, but the velocity in it will be greater, and there will therefore be a still greater tendency to scour. If the abandoned loop is left open the velocity in it will be greatly reduced, owing to the lower water level at A, and at B will be further reduced by heading up. It generally silts up

To increase the discharge of a channel ABC (Fig. 136, p. 240), supposed to be of shallow section, without enlarging it through out, the plan involving least work is to alter the bed to DB. As D recedes from A the discharge increases, but so does the tendency to silt. (Cf. chap 1) art 2)

9 Effect of a Weir or Raised Bed —The tendency to silting common to all cases of heading up, may be somewhat enhanced in the case of a rise in the hed or a weir extending across a channel, because of the obstruction offered to rolling material. This however does not seem to be very great. The silt may form a long slope against the weir, and material may be rolled up the slope Usually even this slope is not formed. Probably the eddies stir up the silt, and it is carried over

The deposit occurring upstream of a rise or a weir less caused it to be supposed that there is a layer of still water upstream of and

below the level of the crest. This idea is absolutely untenable The general velocity undoubtedly decreases as the rise or weir is approached This is due to the increasing section of the stream If the water below DI (Figs 124 and 128) were still the section would be decreasing. The same amount of heading up might be caused by obstructions of other forms, but it has been shown, (art 4) not only that the water upstream of them is moving, but that upstream of the eddies not even the distribution of the veloci ties is affected. The same is no doubt true of a rise or weir. If in a silt-bearing stream the water near the bed were still, there would be a rapid deposit of silt as there is in a short hollow or recess But the contrary often happens In some of the large canals in India the bed upstream of bridges has been scoured for miles, to a depth of perhaps two feet below the masonry floors of the bridges which are left standing up, and forming, in fact, submerged weirs This alone shows the preposterous nature of the still water theory

The idea might have been supposed to be exploded, but for a somewhat recent case. In a paper on the Irrawaddy 1 it is stated that, if the discharges for the water levels A, C, etc (Fig. 133), are plotted, the discharge seems to become zero at L, which is level with a sand bar four miles down stream, although the depth LG was 34 feet, and that 'this dead area of cross section lying below the level of the bar regulating the discharge, exists on almost all rivers' It is



natural that the discharge should become zero at L As the water level falls the effect of the obstruction at F increases (art 7), and the surface slope becomes flatter If the water level ever fell to L the surface would be horizontal and the discharge zero But the reduction of the discharge to zero is due to the flattening of the slope, and not to a portion of the section of the stream being still If it were still it could never have been scoured out, or being in existence it would quickly silt up

'Profile walls' are sometimes built across a channel at intervals They are useful for showing the correct form of the cross section. but will not prevent scour, unless built extremely close together A single wall built at a point where the bed slope becomes steeper will not prevent scour If scour does occur, walls or weirs will of course stop it eventually

<sup>1</sup> Vanutes of Proceedings, Institution of Civil L gineers, vol. cxiii,

In clearing the silt from a cinal it is often convenient to make the level of the cleared bed coincide with the level of a masoniy bridge floor, but it is not a fact that any deeper clearance is use less. The deeper bed gives an increased discharge for the same water level, and there is not necessarily a deposit of silt upstram of the raised floor. Similarly, there is no particular harm in omitting the clearance in any reach where, the depth of the deposit being small, say half a foot, it is troublesome to clear it

## Section III -Variable Flow in a Uniform Channel

## (Formulæ and Analysis)

Therefore  $L = \frac{C^2 R(D_1 - D_2 + h_1)}{V^2 - (AB)^2}$  (74),

where  $C_i$ ,  $R_i$  and V have values stated to the me in section between the two points The quantity  $h_i$  is nearly always small compared to  $(D_1 - D_2)$ . In heading up  $(D_1 - D_2)$  and  $(V - C^*R^2)$  are negative, so that in equation 71 both numerator and denominator in negative. In drawing down the above quantities are positive

To find the surface slope S at any point, consider a point midway between the two sections, and suppose them very near together, so that the changes are very small. Let  $V_1 - V_2 = r$ , then  $V_1^* - V_2^* = \left(V + \frac{v}{2}\right)^3 - \left(V - \frac{v}{2}\right)^3 = 2V_1$  and equation 17

becomes 
$$h = \frac{I^{*}I_{-}}{I^{*}I_{-}} = \frac{I^{*}I_{-}}{I_{-}}$$
 (75)

Let I be the sectional area and I, the surface width at the midway point. Let a be the difference in area in the length I. Then  $Q = I^* I = \binom{I' + \frac{1}{2}}{2!} \binom{I - \frac{a}{2}}{2!} = I^* I + \frac{1}{2} I - \frac{I^* a}{2!} \binom{a}{4!}$ .

neglecting the very small last term, r l= l a or i= al

Therefore from equation 75,  $h = \frac{l^2L}{c_1l} - \frac{l^2a}{c_2l}$ But  $a=L(D_1-D_1)$ and if d is the mean depth in the cross section, A = Id

Therefore 
$$h = \frac{l^{-1}L}{c^{-1}L} - \frac{l^{-}}{g} \cdot \frac{D_1 - D_1}{d} = \frac{l^{-1}L}{c^{-1}L} - \frac{l^{-}}{g!}(I, S - h)$$
  
or  $h(1 - \frac{l^{-}}{dl}) = L(\frac{l^{-}}{l^{-}}L - \frac{l^{-}}{g!})$ 

Therefore 
$$S = \frac{\hbar}{L} = \frac{I^{*}}{\epsilon L} \frac{1 - \frac{CLS}{qL}}{1 - \frac{V^{*}}{\epsilon}}$$
 (76)

The difference between the bed slope and the surface slope is

$$S \sim S = \frac{S\left(1 - \frac{I^{**}}{gI}\right) - I^{**}\left(\frac{1}{C^{**}I_{*}} - \frac{S}{gI}\right)}{1 - \frac{I}{gI}} = \frac{S - \frac{I^{**}}{C^{**}I_{*}}}{1 - \frac{I}{gI}}$$
(77)

The fraction by which  $I^{rs}$  is multiplied in equation 76 is the ratio of the surface slope to what it would be in a uniform stream with the same velocity and hydraulic radius. This friction may

be written  $\frac{1-\frac{I^{n_1}}{qd}}{1-\frac{I^{n_2}}{qd}}$  where  $I^n$  is the velocity in a uniform

stream with the same values of C and R but with a slope equal to the bed slope For ordinary depths and velocities the nume rator is not much less than unity. In cases of heading up the denominator is still nearer unity, but in drawing down less so

In a stream of shallow section R is nearly as d and V is as  $\frac{1}{2}$ , so

that, neglecting the above fraction S is for moderate changes in depth roughly as 1 In order that the slope obtained by

observing the water levels at the ends of a reach may agree with the local slope at the centre of the reach, the sectional areas of the stream at the two ends of the reach must not differ, in ordinary cases, by more than 10 or 12 per cent

Equation 76 establishes a direct connection between the depth at any cross section and the surface slope at that section, but not the connection between the depth or slope at any section and the position of the section To find this, the profile must be worked out in short reaches (restricted as above as to length) by equa

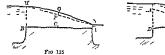
tion 74, or by a method which will be given below

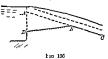
To find the length of a tangent from any point K (Figs 122 and 123, p 229) to N, where it meets the line of natural water surface Let D be the depth at K and D the natural depth Let GN=x, GD=y Then y=xS and y+D-D=xS

Therefore D-D=x(S-S)

 $x = \frac{D - D'}{S - S} = (D - D) \frac{1 - \frac{V^2}{g l}}{S - \frac{V^2}{S}}$ and (78)

When the bed is level or slopes upward (Figs 135 and 136)





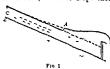
S' in equations 74 and 76 is zero or negative In the former case

(79)

and

 $S = \frac{V}{CR} \left( \frac{1}{1 - V} \right)$  (80)

11 Standing Wave -If a stream has a high velocity relatively to the depth of water in it V" may be greater than gl I et heading up occur in such a stream, so that V' becomes less than gd Then the curve of heading up does not extend back till it touches the natural water surface, but ends abruptly at a point I (Fig. 137) At this point  $I^n = gd$ , the denominator in equation 76 is zero, and the slope therefore infinite, that is, the water



surface is vertical, or a standing wave occurs In order that the velocity may be sufficiently high, relatively to the depth, to pro duce a standing wave, the slope must be steep or the channel smooth It is not necessary that

there should be any variable flow except it the wave. The flow in both the upstream and downstream reaches may be uniform. Instances may I so n where a steep wooden trough tails into a pond or downstream of a sloping weir or contracted water way. One occurs where the Amazon suddenly changes its slope. The quantity  $\frac{V_1^* - V_2^*}{2g}$  in equation 17 is greater than, and of opposite sign to the quantity,  $\frac{V_1^* L}{c^* R}$ . In order that  $V^*$  or  $C^* RS$  may be greater than gd, S must be greater than  $\frac{g}{\ell_R}$  assuming R and d to be equal If C is 100, S must be more than 0032.

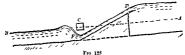
At the foot of a rapid forming the left flank of the weir across the river Ravi at the head of the Bari Doab Canal the standing wave, when floods are passing, is 6 or 8 feet high, not counting the masses of broken water on the crest of the wave Logs 6 feet in diameter brought down by the flood disappear into the wave.

The following statement shows some results observed by Bidone -

(1)	(2) (3) (5)		(5)	(6)	(7)	(8)	
Di	D.	1,	1,	$\frac{1_1^2 - V_2^2}{2g}$	D2 - D1	Difference of C lun ns 5 and 6	(1 1 - 1 1)2 2g
Feet. 149	Feet '423	4 59	1 62	287	Feet 274	013	137
246	739	6-28	2 09	545	493	052	273

Column 7 shows (chap 11 art 1) the head lost. This is small and is nothing like (Y<sub>1</sub> - Y<sub>2</sub>)<sup>2</sup> (chap 11 art 18), but it is much greater for the second case for the first. It appears that for very small streams where perhaps there is no foam or broken water, the loss of head is slight, and the height of the wave may be calculated, but it does not seem possible to do this accurately in large streams, the loss of head being probably great.

Let AB (Fig. 138) be a stream, and let it be desired to lower



. 10 1

the water level at L, say in order that floating logs or rafts may clear a structure C, or in order to allow of a drainage outfall into

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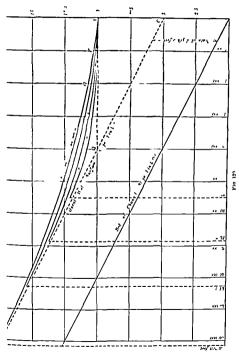
the stream The object can be to some extent attained by heading up the stream and introducing a ripid DE. It is concentable that some practical application of this principle might occur (Of case of constricted pipe, chap i art 7).

12 The Surface curve—In any given channel with a given

discharge there is only one curve of heading up and one of drawing down, whatever the cause of the variable flow may be If the cause operating at A (Figs 122 and 123) be removed and another cause introduced say at K, making the water level at A as before, the curve BK is the same as before. The water in the reach BK is only concerned with accommodating itself to the water level at K, and not with the question how that water not have to be found again for any lesser change of water lovel, but only a part of the same curve used Theoretically the curve extends to an infinite distance upstream, approaching indefinitely near to the line BC, which is an asymptote of the curve Practi cally the curve extends to a limited distance beyond which no change in the natural water surface is perceptible. The less the ratio of AD to AF the greater is the relative length of the curve LA If the discharge of the channel is altered, the curve is entirely changed, and no part of it is the same as any part of the original curve. If the natural water level is higher than before, a change of the same amount as before will cause a smaller ratio of AD to KI, and therefore a longer curve. The greater the relative irra of that part of the cross section of a stream which lies over the side slopes of the channel, the more rapidly does the section change with change of witer level the more, therefore, does the surface slope at K differ from the natural slope and the less the length of the curve. The length of the curve is of course le s the steeper the bed slope

13 Method of finding Surface curve — To obviate the tedious process of working out length by length, and obtain a direct approximation to the surface curve, one or two methods have been used. An old rule, given by Neville for cases of heading up is that the total length of the curve LK (1 g 122 p 229) is 1 5 to 1 9 times the length of the horizontal line A W. This is only an approximation, or rather guess of the very roughest kind and it gives no idea of the form of the curve, that is of the depths at intermediate points. For an imaginary case in which the led width is infinite, the sides vertical, and the coefficient (constant for all depths, an equation to the curve can be found by integration.

It is far too complicated for practical u.e., but certain tables have been based on it. Such tables, owing to the wholly imaginary condi-



tions of the case, are of very limited use. For channels with vertical sides they are not accurate, for others not even fairly accurate

Fig 139 shows four curves worled out length by length by equation 74 (p 238) for streams 5 feet deep with a slope of 1 in 4000, the co efficient C being about 60 when the depth is 5 feet For other depths the co efficient is suitably increased. The curves all tend to become straight lines as the depth increases. This is owing to the minuteness of the surface slope at great depths. The fall in GF has a great relative difference to the fall in FA, but both are so small that the divergence of the curve from a strught line is sometimes imperceptible. The curves are drawn up to a depth of 10 feet in one direction and 5 125 feet in the other Below this depth the curve again tends to become strught. The three uppermost curves are for channels of rectangular section The uppermost curve represents the extreme hmit possible the bed being assumed of width zero, or, what is the same thing assumed to be quite smooth the sides being only taken into account in calculating R, which is therefore constant. In the second curve J increases from 2 50 feet to 3 33 feet. The third curve is for a channel of infinite width but it is not the imaginary curve mentioned above, because the co efficient C has been increased as D increases, instead of being constant As D increases from 5 to 10 feet I also increases from 5 to 10 feet. In channels with sloping sides increase of depth is accompanied by a rapid increase of section and of R and C The profiles curve more rapidly, and the points where the curves become strught are sooner reached The lowest curve is for a triangular section (bed width zero) and represents the extreme limit possible. For greater lid widths the teffect of the side slopes becomes less and vanishes when the led width is infinite. The third curve therefore represents the other limit in this case. The surface slopes at I are, for the four curves in the state of the slope at I are, for the slope at I ar

 $\frac{1}{1} \text{ rom equation } \frac{1}{1} \text{ (p. 238)} \\
\frac{1}{L} = (r_1(D_1 - D_2 + h_2) - \frac{S}{D_1 - D_2 + h_2}) \tag{81}$ 

I et  $x = \frac{D - D_1}{D}$ , then x is the length in which the led level changes by  $(D_1 - D_1)$  feet and I is the length in which the depth changes by  $(D_1 - D_1)$  feet. If the ratio  $\frac{x}{I}$  is known L can be easily found

by  $(B_1 - B_1)$  feet. If the ratio  $\frac{1}{I}$  is known L can be easily  $\frac{1}{I}$ . This ratio, for each of the above curves (e) the  $m_1$  which is not no led) and for some  $m_1$ .

approximately in table he for a rate

2D, the value of  $(D_i - D_i)$  being usually  $\frac{D_i}{D^i}$  which gives reaches sufficiently short to enable equation 74 or 81 to apply without any considerable error. The approximate ratios  $\frac{\tau}{L}$  are easily found by disregarding  $h_r$ . Then, putting  $C^*RS = I^{r_i}$ , from equation 81,  $\frac{z'}{L} = \frac{D_i - D_i}{L_i} = \frac{I^{r_i}}{I^{r_i}} = 1$  (82)

This quantity, since  $D_i > D_i$ , is negative, and in table if the quantity  $1 - \frac{V^i}{V^i}$  is shown instead

Now the ratios  $\frac{z}{L}$  in table in apply, not only to the cases from which they were deduced, but with certain corrections to most other cases. Let the size, roughness, or bed slope of the stream later in any manner, the proportions of the stream being mun tained, and the proportionate change in C with change of R being also maintained, and let  $\frac{D_1 - D_2}{|T|}$  be as before, then  $\frac{T^2}{|T|}$  and  $\frac{T}{L}$  are as before. Thus the ratios in table in can be used, with suitable interpolations, for any channel whose section is rectingular or trapezoidal. For a curvilinear or irregular section the section most resembling it can be adopted. For most cases the above approximation will be sufficient, but greater exactness can be obtained as follows.

Denoting by  $C_1$  the value of C for the natural depth D, and  $C_2$  the value for the headed up depth 2D, column 14 of table it shows the ratios  $\frac{C_2}{C_1}$ or M, which actually occurred in the cases worked out These ratios are fair averages, being such as occur with streams 5 feet to 10 feet deep with N about 0275, but for other cases the ratio may be different. For a very smooth deep stream it will be less and for a rough shallow stream more For values of R (in the reach of natural flow) ranging from 2 feet to 8 feet, an l N ranging from 017 to 030 the value of M (Kutter and Bazin) may possibly vary as shown in columns 15 and 16 For any given stream it will be difficult to say what the value is and the extreme values shown are not likely to occur Suppose that, for the second case shown in table li , it is  $M = \frac{116}{110}$ 100) and  $\frac{1l'^2}{ll} = 111$  nearly beheved that M is 1 16 Then Corrections can be applied as follows -

 $\begin{array}{c} \text{Corrections} \left\{ \begin{array}{lllll} & \text{Column of table ii} & \text{S} & & & \text{11} & \text{12} & \text{13} \\ & \text{In } CP \text{ or } V^{-2}(+) \text{ say}, & \text{1} & \text{2}, & & \text{9} & \text{10} & \text{11} \text{ per cent.} \\ & \text{In } V^{-1} V^{-2}(-) \text{ say}, & \text{1} & \text{1} & \text{2}, & & \text{2} & \text{2} & \text{2} \text{ per cent.} \\ & \text{In } V^{-1}$ 

The correction to be applied to  $\frac{x}{L}$  is + or according as  $\frac{M}{M}$  is > 1.0 cr < 1.0

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tions of the case, are of very limited use. For channels with vertical sides they are not accurate, for others not even fairly accurate

Fig 139 shows four curves worked out length by length by equation 74 (p. 238), for streams 5 feet deep with a slope of 1 in 4000, the co efficient C being about 60 when the depth is 5 feet For other depths the co efficient is suitably increased. The curves all tend to become straight lines as the depth increases. This is owing to the minuteness of the surface slope at great depths. The fall in GF has a great relative difference to the fall in FA but both are so small that the divergence of the curve from a straight line is sometimes imperceptible. The curves are drawn up to a depth of 10 feet in one direction and 5 125 feet in the other Below this depth the curve again tends to become straight. The three uppermost curves are for channels of rectangular section The uppermost curve represents the extreme limit possible, the bed being assumed of width zero, or, what is the same thing, assumed i to be quite smooth, the sides being only taken into account in calculating R which is therefore constant. In the second curve P increases from 250 feet to 333 feet. The third curve is for a channel of infinite width, but it is not the imaginary curve mentioned above, because the co efficient C has been increased as D increases, instead of being constant As D increases from 5 to 10 feet R also increases from 5 to 10 feet. In channels with sloping sides increase of depth is accompanied by a rapid increase of section and of R and C The profiles curve more rapidly, and the points where the curves become straight are sooner reached The lowest curve is for a triangular section (bed width zero), and effect of the side slopes becomes less and vanishes when the bed width is infinite The third curve, therefore, represents the other limit in this case The surface slopes at A are, for the four curves,  $\frac{1}{16\cdot 95}$ ,  $\frac{1}{24\cdot 451}$ ,  $\frac{1}{9\cdot 25}$  and  $\frac{1}{26\cdot 35}$ , the last being only  $\frac{1}{4}$ , th of the slope at L

From equation 74 (p 238),
$$\frac{1}{L} = \frac{V}{CR(D_1 - D_2 + h_1)} - \frac{S}{D_1 - D_2 + h_0}$$
(81)

Let  $x = \frac{D_1 - D_2}{S}$ , then x is the length in which the bed level changes by (D1-D2) feet, and L is the length in which the depth changes by  $(D_1 - D_2)$  feet If the ratio  $\frac{x}{L}$  is known L can be easily found

This ratio, for each of the above curves (except the uppermost, which is not needed) and for some intermediate cases, is given approximately in table li for a range of depth extending up to

2H, the value of  $(D_1 + D_1)$  being usually  $\frac{D^2}{10}$ , which gives reaches sufficiently short to enable equation 74 or 91 to apply without any convolerable error. The approximate ratios  $\frac{T}{L}$  are easily found by disregarding  $I_T$ . Then, putting  $(T^2 \times 1)^{-n}$ , from equation 81,

This quantity, since  $D_1 > D_{11} = \frac{D_1}{L} = \frac{D_2}{L} = \frac{D_3}{L} = \frac{D_$ 

quantity  $1 - \frac{I^{-1}}{I}$  is shown instead

Now the ratios  $\frac{x}{L}$  in table li-apple, not only to the cases from which they were deduced, but with certain corrections to most other cases. Let the size, roughness, or hed slope of the stream alter in any manner, the proportions of the stream being main tained, and the proportionate change in C with change of R being also maintained, and let  $\frac{D_1-D_1}{L'}$  be as before, then  $\frac{T}{l}$  and  $\frac{T}{L}$  are as before. Thus the ratios in table li-can be used, with suitable interpolations, for any channel whose section is rectangular or trapezoidal. For a curvilinear or irregular section the section most resembling it can be adopted. For most cases the above approximation will be sufficient, but greater exactness can be obtained as follows.

Denoting by  $C_1$  the value of C for the natural depth D, and  $C_2$  the value for the headed up depth 2D', column 14 of table it shows the ratios  $C_1$  or M, which actually occurre 1 in the cases worked out. These ratios are fair alout 0.755, but for other cases the ratio may be different. For a very smooth deep atternant will be less, and for a rough shallow stream more. For values of R (in the reach of natural flow) ranging from 2 fect to 8 feet, and N ranging from 0.71 to 0.30 the value of M (butter and Bann) may possibly vary as shown in columns 15 and 16. For any given stream it will be difficult to say what the value is, and the extreme values shown are not likely to occur. Suppose that, for the second case shown in table h, it is believed that M is 1.16. Then  $\frac{M}{M} = \frac{1}{100}$  1000 and  $\frac{M'}{M} = 1$  11 nearly. Corrections can be applied as follows.

Corrections In Graphica as found in the second of the sec

The correction to be applied to  $\frac{x}{L}$  is + or according as  $\frac{M}{M}$  is > 1.0 cr < 1.0

For trapezoidal channels table  $\ln$  gives the ratio  $\frac{A_1}{A_2}$ , but the channels concerned had side slopes of 4 to 3. For other side slopes the increase of I even with the same value of  $\frac{A_2}{A_2}$ , may differ somewhat, but the difference is likely to be considerable only for a deep narrow channel. In any case a correction can be made, as above, by considering the change in  $\frac{C_1^2}{G_1^2}$  instead of  $\frac{C_1^2}{G_1^2}$ . The actual values of  $R_1$  and  $R_2$  were is follows—

Section ratio	-	Infinity	3	75	0.0
$R_1$	=	50	3 64	2 69	20
$rac{R_2}{R_2}$	=	10 0	6 25	4 78	40
<u>R.</u>	=	2.0	1.72	1.78	2.0

Regarding the hitherto neglected quantity h, the following table shows such values of it as have been worked out for the above cases

Except with

VALUES OF h.

Dept! s of Water	_							
	1							
Section   loc ts   ta   to   ta   ta   ta   ta   ta   ta	to 9	9 to 95	9 3 to 10					
table 1 ) is 5 feet Values of D <sub>1</sub> D	Values of D <sub>1</sub> D							
170 75 5 5 5 5 5 5	5	5	5					
( 2   6 0   025   046   074   058   046   036   030   026	021	018	01 ;					
(a) 4 173 006 005 0025		0014	0013					
E Infin tr 2 12 003 006 009 007 0046			002					
3 1 81 008 006 0023								
8 75 1 6 007 0015		001						
£ 0 0 2 68 013 023 015 018 007 000 004			0016					

high velocities  $h_*$  is small compared to  $(D_1 - D_2)$ . For a smaller channel  $(D_1 - D)$  will be less, but probabily I' and  $h_*$  will also be less. By interpolating and noting that  $h_*$  is as 1' the values of  $h_*$  for any case can be approximately obtained and  $\frac{x}{L}$  corrected by multiplying it by  $D_1 - D_2 + D_1$ , which since  $D_2 > D_1$  is greater than unity, so that the correc

tion increases  $\frac{x}{L}$ 

Ordinarily the corrections have little effect, because D changes less rapidly than  $\frac{d}{L}$ . Suppose the ratio  $\frac{d}{L}$  used is wrong by 4 per

cent, then instead of giving the point where D is, say, 1 30, it gives the point where D is 1 28 or 1 32

The profile can be easily extended with accuracy to a point where the depth is greater than 2D by simply calculating the surface slopes at the two ends of the extension and drawing two straight lines or even one

Table in shows some co efficients  $\frac{z'}{L}$  for cases of drawing down extending to half the natural depth As with the curves of heading up the greatest change of slope and the shortest curve occurs with a channel of tringular section Fig. 140 shows one of the

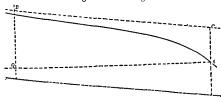


Fig 140.

curves. The channels are the same as before, but the natural depth D is now 10 feet, so that column 1 is not as before, and  $D_1 - D_2$  in  $\frac{I'}{20}$ .

 $C_1$  now refers to the depth D and  $C_2$  to the depth  $\frac{D}{2}$ . The correction to be applied to  $\frac{x^n}{L}$  for change in M is, as before, + or according as  $\frac{M}{16}$  is > 1 0 or < 10, but it is greater than before in relative amount. The values of  $\frac{R_1}{L}$  for the trapezoilal channels are the same as it evalues of  $\frac{P_1}{L}$  given above. The correction for h, is the same as before and as before has the effect of increasing  $\frac{x^n}{L}$ .

Where D is not much less thin D the surface curve is very similar to that of heading up, with similar proportionate depths, but as D decreases the resemblance ceases, and the curvature increases rapidly, a tangent to the curve tending to eventually become vertical instead of horizontal, as in heading up

The ratios in tables h and hi have been arranged in the form

IIN DPAIRLICS

For trapezoidal channels table h gives the ratio  $\frac{A_b}{A_s}$ , but the channels concerned had side slopes of 4 to 3 For other side slopes the increase of R even with the same value of  $\frac{A_S}{A_s}$  may differ somewhat, but the difference is likely to be considerable only for a deep narrow channel. In any case a correction can be made, as above, by considering the change in  $C_i^{\frac{1}{2}} h_1$  instead of in  $C_i^{\frac{1}{2}}$ . The actual values of  $R_i$  and  $R_s$  were as follows —

<i>U</i> <sub>1</sub>			
Section ratio = Infinity	3	75	0.0
$R_1 = 50$	3 64	2 69	20
$R_2 = 100$	6 25	4 78	40
$\frac{R}{D}$ = 2.0	1 72	1 78	20

Regarding the hitherto neglected quantity he, the following table shows such values of it as have been worked out for the above cases Except with

VALUES OF h.

				Depti s of Water										
Sect on Ratio (see	Ve loc ty where depth	51 2 to 5 %	5 25 to 5 5	5 5 to 6	6 to 6.5	6 a to	7 to 75	to	s to 8 \$	8 5 to 9	9 to 95	9 J to 10		
taù	le l ).	1s 5 feet								of D <sub>1</sub> D				
			100	*5	5	,	5	5	5		5	5	5	
보 (	2	60	02ა	046	074	0,9	046	036	030	026	021	-018	01,	
ಒ	4	1 73			006	000			002ა		j ,	0014	0013	
Fef.	Iifi ty	2 12	003	006	009	007		0046					002	
∃ (	3	1 81			008	006				0023				
ezo dal	73	1 ა6			007					0015		001		
Ē(	00	2 68		013	023	015	oís	007	00ა	004			0016	

high velocities  $h_t$  is small compared to  $(D_1-D_2)$  For a smaller channel  $(D_1-D)$  will be less, but probably I and  $h_t$  will also be less. By interpolating and noting that  $h_t$  is as I the values of  $h_t$  for any case cut be approximately obtained and  $\frac{x}{L}$  corrected by multiplying it by  $\frac{D_1-D_1}{D_1-D_2+h_s}$ , which, since  $D_2>D_1$  is greater than unity, so that the correct tion increases 7

Ordinarily the corrections have little effect, because D changes less rapidly than  $\frac{r}{L}$  Suppose the ratio  $\frac{r'}{L}$  used as wrong by 4 per cent, then instead of giving the point where D is, say, 1 30, it gives the point where D is I 28 or I 32

The profile can be easily extended with accuracy to a point where the depth is greater than 2D' by simply calculating the surface slopes at the two ends of the extension and drawing two straight lines or even one

Table lit shows some co-efficients  $\frac{x^2}{I}$  for cases of drawing down extending to half the natural depth As with the curves of heading up the greatest change of slope and the shortest curve occurs with a channel of triangular section Fig. 140 shows one of the



FIG 140.

curves The channels are the same as before, but the natural depth D' is now 10 feet, so that column 1 is not as before, and  $D_1 - D_2$ 18  $\frac{D'}{20}$ 

 $C_1$  now refers to the depth D and  $C_2$  to the depth  $\frac{D}{2}$ . The correction to be applied to  $\frac{x''}{L}$  for change in M is, as before, + or - according as  $\frac{M}{M}$ is > 10 or < 10, but it is greater than before in relative amount. The values of  $\frac{R_1}{D}$  for the trapezoidal channels are the same as the values of  $\frac{R_2}{P}$  given above The correction for h, is the same as before, and, as before, has the effect of increasing  $\frac{x^*}{r}$ 

Where D is not much less than D the surface curve is very similar to that of heading up, with similar proportionate depths, but as D decreases the resemblance ceases, and the curvature increases rapidly, a tangent to the curve tending to eventually become vertical instead of horizontal, as in heading up

The ratios in tables h and hi have been arranged in the form

For trapezoidal channels table  $\ln$  gives the ratio  $\frac{A_1}{A_2}$  but the channels concerned had sade slopes of 4 to 3. For other side slopes the increase of R even with the same value of  $\frac{A_2}{A_2}$ , may differ somewhat, but the difference is likely to be considerable only for a deep narrow channel. In any case a correction can be made, as above, by considering the change in  $\frac{G_2}{G_1}P_1$  instead of  $\ln \frac{G_2}{G_2}$ . The actual values of  $R_1$  and  $R_2$  were as follows —

C <sub>1</sub>	or my	and mere as	20,10
Section ratio = Infinity	3	75	0.0
$R_1 = 50$	3 64	2 69	20
$R_2 = 100$	6 25	4 78	40
$\frac{R}{R_2}$ = 20	1 72	1 78	20

Regarding the hitherto neglected quantity h, the following table shows such values of it as have been worked out for the above cases. Except with

VALUES OF h

				Dept! s of Water										
1	section Ratio (see	Ve loc ty v he r depti	5 125 to 5 °5	5 23 to 5 5	5 5 to 6	6 to 6 5	6 5 to 7	7 to 75	to 8	8 to 8 5	to 9	to 9 5	9 . to 10	
ta	ble li )	15 5 feet	Values of D <sub>1</sub> D.											
			195	25	5	5	5	5	5		5	5	5	
	( 2	60	025	046	074	058	046	036	030	026	021	-018	01-	
8	4	1 73			006	005			0025	}		100	0013	
Rectn	Infinity	2 12	003	006	009	007		0046		ļ			002	
2	(3	1 81			008	006				0023				
Try ezoidal	75	1 26			007		۱			0015		001		
12	00	2 68	-	013	023	01.	018	007	000	004			0016	

high velocities  $h_i$  is small compared to  $(D_1 - D)$ . For a smaller channel  $(D_1 - D)$  will be less but probabily I' and  $h_i$  will also be less. By later polating, and noting that  $h_i$  is as I' the values of  $h_i$  for any case can be approximately obtained and I' corrected by multiplying it by  $D_1 - D_1$ , which since  $D_2 > D_1$ , is greater than unity, so that the correction increases I'.

Ordinarily the corrections have little effect, because D changes less rapidly than  $\frac{r}{L}$ . Suppose the ratio  $\frac{r'}{L}$  used is wrong by 4 per

discharge will be a maximum, BM being given, let BM=D and NA=y. The section CQ is nearly as  $\frac{D+y}{2}$ ,  $\sqrt{L}$  as  $\sqrt{\frac{D+y}{2}}$ , and  $\sqrt{S}$  as  $\sqrt{\frac{D-y}{L}}$ . Then assuming C constant, Q is nearly as  $(D+y)(D^1-y^i)^3$ ,

 $dQ = \text{constant} \times \{(D^1 - y)^{\frac{1}{2}} - y(D + y)(D^1 - y^2)^{\frac{1}{2}}\},$   $= \text{constant} \times \{(D^1 - y^1 - Dy - y^1)\}$  = D = 3D

When the expression in brackets is zero  $y + \frac{D}{4} = \pm \frac{3D}{4}$ 

The discharge is a maximum when  $y=\frac{D}{2}$  and a minimum when y=D. The discharge, however, varies little for a considerable variation in y. In the case just referred to, when D was 8 feet, the discharges found were, C being constant,

y=1 ft 2 ft 3 ft 4 ft 5 ft 6 ft Q= 249 253 255 259 240 229

Similar interesting problems occur on Inundation Canals, though, owing to the temporry nature of the conditions, approximate solutions are sufficient. When the head reach of a canal is sitted and the time is approaching when the canal, owing to the falling of the river, will go dry, a reserve head channel is often opened Sometimes the first one is also left open. Whether it should be left open or not depends on what extra supply it will give (when the water level at the junction is raised by the opening of the reserve head) and on whether the slope in it will be so flat as to cause it to sit excessively. If only one head is to be open it is sometimes better to keep the reserve head closed, as the slope along it may be flat owing to the conditions in the shifting river

On the Choa branch of the Sirhind Can'l the water four miles from the head, was headed up in order to work a mill, and the variable flow extended up to the head, thus vitating the discharge table which depended on the reading of the head gauge. The use of the table was abandoned, but it would be possible to correct it on the above principles, a gauge above the mill being also read The case of a silted canal head (art 8) is different because the bed is constantly changing

### SECTION IV -VARIABLE FLOW IN GENERAL

15 Flow in a Variable Channel —Sections 11 and 111 of this chapter treat of uniform channels but though the propositions

given so as to admit of corrections being applied, or at least to show how the corrections affect them. Otherwise it would be

more convenient to show  $\frac{L}{\lambda}$  instead of  $\frac{x}{L}$  It is, however, easy

to convert the figures It is clear that the total length of a curve (say of heading up and starting from the point where  $D_1$  is  $1\ 025D$ ) is relatively very great when the heading up is small, and that co efficients showing its total length would require a table as large as table li, and similarly with drawing down

14 Calculations of Discharges and Water levels - When the flow in a reach is not variable throughout, the discharge can be found from the depth-or vice versu-in its upper portion, and thus V is known Then, the depth at the lower end, or at any point in the variable length, being also known, the surface curve can be

found by the method of the preceding article

When the flow is variable throughout a reach, such as Ah (Figs 122 and 123, p 229), supposing a breach in uniformity to occur at K, an approximate discharge can be found by the formula for uniform flow, the slope being KA and the depth being greater or less than the mean of the two depths at K and A, according as draw or heading up exists. The reach can then he divided into a few lengths, or left undivided (according as the relative difference in the two depths at K and A is great or small) and a nearer approximation made by using equation 74 If the depths at K and A are very different the channel can be assumed to extend up to B and table h or he used In any case the correct discharge is obtained when, the water level at one end being assumed, that at the other end comes out correct

Whether or not the flow is variable throughout the reach, if the discharge is so great as to affect the original water level at the head of the reach, allowance must be made for this in assuming the

water level at B or K

A case occurred 1 in which a cut, BA, with a level bed (Fig. 135, p 240) connected two rivers. It was desired to ascertain how much water would flow along the cut The writer of the article worked out the discharge from first principles by the aid of the calculus, the working occupying several pages This case, as well as that shown in Fig 136, can be dealt with as above, except that, D being infinite, tables h and hi cannot be used, and that for the level bed equation 79 (which is simpler) is to be used instead of 74 To find approximately the depth AN (Fig 135) for which the

Minutes of Proceedings Institution of Civil Injuneers vol lin

descharge will be a maximum, I M being given, let BM=D and MA=v. The section CQ is nearly as  $\frac{D+v}{2}$ ,  $\sqrt{L}$  as  $\sqrt{\frac{D+v}{2}}$ , and  $\sqrt{S}$  as  $\sqrt{\frac{D-v}{L}}$ . Then assuming C constant, Q is nearly as  $(D+v)(D^*-v^*)^{\frac{1}{4}}$ .

When the expression in I rickets is zero  $v + \frac{D}{4} = \pm \frac{3D}{4}$ 

The discharge is a maximum when  $y=\frac{D}{2}$  and a minimum when y=D. The discharge, however, varies little for a consideral le variation in y. In the case just referred to, when D was 8 feet, the discharges found were, C being constant,

y=1 ft 2 ft 3 ft 4 ft 5 ft 6 ft Q=249 253 255 259 240 229

Similar interesting profilems occur on Inundation Carals, though, owing to the temporary nature of the conditions, approximate solutions are sufficient. When the head reach of a canal is silted and the time is approaching when the canal, owing to the falling of the river, will go dri, a reserve head channel is often opened Sometimes the first one is also left open. Whether it should be left open or not depends on what extra supply it will give (when the water level at the junction is raised by the opening of the reserve head) and on whether the slope in it will be so flat as to cause it to silt excessively. If only one head is to be open it is sometimes better to keep the reserve head closed, as the slope along it may be flat owing to the conditions in the shifting river.

On the Choa branch of the Sirhund Can-il the water, four miles from the head, was headed up to the head, thus vitrating the discharge table which depended on the reading of the head gauge. The use of the table was abandoned, but it would be possible to correct it on the above principles a gauge above the mill being also read. The case of a silted canal head (art. 8) is different because the bed is constantly changing.

#### SECTION IV -- VARIABLE FLOW IN GENERAL

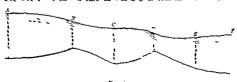
15 Flow in a Variable Channel -Sections 11 and 111 of this chapter treat of uniform channels, but though the propositions

are more early taken and prove or manage course there and will remain in constitute ville will read in the total -ares or manus comments in the first for the first fir and 'the time of the hard of these manners in a virial's carrel to the violation and the state of the are remark the national enteriors and it for total "-v" is taken it all LEFERINGE IN BEATH WE HE TO BE SHOWN IN A PUBLIC. intime in a vent in maker a train creme, as rise dovo THE C LE ALERTON L'IL NAME L'ACTURE VINCHA .. TO seriled in arti. a 5 martie contact headmoon or one wind CIVIL TO LOT MAT COM STATE SALE CLIST RESTREE to COV material.

Garratte a variante carrel in acres v. o .. 2 .. a va e fare. - a. Per one Came car ca c ared. One problem E to use we come a waterland me a mil to proved b a mante de une comercal. The court war of finding the war of -man essent to the course of a course to at a larger in ea ho we a de som a le ealer en em color varue un ore direct mane to make and mil (" . The halfer arough It the countries of the countries of the and Tan ma et e a canco o lovel au ant tun will of en exosibancer thoses raw

The sing we as asset as a same of the main To (- 23 ) ... 1 - E. al- h- \_ e. \_ = F= P. T. w-- e S b he wrater a diant seried poin to B be the widh of the wall of the wall of mean control. Then much!

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a fil affichance in a came manner on the process to bot not the It is all a man the be opened in a " In which a total are emiscoc area r 11/11/1



The surface slopes at opposite banks of a stream are not generally equal unless it is quite uniform and straight

17 Rivers—A river, especially at low water, may be a series of separate streams with numerous junctions and bifurcations. The water level in a side channel CAL (Fig. 142) may afford only



wery poor indication of the general water level in the river. Suppose that with a good supply the water level at A is the same as that at B. If there is silt in the channel CA—the silt being deepest at C—a moderate decrease of the river discharge may cause a great decrease in the discharge of CA, or even a total cessation of discharge. This causes great difficulties in the matter of gauge readings in some Indian rivers. Suppose a gauge to have been originally at B. If erosion of the balk sets in the gauge has to be moved, and sometimes it is difficultied.

to find another place (free from practical difficulties in the matter of reading the gauge and despatch of readings), except at such a place as A in a side channel. In floods, especially when the sandbanks between the channels are submerged, there is a general tendency for the water surface to become level across, but it by no means follows that it becomes so. When the deep stream is at one side of the river channel the flood level is nearly always higher on that side than at the opposite side.

Since a small cross section tends to cruse scour and a large one silting, it follows that every stream tends to become uniform in section. The remarks made in articles 1, 2, and 8 also show that it tends to destroy obstructions, to assume a constant slope, and to become curved in such a way that its velocity will suit the soil through which it flows. If a river always discharged a constant volume its regimen would profably be permanent. It is the fluctuations in the discharge that cruse disturbance.

#### EXMPLES

Example 1—In the channel considered in example 3 of chapter is a heading up of 1.25 ft is caused by a weir. What heading up is caused 2000 feet upstream of the weir?

Table Alv shows l = 102.6 sq ft Also  $A_b = 80 \times 4.75 = 380$  sq ft  $A_s = 22.6$  sq ft and  $\frac{f_b}{I_s} = 17$  nearly, so that  $\frac{f'}{I}$  hes between the values for the first and second cases in the second part of table h, and somewhat nearer to the first than the second

Since  $S = \frac{1}{5000}$  and  $D_i - D_i = \frac{D}{10} = 475$  ft  $z' = \frac{D_i - D_i}{S} = 475 \times 5000 = 2375$  ft

The headed up depth at the weir is 6 ft = 4.75 × 1.264 From table h  $\frac{\pi}{L}$  is about 550 when  $D_1$  is 1.2D and  $D_2$  is 1.3D'. Therefore  $L = \frac{\pi'}{550} = \frac{2375}{550} = 4318$  ft The distance of the weir downstream from the point where the depth is 1.20D' is  $\frac{1.264 - 1.200}{1.30 - 1.20} \times 4318 = 2764$  ft. The point 2000 ft upstream of the weir is thus 764 ft from the above point, and the change of depth in this length is  $(1.30 - 1.20)D' \times \frac{318}{150} = 018D$ , so that the heading up is (1.218 - 100)D', or  $218 \times 475$  ft, or 1.04 ft Corrections if applied to this case might after the result by 0.1 ft

Example 2—From the stream considered in the first trial in example 2 of chapter vi a branch is taken off and discharges 120 c ft per second What lowering of the water level is caused 1500 ft upstream of the branch?

 $A_s=56.3$  sq ft and  $\frac{A_b}{A}=5.32$ , so that  $\frac{x^*}{L}$  has between the

Table also shows A=3563 Also  $A_b=40\times75=300$  sq ft

values in the first two lines of the second part of table lii. The discharge below the bifurcation is 957 c. ft., and this is given by a depth of 7 ft., so that the lowering is 5 ft. Since  $S'' = \frac{1}{5000}$  and  $D_1 - D_2 = \frac{1}{20} = 375$  ft.  $r^2 = \frac{D}{5^{\prime\prime}} - \frac{D_1}{5^{\prime\prime}} = 375 \times 5000 = 1875$  ft. The drawn-down depth at the bifurcation is 7 ft = 75 × 93 ft. From table lii.  $\frac{z'}{L}$  is about 33, when  $D_1$  is 90D. Therefore  $L = \frac{z'}{33} = \frac{1875}{33} = 5682$  ft. The distance of the bifurcation downstream from the point where the depth is 95D is  $\frac{95-93}{95-90} \times 5682 = 1894$  ft. The point 1500 ft upstream of the werr is thus 394 ft from the above point, and the change of depth in this length is  $(95-90)D \times \frac{394}{56} = \frac{1}{2} \times \frac{1$ 

TABLE LI —RATIOS FOR CALCULATING PROFILE OF SUFFACE
WHEN HEADED UP (Art. 13)

		WHEN HI	ADED	or (	(AIL	13)					
(1)	(2)	(3) (4) (5)	(6) (7)	(8) (9	) (10) (1	1) (12)	(13)	(14)	(15)	(16)	
Section Ratio	Ratos	Depth Rat o	Upperf	gures sl	ow Di lo	wer figu	res D	Val 1es	of V	or (2)	
		to to to 1 05 1 10 1 05 1 10	1 °0 1 30 to to 1 30 1 40	1 40 1 5 to to 1 50 1 to	0 1 0 1	0 1 80 to 1 0 1	1 90 to 20	Actual 1 cl oc rrel	Fxt: Val Mari	es	
I ectang tlar Sections Rato of Wilth to Deptl as in column 1											
2 {	$\frac{x}{L^{\text{orl}-\{1-1^{n}\}}}$	003 500 65° 004, 180 318	45" 55"	62º 6S	733 7	71 901	,, <sub>o</sub> }	1 07			
1 {	I -I zer1-(I -I"	°9 804 6 9 108 196 341	510 410 181 581	661 (2	0 766 7	01 1 1 00 S20	14°} %51}	1 10	1 16	1-03	
In finity {	$\frac{1-1}{\frac{\tau'}{L}} \text{or } 1-(1-1)^2$	850 014 120 223 386	458 3 1 549 649	74 718	8 175 1 2 825 S'	43 118 7 892	001}	1 17	1:28	10	
Traje or lig Sections Ratio 1/4 = ur nof section overled, as medium 1											
In he its	(TI for	r sare tle su	ne as for	tle pre e	ling ca	se )		1 17	1 28	0	
3 {	$\frac{1-1^{-2}}{L}$ or $1-(1-1)$	136 240 100						1 13	1-21	01	
7.s {	1 -1  x'or1-(1 -1-)	54" -30 543 153 270 457	3 0 <i>a</i> 630 731	194 146 806 851	10° 0 501 01°	036 9	19}	1 11	21 1 	01	
0.0 {	1 :-1 "2 x' or1 - {1"2-1"2}		2 19 70° 80°					15 1	_S 1	0.	

# TABLE LII —RATIOS FOR CALCULATING PROFILE OF SURFACE WHEN DRAWN DOWN

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
Section Ratio	1.3 and 1.7-1 1.3 Latio	Depth Ratios $ \text{Lp}_{1} \text{erfigures show } \frac{D_{1}}{D} \text{ lower figures } \frac{D}{D'} $							Values of Wor C1				
		-05 to	-ng to 85	85 t 1	SO to	~5 te 70	ro to	65 to	60 to	55 to	Actual which	Ext	
		-90	85	*80	<sup>5</sup>	70	-65	60	55	50	curred	Maxi mum	Mini mum
Rectangular Sections Ratio of Width to Depth as in column 1													
1 {	$r_2 - r_2$ $\frac{x}{L}$ or $1^2 - r_2 - 1$	21	39	İ	90	i	i	s ss 2 33	4 14 3 14	5 31 4 31	935	89	98
2 {	1,- 1,-1	1-04 24	ı		1 .		1	3 -2 2 72	4 °C 3 76	6-24 5 24	909	40	97
In huity {	$\frac{1}{2}$ or $\frac{1}{2}$ or $\frac{1}{2}$ or $\frac{1}{2}$	1 31			ı			5 07 4 07	l 1		} 8.s	78	9.
Trape_oidal Section: Ratio $\frac{A_b}{A_c}$ = area of section over hed $A_b$ as in column 1													
In finity	(The figures	are t	he sa	ıme a	s for	the	] rec	eding	case )		95	78	۹,
15{	1"2_1"2 <u>x</u> " or 1"'-1 '2-1	1 34 34			1	1	i	5 00		11·35 10 35	1 88	۹3	ю
375 {	z or 12-1 , 1	1	i	1		1	1	684	l		} <8	83	-n <sub>ry</sub>
00{	1"21"2 2 or 1 -1"2-1	1 57	1		3 93	1	1	10-94			81	78	าร

## CHAPTER VIII

### HYDRAULIC OBSERVATIONS

[For general remarks on Hydraulic Observations, see chap in art 25]

# SECTION I -GENERAL METHODS

1 Velocities —When the velocity is observed at one or more points in the cross section of a stream, the process is termed 'Point Measurement' When the mean velocity on a line in the plane of the cross section is found directly, it is known as an 'Integrated Measurement' Velocity measuring instruments are of two classes, namely, 'Floats' and 'Fixed Instruments' Fixed Instruments give the velocities in one cross section of a stream 'Ploats give the average velocity in the 'run' or length over which they are timed, and not that at one cross section. Floats are used only in open streams, but fixed instruments sometimes in pipes.

With most instruments time observations are necessary. The best instrument for this is a chronometer betting half seconds, similar to those used at sea, or a stop-watch which can be read to quarter seconds. The next best is a common pendulum swinging in half seconds, and after that an ordinary witch. The error in timing with a chronometer is not likely to exceed half a second, with an ordinary witch it may be one or even two seconds. Some stop-watches and watches not only do not keep proper time, but are not regular in their speed. If any such defect is suspected the instrument should be tested. The time over which an observation extends should be such that any error in timing will be relatively small. In order to climinate the 'personal equation' of the observer similar observations at the beginning and end of the time should be performed by the same individual, or if performed by two they should frequently change places.

Floats include surface floats, sub-surface floats, and rod floats. The first two are used for point measurement, the last for integrated measurements on vertical lines. A float travels with the stream, and so interferts little with the natural motion of the

water. Its relocity is supposed to be the same as that of the water which it displaces

Fixed Instruments are divided into Current Meters and Pressure Instruments In the former the velocity of the stream is inferred from that of a revolving screw, in the latter from indications caused directly by the pressure of the water 1 Velocities cannot be obtained by Fixed Instruments until they have been 'Rated.' that is, until it has been ascertained that certain indications of the instrument correspond to certain velocities. Fixed instruments interfere with the natural motion of the stream, but this need not cause error The disturbance is almost entirely do vistream of an obstruction (chap is art 21), and if those parts of the instrument which are intended to receive the effect of the current are kept well upstream, no difficulty arises, except perhaps in very small streams If a boat is used the bow can be kept pointing upstream and the instrument upstream of the bow, a platform being made to project over the bow. Even if the boat or instrument is so large (which is not likely) relatively to the stream as to cause a general heading up, this will not prevent a correct measurement of the discharge, though it may affect the surface slope. In order that disturbance may not be caused by moorings the boat should (unless it is a steam launch which can maintain its position) be held by shore lines If attached by its bow to a pulley running on a trans verse rope, it can quickly be brought, by using the rudder, to any required point Another transverse rope serves to keep the boat steady and, if divided by marks, shows its position. In a wide stream containing shallows the ropes may rest on trestles placed Where moorings must be used it is best to moor at the shallows two boats side by side, as far apart as practicable, and to work from a platform between them, keeping the instrument well upstream

The choice of an instrument for velocity measurement depends on various considerations. Floats require a regular stream, but fixed instruments can be used in any stream. In comparing the Current-Victer, or Pitots Tube with Floats, regard must be had to the design and quality of the instituments available, and to the manner in which they were rated. Sub surface floats are unsuit

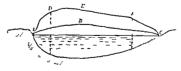
<sup>&</sup>lt;sup>1</sup> Further infermation concerning, Excel Instruments is given in Sections is and v, but the varieties and details are very numerous in leannot all be discussed. There are many papers on these instruments in the Minutes of Proceedings of the Institution of Civil Engineers and Iranvarious of the American Society of Civil Engineers.

able when the stream is rapid or when there are weeds growing in it, fixed instruments unsuitable when the velocity is very low For surface velocities alone surface floats are, in regular streams, the best instruments unless there is considerable wind. For integrated measurements the rod float is as good as any instrument, provided the bed is even enough to allow of a rod of the proper length being used.

The above considerations refer to accuracy only. As regards the time occupied and the number of observers required, fixed instruments generally have the advantage. In a dicharge measurement of a large river current meter integration measure ments can be made while the soundings across the channel are being taken. On the other hand, the time occupied in rating the fixed instruments, their initial cost, and their liability to damage or loss, especially in out-of the way places, may be very important frictors. If a stream is too wide to be reached at all points without a boat, has no suitable bridge, but is still narrow enough for the floats to be thrown in from the sides, and if no soundings are required, float observations may take less time than others.

2 Discharges—The discharge of an aperture or pipe is not usually found by measuring the velocity but by letting the water pass into a tank and measuring the volume added in a given time 1 Whenever leakage, absorption, or evaporation occur, allowance must be made for them, but some error is likely to result

The discharge of an open stream is usually found by observing the depths and mean velocities on a number of verticals. Let ABC (Fig. 143) be the mean velocity curve, and ADEFC a curve



Fic 16

whose ordinates are found by multiplying the depth on each vertical by the corresponding velocity. Then IDIF( is the dis

<sup>1</sup> The velocities in large pipes may however be beenvel (art 14). When this is done it is best to divide the section into the reentrie circles found areas.

charge curve, and its area is the discharge. If floats are used the velocities obtained are the averages in the run, and the depths must also be averages in the run. The more numerous the verticals the more accurate the result. For ordinary work ten is a fair number, for very accurate work, twenty. In the segments of D, EC, near the sides the verticals should be nearer together than elsewhere, because the ordinates change rapidly. The equal spacing of the verticals in each segment is not essential, but it simplifies the calculation, as it is only necessary to add together all the ordinates in a segment—deducting half the first and last—and multiply the sum by the distance between the ordinates. The discharges of all the segments added together gives that of the stream. If the number of equal spaces in a segment is even Simpson's rule can be used, but ordinarily the results of formulæ such as this differ very little from those of the simpler rule.

Sometimes the spacing in a segment cannot be equal. If there is in the cross section any marked angle, whether salient or reentering, a measurement should be made there. Sometimes when floats are used in rivers the velocities must be observed where the floats happen to run. In such cases the depths at these exact points need not be measured, but may be inferred from those observed at fixed intervals or found by plotting the section.

If the mean velocity on a vertical is obtained by multiplying the observed surface velocity by the co efficient  $\beta$  (chap vi art 9), and if  $\beta$  is the same for all verticals, the discharge may be calculated as if the surface velocities were the means on verticals and

the whole discharge multiplied by  $\beta$ 

Discharge observations in an open stream are greatly facilitated by the construction of a 'Flume' A short length of the channel is constructed of masoniy or timber. The sides may be sloping but are preferably vertical. In the absence of silt deposit the section of the stream is known from the water level, and if rod floats are used they are all of one length. Flumes may, however, prevent proper surface slope observations (chap vii art 5). Discharges can be obtained with more or le s exactness by the observation of U or U, and the use of a or  $\delta$  (chap vii art 10), but a flume is often unsuitable for this (chap ii art 21).

When a discharge table has been prepared for any site or aperture, the discharge can be found by simply obering the water level or head or—in the case of a pipe—the hydraulic gradient. The discharge of a pipe may be altered by corrosion,

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and that of an open channel by changes occurring, not only at the site but downstream of it. Honce orifices and wers in thin walls afford the best means of measuring moderate quantities of water. For larger quantities, and for small quantities when no fall is available, measurement in a flume or regular channel is adopted, but the relocities should be observed sometimes, if not in the whole section, then in the centre.

3 Soundings —Soundings are generally taken to obtain a cross section of a stream, but longitudinal sections may be required in order to find the most regular site, or in connection with float observations. In water not more than about 15 feet deep soundings are best tallen with a rod, which may carry a flat shoe to prevent its being driven into the bed. In greater depths a weighted line is used.

Unless the velocity is very low it is best to observe soundings from a boat drifting downstream The current then exerts little force on the rod or line, which can thus be kept vertical. It can be held so as to clear the bed by a small amount, and lowered at the proper moment This plan is particularly suitable for obtain ing the mean cross section in the run when floats are used As the boat drifts the bottom is frequently touched with the rod or line, and the readings booked and averaged. Any local shallow likely to interfere with the use of rod floats is also thus detected When shore lines can be used the boat can be worked and the widths measured as described in article 1. In wide rivers lines of flags or 'range poles' are used instead of ropes. An observer on the boat or on shore can note the moment when the boat crosses the line, and give a signil for the soundings to be taken To determine the distance of the boat from the bank an observer in the boat reads an angle with a sextant, or an observer on shore reads it with a theodolite, following the boat with his instru ment and keeping the cross wires on some part of it. When the line is reached the motion of the instrument is stopped and the angle read off

4 Miscellaneous —The diameters of pipes, while water was flowing, were measured by Williams, Hubbell, and Fenkell by means of a red with a hook mose ted through a stuffing box for obtuning the mean diameter in a length of pipe one method is to fill it with water, which is afterwards measured or weighed. If the joints are not closely filled in some error may be caused, and Smith in some experiments filled eich separate piece of pipe before it was laid, and weighed the water it contained.

For ascertaining c, and c, for orifices special arrangements are required. The velocity of the jet is found by observing its ringe on a horizontal plane. A ring or movable orifice of nearly the size of the section of the jet may be placed so that the jet passes through it the flow stopped and the necessary distances measured. The actual velocity can then be found from equation 29 or 30 (p. 52) and the actual head bein, measured c, is easily found

When observations of any kind are made a suitable form should be prepared and filled in. It should have spaces set apart for recording the date time gauge reading and (at least when floats are used) the direction and force of the wind

#### SICTION II -WATEL LEVELS

5 Gauges -- I r ol erving the water level of an open stream the simplest kind of gauge is a vertical scale fixed in the stream and graduated to tenths of a foot. It may be of enamelled iron. screwed to a wooden post which is driven into the bed or spiked to a masonry work. The zero may conveniently be at the bed level, so that the reading gives the depth of water. The actual gruge may extend only down to low water level. If a gauge is exposed to the current it may be damaged by floating bodies and it is difficult to read it accurately owing to the piling up of the water against the upstream face and the formation of a hollow downstream. These irregularities can be greatly reduced by sharpening the upstream and downstream faces of the jost or the up tream face only Greater accuracy can be obtained by placing the gange in a recess in the bank, but not where it is exposed to the effects of irregularities in the channel (chap vii art 2) and by watching the fluctuations of the water level noting the highest and lowest readings within a period of about half a minute and taking their mean but very great accuracy by direct reading of a fixed gauge is difficult because of the adhesion of the water to the gauge, and the differences in level of the point observed and the eve of the observer

With floating gauges these difficulties are almost got rid of The graduited rod is attached at its lower end to a float which rises and falls with the water level. The rod travels vertucally between guides and it is read by means of a fixed pointer on a level with the eve of the observer. The float and rod should be of metal, so that they may not alter in weight by absorbing moisture, the float perfectly water tight and its top conical so that it may not

form a resting place for solid matter ally be tested by comparison with a fixed gauge or bench mark. For a given weight of float and rod the smaller the horizontal section of the float at the water surface the more sensitive the gauge will be

To reduce the oscillations of the surface a gauge, whether fixed or floating, may be placed in a masonry well communicating with the stream by a narrow vertical sit. It is not certain that the average water level in the well is exactly the same as in the stream, but the difference can only be minute. The larger the well the better the light and the less the oscillation of the water. The advantage of a slit as compared with a number of holes is that it can always be seen whether the communication is open, but in order to avoid the necessity for frequent inspection the oscillation of the water in the well should not be entirely destroyed. In observations made downstream of the head gates of irrigation distributaries in India the oscillations were very violent—amounting to 60 foot—but they were reduced to 03 foot in the well by slits 005 foot wide.

Where a gauge does not exist the water level can be measured from the edge of a wall or other fixed point, either above or below the surface. Owing to the oscillation of the water the end of the measuring rod cannot be held exactly at the mean water level. It should be held against the fixed point, and the mean reading taken is explained above. A self registering gauge can be made by means of a paper band trivelling horizontally and moved by clock work and a pencil moving vertically and actuated by a float. The pencil draws a diagram showing the gauge readings. The water level in a tank may be shown by a graduated glass tube fixed outside the tank and communicating with it.

The level of still water can be observed with extraordinary accuracy by Boyden's Hook Gauge, which consists of a graduated rod with a hook at its lower end. The rod slides in a frame carrying a fixed vernier, and is worked by a slow motion serow. If the hook is submerged, the frame fixed and the rod moved upwards, the point of the hool, before emerging causes a small capillary elevation of the surface. The rod is then depressed till the elevation is just visible. By this means the water level can be read to the thousandth of a foot, and even to one five thousandth in still water, by a skilled observer in certain lights. The hook gauge is not of much use in streams because of the surface oscillation. It is most used in still water upstream of were

To destroy oscillation and ripples, a box having holes in it may be placed in the water and the readings taken in the box When observing with a hook gauge in water not perfectly still the point of the hook should be set so as to be visible half the time A pointed plumb bob hung over the water from a closely graduated steel type is sometimes used, and by it the surface level or the observed to within 005 foot The adjustment of the level of the zero of the gauge above a werr may be effected by a levelling instrument. If effected from the level of the water when just beginning to flow over the crest capillary action may cause some error

6 Piezometers -The name 'Piezometer,' used chiefly for the pressure column of a pipe, is also used to include a gauge well and its accompanying arrangements. In all such cases the surface, where the opening is, should be parallel to the direction of flow and flush with the general boundary of the stream, and the opening should be at right angles. If it is oblique the water level in the piezometer will be raised or depressed according as the opening points upstream or downstream The well or pressure tube can be connected with any convenient point by flexible hose terminating in fixed glass graduated tubes. With high pressures the piezometers may be connected with columns of mercury, which may be surrounded by a water jacket to keep the temperature nearly constant Common pressure gauges are not accurate enou\_h

In the piezometers of pipes air is somewhat hable to accumulate and cause erroneous readings. When the presence of air is suspected the tubes should be allowed to flow freely for a few minutes If flexible they can be shaken and if stiff rapped with a hammer Very small tubes are hable to obstruction by leaves or deposits and should be avoided, as also should glass gauge tubes small enough to be affected by capillarity The orifices should be drilled and made carefully flush Instead of one orifice there may be four, 90° apart, in one cross section of a pipe, all opening into an annular space from which the piezometer tube opens It is not certain that this gives greater exactness but with a single opening from the top of the pipe the accumulation of air is probably greatest. The air probably travels along the pipe at the top

The Venturi meter for pipe observations has been described in chapter 1 (art 7) It has been patented and can be obtained with automatic recording apparatus

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The Venturi meter for pipe observations has been described in chapter v (art 7) It has been patented and can be obtained with automatic recording apparatus

The arrangements at the weirs where the most important observations (chap is art 1) have been made were as below In all cases the surface containing the orifice was parallel to the tire of the stream

Barin —An opening near the bed 4 inches square communicating with a well

Francis -A small box with 1 inch holes in the bottom

Iteley and Steams—For the 19 foot weir there was an opening 04 foot in diameter and 4 feet lower than the crest of the weir From the opening a rubber pipe led to a pail below the weir

For the 5 foot went there was a board parallel to the side of the channel and 15 feet from it. The pipe leading to the pail started from an auger hole in the board 9 feet above the bed of the channel.

To find the heals on wears piezometers connected with perforated tubes placed horizontally in the channel have been used in America, but they appear to give unreliable results, even when the holes open vertically experiments made at Cornell University the 'middle piezometer' was a transperse I inch pipe, laid 8 inches above the bed and 10 feet upstream of the weir The 'upper piczometer' was similar, but 15 feet further upstream \ 'flush piczometer' was also 'set in the bottom of the flume,' 6 inches upstream of the upper prezometer The readings of these two differed on one occasion 1, 3 foot The readings of the upper and the middle also differed It is believed that the opening from the rounded surface of the mpe instead of from a plane surface causes error, and that the error is one of defect A 'longitudinal piezometer' was formed by certain perforated pipes With high heads-a little over 3 feet-the longitudinal piezometer read 099 foot higher than the upper piczometer. With a head of about 17 foot there was no difference between the two Typerments made by Williams also show that the readings obtained with a transferse pipe with holes opening downwards, do not agree with those obtained by a simple opening in the side of the channel being higher with low supplies and lower with higher supplies. It seems clear that all perforated pipe arrangements are to be avoided until their action is better understood

7 Surface-slope —Probably the best method of observing the stope in a short length of open stream is to dig two ditches from the extremities of the slope length, both leading into a well divided into two by a thin partition. The difference between the water levels on the two sides of the partition is the local surface fall. It can be very iccurately measured, especially if the ditches

The box projected somewhat into the stream, and this was not free from election, as it caused an abruit change

Transactions of the American Society of Civil Engineers, vol xliv

<sup>2</sup> Hal vol xliv

are treated as gauge wells, that is, open into the stream by narrow slits This is perhaps the only way by which the slope in a really short length can be found 1 Slight leakage in the partition is probably of no consequence as long as it gives rise to no perceptible current in the ditch. The slope should unless the stream is perfectly uniform and straight, be observed at both banks and the mean taken (chap are art 16)

For measuring the loss of head in a short length of pipe a differential gauge may be used consisting of two parallel glass tubes with a scale fixed between them Capillarity does not vitiate the results because it is the difference that is taken. If the tubes are partly filled with water and the space above the water is occupied by air the difference in the heights of the water columns gives the difference in head To obtain great exectness Williams, Hubbell, and Fenkell used an inverted U tube and substituted kerosene oil for air. This causes the difference in the readings in the two legs to be magnified about five times Another differential gauge used was a simple mercury gauge All these gauges had to be 'calibrated' (their constants determined) and corrections were applied for changes in temperature "

In whatever way slope is observed the openings of any pair of gauge wells, ditches, or piezometers must be exactly similar, and the observations should be repeated at intervals as long as the

velocity observations last

#### SECTION III - FLOATS

8 Floats in general -The size of a float used for point measurement is limited by the consideration that the mean velocity of the stream within the 'direct area' of the float (the area of its projection on a cross section of the stream) must be practically equal to that at the point where the velocity is sought The depth of the submerged part of a surface float may be about one twentieth of the depth of water and the depth of a sub surface float one tenth or, at the point of maximum relocity one twentieth of the depth of water. The width of a float of any kind may be about one twentieth of the width of the stream except for use near the bank, when it may be about one tenth of the distance from the bank to the line of the float. The length is

<sup>1</sup> This method can be used for a pipe provided the lydraulic gradient is at a convenient level

<sup>2</sup> Transactions of the American Society of Civil Ligineers, vol xlvii

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similarly limited because the float may revolve. The exposed part of a surface float should be small compared to the submerged part. For deep water a good surface float is made by a bottle submerged all but the neck, or a log deeply submerged, for shallow water by a disc almost totally submerged and carrying a small cylinder or knob. With all kinds of floats the exposed part should be of such a colour that it can easily be seen

The 'lines' or boundaries of the run are marked by ropes stretched across the stream at right angles, or, if the width is great, by lines of flags. Observers signal each flout as it crosses the lines, and another observer notes the times. When ropes are used the float-courses can be marked by 'pendants' of cloth or brass. Usually about three floats are signalled in rapid succession at the first line and then at the second. If on reaching the second line they have changed order, this affects the individual times recorded, but not the mean. With a stop watch the time observer may also be the float-observer. He can start and stop the watch while noting the float. But in this case each float must complete its course before another can be timed. With a slow current the time observer may also start the floats, and he may even use an ordinary watch. In a wide river the course of a float can be observed by an angular instrument (see art. 3)

A float required to travel in any course usually deviates from it. The deviation increases the distance over which it travels, but this is of no consequence because the object is to obtain the forward velocity (chap 1 art 3). The deviation is of consequence only when the velocities in adjacent parts of the stream differ much from one another, that is, generally, near the banks. In such cases the 'run' of the float can be shortened, the deviation noted, and the mean course adopted. When ropes are used the approximate deviation can be seen by the float-stricter by means of the pendants, especially when the rope is at a low level.

of the pendants, especially when the rope is at a low level. The length over which a float travels, upstream of the run, in order that it may acquire the velocity of the water, is called the 'dead run'. The float may be taken out into the sticum, or thrown in from the bank, or placed in it from a bridge or boat. Throwing in is often practicable with surface floats, and some times with rods. A low level single span bridge is the most suitable arrangement, but if there are piers or abutinents which interfere with the stream they disturb the flow, and a site down stream of them is unsuitable for velocity measurements, at least with floats (chap in art. 21). Liven a boat causes disturbance

downstream. Two small boats or pontoons carrying a platform are better than a large boat

The length of run to be adopted depends on the velocity and uniformity of the stream, the accuracy of the timing, and the distance of the float-course from the bink, this last consideration having reference to deviation. Ordinarily the length may be so fixed that the probable maximum error in timing will be only a small percentage of the time occupied. The length may, however, have to be reduced if the stream is not regular, especially if rods are used. Reduction of the length in order to avoid excessive deviation is most likely to be necessary for observations near the bank, especially with surface floats. The surface currents near the bank set towards the centre of the stream (chap viat 7), so that the tendency to deviation is greater, while the admissible deviation is less. Most observations are made at a distance from the bank, and the rejections for excessive deviation need not generally be numerous. A moderate number of rejections, owing to a long run, does not cause much loss of time, because in order to obtain a particular degree of approximation to the average velocity of the stream the number of floats recorded must be inversely proportional to the length of the run.

9 Sub surface Floats — A float used for measuring the velocity at a given depth below the surface is called a 'double float' A submerged 'lower float' somewhat heavier than water, is suspended by a thin 'cord' from a 'buoy' which moves on the surface In the ordinary kind of double float the buoy is made small, and the velocity of the instrument is assumed to be that of the stream at a depth represented by the length of the cord but it is really different because of the current pressures on the buoy and cord, and the 'lift' of the float due to these pressures There is also 'instability' of the lower float, caused chiefly by the eddies which rise from the bed Any lateral deviation of the lower float adds to the lift, but otherwise is not of consequence, except near the banks The resultant effect of all the faults is a distortion of the velocity curves obtained When the maximum velocity is at the surface (Fig 112, p 166) the buoy and cord accelerate the lower float, and the lift brings it into a part of the stream where the velocity exceeds that at the assumed depth Hence the velocity obtained is always too great and the 'observation curve 'which is shown dotted, lies outside the true curve When the maximum velocity is below the surface the curve is distorted as in Fig 113

A double float is best suited to a slow current. The higher the velocity of the stream the greater the differences among the velocities at different levels and the greater the lift of the lower float the greater also the strength of the eddies and the instability

The defects of the double float cannot be removed, but they can be much reduced by attention to the design. In order that the lower float may be as free as possible from instability, its shape should be such as to afford little hold to upward eddies In order that it may be little affected by the current pressures on the buot and cord, it should afford a good hold to the horizontal current It should therefore consist of vertical plates say of two cutting each other at right angles, with smooth surfaces, and lower edges sharpened The upper edges should not be sharpened Any downward current will then act as a corrective to instability the float tilts much its efficiency is reduced but tilting can be prevented by avoiding a high ratio of width to height, and by making the upper and lower parts respectively of light and heavy materials say wood and lead If the thickness of the plates is uniform the resistance to tilting is a maximum when the heights of the heavy and light portions are inversely as the square roots of the specific gravities of the materials. It is an improvement to remove the central portions of the plates and to substitute for them a hollow vertical cylinder, in the middle of which the cord is attached by a swarel. This causes the pull of the cord, however the float revolves on its vertical axis, to be applied at the point where the average horizontal current pressure acts. The cord should be of the finest wire, and the buoy of light material say hollow metal smooth and spindle shaped the cord leing attached towards one end so as to make the float point in the direction of the resistance

the resistance.

Given the velocity of the stream the force tending to cause instability of the lower float depends on its superficial area. Its stability depends on the ratio of its weight to its superficial area that is on the thickness of the plates. I or all floats of the same shape and materials there is a certain thickness of plate which is the least consistent with stability, and a float should be composed of plates of this thickness in order that the thickness of the corlindoid olime of butto may be small. This thickness of more determined theoretically, but is a matter of judgment and experience. Of any two similar double floats, that which has the larger lower float is the more threem. If the direct areas of the lower floats are as a and a, their weights and the submirged

solution of the broas are as 4 and 1. But the direct areas of the large, if their shapes are similar, are as 4 and 1 or nearly as 25 and 1. The thicknesses and direct areas of the cords are also theoretically as 2 and 1. In both cases the larger instrument has creatly the advantage, and practically, if the lower float is small, it is physically impossible to make the condition enough. The directs one are limited by the considerations set forth above. The larger the stream the greater the admissible size of float.

The following statement shows that the double floats which have been actually used in important experiments have been of had design —

Charrel	0,44042	Crested Deribel	Description of	Ratio c	f D rect	Armas lej th
	0	Rave	Lover Fink.	Lower Fl at.	Cont.	Всоу
Mississipi r	Humphreys and Abbett.	Feet 110	keg with top an I bettom removed.	1-0	1 73	-03
Irrawad ly	Cordon	70	Block of woodloaded with clay	10	73	-06
Ganges Canal	Cunningham.	11	Ball (3 mehes and 15 meh)	1.0	18 72	10

It is obvious that when the lower float was near the bed—or supposed to be near it—the observed velocities must, owing to the very great relative current-actions on the cord, and probably also to instability, have been so much in excess of the truth as to render them mere approximations, the general values found for bed velocities being perhaps about halfway between the real bed velocity and the mean velocity from the surface to the bed. The vertical velocity curves obtained with the above instruments often show marked peculiarities in form, the velocity sometimes seeming to remain constant or even increase as the bed is approached

In the 'twin float the submerged part of the buoy or 'upper float is of the same size, shipe, and roughness as the lower float, and the velocity of the instrument is assumed to be a mean between the stream velocities at the surface and at the level of the lower float. The surface velocity is observed separately and eliminated. This causes a liditional trouble. The best form and size for the lower float are arrived at in the same manner as in the

ordinary double float — The difficulties arising from tilting and instability can be overcome by making the lower float heavy and the upper one light. The current pressure on the cord is less than with the ordinary double float, but its inclination greater — The instrument has been very little used.

Cunningham has proposed a triple float for measuring the mean velocity on a vertical when the depth is too great for rod floats, or the bed too uneven. It has a small buoy and two large submerged floats at depths of 21 and 79 respectively of the full depth, the upper of the two being light and the lower heavy. The instrument is supposed to give the mean of the velocities at these two depths, and this is nearly equal to the mean on the whole vertical. The figures 21 and 79 were arrived at theoretically by Cunningham, and they are the best for general use, the depth of the line of maximum velocity being supposed to be unknown. It would be preferable to use a multiple float with several equidistant submerged floats, the lower ones heavy and the upper ones light, the distance of the lowest from the bed and of the highest from the surface being hiff the distance between two adjoining floats. All these floats are best suited to slow currents.

10 Rod floats —A rod float is a cylinder or prism ballisted so that in still water it floats upright. In flowing water it tilts because of the differences in the velocities of the stream. By using a rod reaching nearly to the bed the mean velocity on the vertical is obtained. Owing to the irregular movements of the water the rod does not move steadily. Both its submerged length and tilt vary. The clearence below the bottom of the rod must be sufficient to prevent the bed being touched. The great advantage of a rod as compared with a multiple float is that there is no uncertainty as regards lift and instability.

uncertainty as regards int and instroning.

Rods are usually made of wood or tin and weighted with lead. A wooden rod is hable to alter in weight from absorption of witer, and it may then become too deeply submerged or sink. A cip means of adjustment. In a rapid stream a wooden rod may have an excessive tilt, and a tin rod is better. It is lighter and early means of adjustment. It is, however, hable to damage and to spring a leak. A rod may sometimes sink, owing to its grounding and being turned over 1's the current. In a rapid stream a wooden rod may be turned over even without grounding. Wooden rods can be more castly made square than of other sections. In any case the section and degree of onghness must be uniform throughout.

For a rod 1 foot long, 1 meh, and for one 10 feet long, 21 mehes are suitable drumeters. Rods are often made up in sets, the lengths increasing by half feet, or for small depths by quarter feet, but this does not give sufficient exactitude, and it often leads to the use of rods much too short. Owing to the unevenness of the bed a rod of the proper theoretical length is usually too long, and the next length is perhaps 10 or 15 per cent shorter. A set of short adjusting pieces to screw on to the tops of the rods should be provided. Rods for use in very deep water are sometimes made in lengths screwed together. It is convenient to have rods divided into feet, beginning from the bottom. If the tilt is likely to be great, allowance can be made for it in selecting the length to be used.

It has been said that a rod, owing to its not reaching down to the slowest part of the stream, must move with a velocity greater than the mean on the whole vertical Cunningham has attempted to show theoretically that the length of a rod must be 945, 927, or 950 of the full depth of water according as the point of maximum velocity is at the surface, at one third depth, or at hild depth. The proof rests on the assumption that the vertical velocity curve is a parabola. It has been shown (chap vi art 9) that it is not a parabola, and that the velocity probably decreases very rapidly close to the bed, and for this last reason it is probable that a rod reaching close to the bed would move too slowly. The proper length of rod cannot be calculated theoretically in the present state of knowledge

A large number of experiments with rod floats were made by Francis. The discharges obtained by rods in a mason; flume of rectangular section with a depth of water of 6 fact to 10 feet were compared with the discharges obtained from a weir in a thin wall, and the following formula was deduced.

$$V = V_r \left( 1.012 - 1.116 \sqrt{\frac{D-l}{D}} \right)$$

when F is the mean velocity on the vertical, F, the rod velocits, d the length of the rod, and D the depth of the stream. According to this formula the correct length of rod so that I and I, may be equal, is 9JD and the errors due to shortness of tells as follows.

The discharges obtained by the weir are behaved to be very nearly correct, and the acceptance of the above figures is recommended. Accepting them, the proper length of a rod is 99 of the full depth, and if the length is only 93 of the full depth the velocity found is 2 per cent in excess. In earther channels a rod of the proper length can hardly ever be used, but allowance can be made for its shortness.

# SECTION IV -- CURPENT METERS

11 General Description -The current meter consists of a screw, resembling that of a ship, and mechanism for recording the number of its revolutions Frequently this mechanism is on the same frame as the screw, and by means of a cord it can be put in and out of gear The reading having been noted the meter is placed in the water, the recording apparatus brought into geni, and, after a measured time, put out of gear and a fresh reading taken The difference in the readings gives the number of revolu tions and this divided by the time gives the number of revolutions per second This again, by the application of a suitable co-efficient determined when the instrument is rated, can be converted into the velocity of the stream The co-efficient depends on the 'ship of the serew, and varies for each instrument and each velocity With many meters the recording apparatus is above water, and there is electric communication between it and the serew meter can then be allowed to run for an indefinite time without laising to read. For each meter there is a minimum velocity I clow which the screw ceases to revolve This may be as low as six feet per minute, but is generally much higher

Sometimes a current-meter is carried on a vertical pivot and provided with a vane. The irregularity of the current causes the instrument to swing about, and so to register the total and not the 'forward' velocity. It is better to keep the instrument fixed with the axis partilled to that of the stream, but if the axis swings through a total angle of 20—10 either way—the velocity reaks tered is only 75 per cent in excess of the forward velocity, and if the total angle is 10°, 7 per cent in excess.

A current meter may be used in a small stream from the lank or from a bridge but generally it is used from a bout. This has already been referred to (art. 1). The rod or chain to which the meter is attached should be graduated. If a right used it

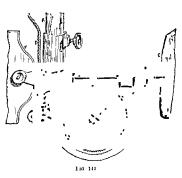
may be sharpened or rounded on its upstream race, the down stream face being flat, and resting against a portion of the platform fixed at right angles to the centre line of the boat. The rod can be provided with a collar, which can be clamped on to it in such a position, that when it rests on the platform the meter is at the depth required. In water 53 feet deep Revy attached the meter to a horizontal iron bar, which was lowered by ropes fastened to its ends, and was kept in position by diagonal ropes. In shallow water un iron rod is sometimes fixed, on which the meter slides up and down, but this causes delay.

In some experiments the time in quarter seconds, position of the meter, and number of revolutions of the screw have been automatically recorded on a band driven by clockwork meter having electric communication with the bank a wire rope has been stretched across a wide stream, the meter carried on a frame slung from the rope and the discharge of the stream thus observed In other cases the observers travel in a cage slung from a wire rope It is quite usual to have several meters work ing simultaneously at different depths. In integration it is not necessary for the descending and ascending velocities to be equal, and two or three up and down movements may be made without raising to read It is a common practice, after taking an observa tion lasting a few minutes, to check it by a shorter one To facilitate the computation of the meter velocity the times may be whole numbers of hundreds of seconds A stop-watch may be started and stopped by the same movement which puts the instru ment in and out of gear

The rate of a current meter is hible, at first, to increase shelity of the bearings working smoother by use. It should be allowed to run for some time before I eng rated. Oil should not be used, as it is gradually removed by the water, and the rate may then alter. Every time a meter is used the screw should be spin round by hand to see that it is working smoothly. A centle breeze sould keep it revolving. A second instrument should be kept at hand for comparison. Occasionally a short to to the riting should be made. If tests made at two or three velocities all show small or proportion to changes of one kind similar cert tions may be applied to other velocities. But if the changes are great or irregular the instrument should be rated africh.

The speed of a current meter is halle to be affected by weed leaves, etc. becoming entangled in the working parts. If any are found when the instrument is read the observation can be rejected.

but some may become entangled and detached again without being seen. The effect must be to reduce the velocity, and any almor mally low result may be rejected. The rate of the instrument is also hable to be affected by silt and grit getting into the working parts and increasing the friction. The only rubbing surface which has a high velocity is the axis of the screw, and this is probably the part chiefly affected. In using a current-meter of the kind illustrated (Fig. 144) it was found on one occasion that it rapidly became stiff. The meter having been cleaned, the screw ran ficely again, but again became stiff. The stream was six feet deep and



had a velocity of about seven feet per second. The water contained silt and probably fine sand, which gradually increased the freeton. The elogging was most rapid in observations I clow middepth, and it is probable that there was more sand in that part of the stream.

12 Varieties of Current-meters.—There are probably twonly hin Is of current meter. I hack hind have its own special advantages or disadvantages. It it is shown a meter sold by Thioti Brothers, I ondon. The instrument is attached by the clamping series to a rod A. By pulling the cord D the wheel I is genred with the series. A sine F can if desired be attached. A meter very similar to the above is made in the Canal workshops at Loorkee,

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India, but it is pivoted on the tube which carries the seres for clamping it to the rod

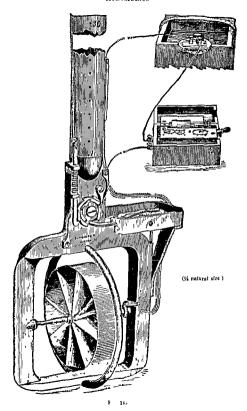
In lieux a current meter friction is reduced by a boll we loss on the axis of the screw of such a size that the weight of the whole is equal to that of the vater displace 1. The re-ording mechanism is enclosed in a box covered by a placy [late, filed with clear water, and communicating by a small let with the water in the stream, so that the place may not be broken 1) the pressure at great depths. All resultable value is a filed under the size, so that they are to be freely which the meter rests on the bar.

More a current meter course of a leave-clinder, 10; inches long, provided with a rew liabs. In front of the cylinder is an ogival head which is fixed to the frame. The cylinder, which is water tight, revolves, and the revoluge a paratius is involved, to the real ling being closted through a pane of gives. The instrument is houng for an cord or chuir. This renders it casier to many abite. To prevent its being free live out of position, a weight is septembed to the frame, and its boil the sufficient to prevent the instrument being it importantly deplaced by the tightening of the gearing on! The instrument is born into an interchon.

In Harlacler's current meter there is electric connection between the worm wheel driven by the screw and a love above water. At every hundred revolutions of the screw the worm wheel makes an electrical contact, and an electromagnet in the box exposes and withdraws a coloured disc. The meter slides on a fixed wooden rod. A tube himz along the rod carries the electric wires, and serves to adjust the meter on the rod. In one variety the axle of the screw carries an eccentric which makes an electric contact every revolution, and thus enables individual revolutions to be noted.

Fig 145 shows a current meter sold by Buff and Berger, Boston, U.S.A. The object of the hand encircling the screw is to protect the blades from accidental changes of form, which would cause a change in the rate of the instrument. A lar underneath the screw and a stout wire running round at a short distance outside it affords additional protection, and enables the instrument to be used close to the bed or sude of a channel. There are two end bearings and a very light screw and axle, and the screw revolves with one fourth of the velocity required to turn a similar one with the usual sleeve bearing. The friction is so small that the rate is not altered by silt or gift. The meter is fixed to a brass tube, which has a line along it to show the direction of the axis when the meter cannot be seen. The meter is sold with the recording apparatus either on the frame or with electric connection, as in the figure. Stearns used a meter of this type, and provided with two screws, either of which could be used. One

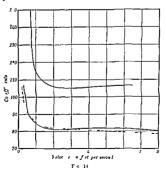
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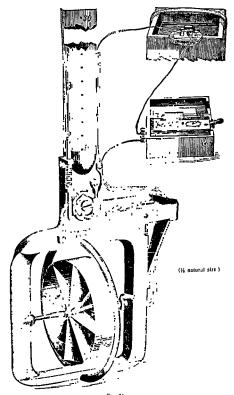
had eight runes and the other ten. In the latter half the vanes had one pitch and the other half a different pitch. The eightnane screw began to more with a velocity of 104, and the ten rune screw with a velocity of 094, feet per second.

One kind of current meter has no regul ir recording apparatus, but simply a device for making and breaking circuit and a sounder. The revolutions are counted by the clicks. A current-meter made by you Wagner gave its indications by sound, but the counting was effected by an arrangement like the seconds hand of a watch. At each stroke, or with high velocities at every fourth stroke, the observer pressed a button which caused the hand to move one division.

13 Rating of Current meters —The usual method of rating is to more the instrument through still water with a uniform velocity, and to repeat the process with other velocities covering a wide range. The instrument may be held at the bow of a boat, or attached to a car running on rails, or on a suspended wire. In case the water should not be quite still the runs should be taken alternately in reverse directions.



When rating a meter the length of run being a fixed quantity, it is only necessary to record for each observation the time occupied and the difference of the meter readings. After several

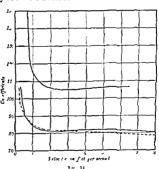


F 17 1 4 34

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Both equations give curves of the same general form, and becoming practically straight lines at high velocities They can never agree exactly with curves having a sag and as the constants cannot be arrived at until some experimental co efficients have been found the equations are not of much practical value

It has been shown by Stearns 1 that rating by ordinary towing through still water is not perfect. In a flowing stream the velocity and direction of the water constantly vary, but in rating this is not so Stearns shows theoretically that the screw turns more rapidly when the velocity varies than when it is constant, that an ordinary screw probably turns more rapidly when the current strikes at an angle than when it is parallel to the axis, but that with his meter (Fig 145) the pand and parts of the frame intercept portions of the oblique currents, and so cause decrease in the number of revolutions, the net result depending chiefly on the design of the instrument He also moved the meter with mean velocities ranging up to 3 7 feet per second through still water, first with an irregularly varying velocity and then with its axis inclined to the direction of motion He found that inclining the axis 8° and 11° had no appreciable effect but that inclinations of 24° and 41° decreased the number of revolu tions about 9 per cent, and that with irregular velocities the number of revolutions was increased, the increase varying from zero to 5 per cent, being generally greater for low veloci ties, and in one case reaching 13 per cent when the mean velocity was only 85 feet per second This velocity was not a very low one when compared with that for which the screw ceased to revolve

By measuring with the same current meter the discharges in a masonry conduit, the depths varying from 15 to 45 feet, and the velocities from 17 to 29 feet per second, and comparing the results with others known to be practically correct, Stearns found that, with point measurement, the discharge given by the meter observations was practically correct, both in the ordinary condition of the stream and when the water was artificially disturbed, and that with integration the discharge was correct when the rate of integration was 5 per cent of the velocity of the stream, but too small by 9 per cent when the rate was 55 per cent of the velocity. In the above experiments both the eight bladed

<sup>1</sup> Transactions of the America i Society of Cir I Li gineers vol xii

Other experiments have shown that it clinations of 20 35° and 4, give a decrease in the number of revolutions of 8 10 and 31 er cent respectively

and ten bladed screws were used, the results being generally sımılar

It seems clear that, with the instrument used, the increase in the velocity due to the variations in the velocity of the stream was counter balanced by the decrease due to oblique currents, and that the instrument gave correct results with point measurements even when the water was disturbed, but with an instrument of different design, and especially one without a band, it seems probable that the results obtained by point measurement err in excess, that no additional error is introduced by a moderate inclination of the axis, or by slow integration, but that rapid integration causes error These, however, are only probabilities. The real lesson to be derived from Stearns's investigations is that rating effected by steady motion in still water may be erroneous when applied to running streams, especially with rapid integration, and that additional tests should be adopted To move a meter obliquely or with an irregular velocity would be troublesome, and would not produce the conditions existing in streams It is best to place the meter in a running stream just below the surface, and to find the velocity by floats submerged to the same depth as the screw blades If a sufficient range of velocities cannot be obtained the meter can be moved upstream or downstream with a known velocity. This plan can be combined with ordinary rating The instrument can also be moved through still water while giving it a movement as in integration A com parison of discharges obtained by the meter, with results known to be correct, affords a further test An immense saving of labour is obviously effected by rating a number of meters together

When it is necessary to rely on ordinary rating rapid integra tion should be avoided The error, if any, will probably be less as the velocity is higher For ordinary velocities the relative error is probably nearly constant, so that the results will be consistent with one another, and sometimes that is all that is required

#### Section V -- Pressure Instruments

14 Pitots Tube -This instrument usually consists of two vertical glass tubes open at the ends placed side by side, one the 'pressure tube,' straight, and one the 'impact tube,' with its lower end bent at right angles and pointing upstream. The water level in the pressure tube is nearly the same as that of the stream

in which the instrument is immersed, but that in the impact tube is higher by a quantity which is equal to  $K \frac{P^2}{2g}$ . Theing the velocity of the stream at the end of the tube, and K a coefficient whose value has to be found by experiment

The chief objections to this instrument were originally the fluctuation of the water level in the tubes, owing to the irregu larity of the velocity, and the difficulty in observing the height of a small column very close to the water surface. Darer in his cause tube reduces the fluctuations by making the diameter of the orifice only 15 millimetres, that of the tube being one centimetre. The horizontal part of the tube tapers towards the point. and this minimises interference with the stream. The difficulty in reading is surmounted by means of a cock near the lower end of the instrument, which can be closed by pulling a cord. The instrument can then be raised and the reading taken. To give strength and to carry the cock, the lower parts of the tubes are of copper and are in one piece. For observations at small depths the heads of the water-columns are in the copper portion of the instrument, where they cannot be seen. To get over this difficulty the tops of the tubes are connected by a leass fixing and a stopcock to a flexible tube terminating in a mouthpiece By sucking the mouthpiece the air pressure in the tubes is reduced, and both columns rise by the amount due to the difference between the atmospheric pressure and that in the tubes, but the difference in the levels of the two columns is unaltered The upper cock being closed and the mouthpiece released, the reading can be taken For reading the instrument a brass scale with verniers is fixed alongside the tubes The instrument is attached to a vertical rod. to which it can be clamped at any height, and it can be turned in a horizontal plane, so that the horizontal part of the impact tube points upstream To get rid of the effect of the fluctuations in the tube several readings, say three maximum and three minimum, can be taken in succession. The co-efficient K is nearly equal to unity, and it does not vary appreciably, if at all, with the velocity

The Pitot tube has been improved by interposing a flexible hose between the nozzles and the gauge. The rod carrying the nozzles is thus more handy and the fluctuations of the water-column can be watched.

In the Detroit pipe experiments mentioned in chapter v (art 4) various developments of the Pitot tube were used The

tubes were inserted in the pipes through stuffing boxes without interfering with the flow. The diameters of the orifices both impact and pressure were usually  $\sqrt{3}$  inch. The tubes were connected by rubber hose 10 feet long to a differential gauge (art 7), where the readings were taken. When the impact tube was made to point at an angle with the axis of the stream the reading decreased. When the angle was a little over  $45^\circ$  negative reading decreased. When the angle was a little over  $45^\circ$  negative readings occurred up to an angle of  $180^\circ$ , the greatest negative reading being for an angle of  $90^\circ$ . In one kind of tube the pressure orifices, instead of opening into the stream, opened into a ring or annular space outside the pipe and connected with the pipe 1) four holes  $\frac{1}{16}$  inch in diameter, but this was not adopted to any considerable extent for use in the experiments

The Pitot tube is well adapted for observations in depths ranging up to 5 or 6 feet. It has the great advantage of requiring no time observations. It has never been used in large bodies of water, but there does not seem to be any reason why it should not be, if suitably constructed and strengthened. It would be exceedingly useful for measuring velocities close to the border.

15 Rating of Pitot Tubes —This was effected by Williams, Hubbell, and Fenkell (a) by moving the tubes through still water with velocities of 63 feet to 70 feet per second, and (?) by placing them in a 2 inch pipe at various points in a cross section and finding V, the mean velocity in the pipe (which varied from 73 foot to 16 feet per second), by weighing the water discharged The average results were as follows —

(Reference Number of Tubes) Co efficients from still water ratings Co efficients from pipe rating,	926 900	No 6 950 810	No 5 509 7 0
Difference,	036	110	109

For the still water rating the plotted curve of the coefficients of tube No 5 was sinuous (the others being strught), and this was attributed to a wave effect. Tube No 5 was the luntest and No 3 was the finest, and should have the highest coefficient. The pipe ratings were accepted, but it does not seem to le proved that they would be correct for any pipe or any velocity. The above coefficients are the means. In the individual rating, experiments the results differed from the means in still water by 10 to 17 per cent, and in the 2 inch pipe by 2 to 8 for cont. In Bruni's experiments the differences in rating in moving with

whose velocity was known were about 4 per cent. With the ring form of instrument the co-efficient differed from that obtained with the same impact tube when used with the ordinary pressure tube. The above figures seem to show that still water ratings are not at all reliable, and also that there are elements in the case that are somewhat doubtful and not thoroughly understood Probably further experience in ratings will place the instrument in a more satisfactory position.

#### 16 Other Pressure Instruments -

In Perrodil's Hydrodynamometer a vertical wire carries at its upper end a horizontal needle and at its lower end a horizontal arm, to the end of which is fixed a vertical disc. The arm is connected with a graduated horizontal circle at the level of the needle. When the arm points down stream the needle points to zero on the circle. The needle is tusted row I by han I till the arm is forced by the torsion of the wire to a position at right angles to the current. The pressure of the water on the disc is proportional to the square of its velocity, and it is proportional to aid measured by the angle of torsion of the wire as given by the position of the needle. The disc oscillates owing to the unsteady motion of the stream, and the graduated circle oscillates with it, but the mean reading can be taken. The instrument has not been much used but it is said to give goo! interferes somewhat with the free movement of any stream in which it is placed.

The Hydrometire Pendalum consists of a weight suspended from a sting. The pressure of the current causes the string to become inclined to it evertical, and the angle of inclination can be read on a graduated are Except for observations near the surface the current pressure on the string must affect the reading. Brunings Tachometer also has an arm and disc, but the pressure of the water, instead of long measured by the torsion of a wire, is measured by a weight carried on the arm of a lever. These two instruments have been little used, and it is not known how far their results can be relief or.

## CHAPTER IX

#### UNSTEADY FLOW

## SECTION I -FLOW FROM ORIFICES

1 Head uniformly varying—Let the head over an orifice during a time t vary from  $H_1$  to  $H_2$  and let the discharge in this time be Q. The mean head or equivalent head H is that which would, if maintained constant during the time t, give the discharge Q. Let the head H vary uniformly, that is, by equal amounts in equal times, as, for instance, in the case of an orifice in the side of an open stream, whose surface is falling or rising at a uniform rate. In this case h=Ct where C is constant. Let  $\mathcal{A}$  be the area of the orifice and  $\varepsilon$  the co-efficient of discharge, which is supposed constant. The discharge in the short time dt under the head h is

$$dQ = ca \sqrt{2gh} dt = ca \sqrt{2gC} t^{\frac{1}{2}} dt$$

The discharge between the times  $T_1$  and  $T_2$  is

$$Q = \int_{Ca}^{T_1} \sqrt{2gU} t^{\frac{1}{2}} dt = \frac{1}{3} ca \sqrt{2gU} (T_1^{\frac{1}{2}} - T_2^{\frac{1}{2}})$$

$$= \frac{c}{3} \cos \sqrt{2g} C \frac{H_1^{\frac{3}{2}} - H_2^{\frac{3}{2}}}{C^{\frac{3}{2}}}$$

Under a fixed head H

$$Q = ca \sqrt{2gII} (T_1 - T_2) = ca \sqrt{2gII} \frac{II_1 - II_2}{C}$$

Equating the two values of Q

$$\sqrt{II} = \sqrt{\frac{II_1^{\frac{3}{2}} - II_2^{\frac{3}{2}}}{II_1 - II_1}}$$
 (83)

If  $H_1=0$ , that is, if the head varies uniformly from  $H_1$  to  $\theta$  or from  $\theta$  to  $H_1$ ,

from 
$$O$$
 to  $H_1$ ,  $/H = \sqrt[3]{/H_1}$  (84), or the equivalent heal is  $\frac{t}{9}H_1$ 

2 Filling or Emptying of Vessels -I et water flow from an

orifice in a prismatic or cylindrical vessel whose horizontal sectional area is A. The discharge in time dt is dQ = A dh = ca  $\sqrt{27h} dt$ 

$$dt = \frac{A}{ca} \frac{dh}{\sqrt{2g} h} = \frac{A}{ca} \frac{h^{-1}}{\sqrt{2g}} \frac{dh}{dh}$$

The time occupied in the fall of the surface from H, to H, is

$$t = \int_{a}^{H_1} \frac{A}{\sqrt{2}q} h^{-\frac{1}{2}} dh = \frac{2}{ca} \frac{A}{\sqrt{2}q} (H_1^{\frac{1}{2}} - H_1^{\frac{1}{2}})$$

Under a fixed bead II'

$$t = \frac{A(H_1 - H_2)}{\epsilon a \sqrt{2\sigma H'}}.$$

Therefore 
$$\sqrt{H} = \frac{H_1 - H_2}{2(H_1^{\frac{1}{2}} - H_2^{\frac{1}{2}})}$$
 (85)

This is useful for can'l locks

If  $H_1=0$ , that is, if the vessel is emptied down to the level of the orifice,

$$\sqrt{H} = \frac{\sqrt{H_1}}{2} \tag{86}$$

The following are the ratios of AH to AH, for certain cases -

a ronouring are the ratio, or \$11 to \$12 to return eases	
For a prism or cylinder,	1
For a sphere,	1
For a hemisphere concave downwards	÷
For a hemisphere concave upwards	Ϋ́Υ
For a cone with apex downwards,	ŧ
For a cope with anor upwords	3.

For a wedge with point downwards
For a wedge with point upwards,

For a wedge with point upwards,

For a vessel whose vertical section is a parabola with

vertex downwards —

When all vertical sections are the same
(Faraboloid of revolution)
When the horizontal sections are rectangles

(Two opposite sides of the vessel rectangles and two parabolas)
In the last case the surface falls at a uniform rate as in the case considered
in art. 1

In all cases the times occupied in emptying the ressels are greater than with a constant head H, in the inverse ratios of the above fractions. If a ressel is filled, through an ordice in its bottom, from a tank in which the water remains level with the top of the ressel, the ratio of  $\sqrt{H}$  to  $\sqrt{H}$ , is the same as for filling the ressel when inverted. Thus for a cylinder, prism or sphere the time for filling is the same as for emptying

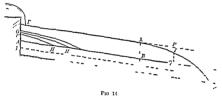
If two prismatic vessels communicate by an orifice, and  $H_1$  is the difference in the water levels of the vessels, and  $A_1$  and  $A_2$  their horizontal areas the time which clapses before the two heads become equal is

$$t = \frac{2 I_1 A_2 \sqrt{H_1}}{\epsilon a \sqrt{2q} (I_1 + A_2)}$$
 (87)

nd is the same whichever is the dischaiging vessel. This equation may be used for double locks

# SECTION II - FLOW IN OPEN CHANNELS

3 Simple Waves —Let ABC (Fig. 147) represent the surface of a uniform stream in steady flow, the reach commencing from a full



over which is introduced an additional steady supply q such that the surface will eventually le LF. A wave is formed below  $A_t$ , the surface assuming successively the forms  $GH_t$  of  $H_t$ , etc. The point H travels downstream at first with a very high velocity—since the slope GH cannot remain steep for any but an extremely short time—but its velocity decreases as the slope at H becomes less. The point G rises at a continually decreasing rise, because in equal times the volumes of water represented by  $GGHH_t$ , etc. are equal. Obviously the velocity of the point H is greater as g is g inter, that is, it depends on the amount of the eventual rise. It must not be supposed that the actual velocity of the site imerical its surface or velocity of 'translation,' is an thing, unusual As in other cases of wave motion it is the form of the surface which changes rapidly

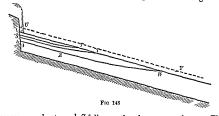
When the surface his risen to F the wave advances only down stream and there is formed a reach Fh, in which the flow is steady and uniform. On consideration it will be seen that if the

channel is long enough, the elongation of the wave ceases, its profile KC becomes fixed, and it progresses at the same rate as the mean velocity in the risen stream EK. The motion of such a wave is uniform, and the mean velocity of the stream is the same at all cross sections The proof given in chapter ii (art 9) applies to any short portion of the wave. The pressure on the upstream end is greater than on the downstream end, but the surface slope is greater than the bed slope, and the equation comes out exactly the same, S being the surface slope At different cross sections in the wave S is greater as R is less, so that V is the same everywhere Obviously the wave is convex upwards If at any cross section in the wave the slope were less than that required by the above con sideration, the velocity there would be reduced, the upstream water would overtake it and increase the slope. If the slope at any cross section were too great, the velocity there would be in creased, and the water would draw away from that upstream of it Thus the wave is in a condition of stable equilibrium, and always tends to recover its form should this be accidentally disturbed The curve KC produced to M and K gives the profile of the wave, supposing the original water surface to have been DM, or the channel to have been dry

Thus the flood wave has two distinct characters according as its profile is forming or formed. The forming wave rises as well as progresses, its velocity is at first very high, and it depends on the amount of the rise that is on the height AF. The formed wave progresses at a uniform rate and its velocity depends only on that of the risen stream, and not on the amount of the rise. The surface is in all cases convex upwards. Since any change in the form of the wave occurring at either end would be communicated to the whole of it, it is probable that, in ordinary cases the moment of time when the point II commences it move with a uniform velocity coincides nearly with the moment when the paint IG exess to rise or the wave becomes formed.

As to the four sof the curve AC the case, is a raby, in to that of the surface curve in variable steady flow (chap, vii) art [3]. The slope at I is it has will with uniform flow and depth IP give the same velocity as the depth IA with slope IA. Thus the surface all pecurre-product of the thick which is the curve can be drawn but the dutter whetheren two points where the depth are given by other hown. In a case of steady flow, with a drawing down RB, the surfaces operator than in the wave now under consideration because in that case I is greater than at A metcal of being the same and also because I is continually increasing and low the leng stored.

In the case of a reduced steady supply at S (Fig. 148) the surface assumes the forms ST, ST, etc., the point T travelling with a



decreasing velocity and S falling with a decreasing velocity. The surface eventually assumes the fixed form VZW, the portion VZ being in uniform flow, and ZW travelling with a velocity the same as the mean velocity of the fallen stream VZ. If the original surface is UY the curve is ZWY.

Ordinarily the curve of a wave is of great length, and the convexity or concavity slight If the point E is such that the volumes E and E is a convergence of the variety will reach any place, after the wave is formed, is found by dividing the distance of the place from E by the velocity of the isserstream

If the additional supply introduced, or the supply abstracted, instead of being steady, is supposed to change gradually as would be the case if it were caused by a wave coming down the upper reach or by the opening or closing of gates or shutters, the wave below A or  $\lambda$  does not at its commencement travel with such rapidity, and it more quickly assumes its fixed form, unless the water is introduced or abstracted too slowly to allow it to do so

The form of a flood wave may be observed by means of a number of gauges, but the wave, except when it is first for med—and even then if the change in the supply is not made with great abruptness—is of great length and its form or even the times of passage of its downstream end, can be accurately found only by very exact gauge readings. Slight changes in the supply, owing to rainfall or similar causes, are sufficient to vitiate the observations. Absorption of water by the channel especially in the case of a wave trivelling down a channel previously dry, may also

greatly affect the movement and form of the wave. On the Western Jumna Canal in Indra, with a mean depth of water of about 7 feet, and a velocity of about 3 5 feet per second, a rise or fall in the surface of 25 foot to 55 foot, caused by the manipulation of regulating apparatus, and occupy ing in each case less than in hour, was found to occupy 5 or 6 hours at a point 12 miles downstream, and 6 to 7 hours at a point 40 miles downstream Attempts made to observe the form of the wave failed owing to the causes just mentioned

4 Complex Cases—If a fall is succeeded by a rise to the original level the fall trivels with velocity due to the fallen stream, but the rise with velocity due to the rallen stream. At first it seems as if the rise must overtake the fall and fill up the hollow, which would result in places a long way down the stream being unaffected by the temporary diminution of supply. This is impossible it would imply that the supply passing such a place was the same as if no temporary diminution had occurred. What really happens is that the convex wave, as soon as it overtakes the other, begins to rise on it, suffirs a decrease of slope, and is checked while the front wave receives an increase of slope and is accelerated. The hollow lengthens and becomes shallower, and this goes on indefinitely. Similarly, if a rise is succeeded by a fall, the wave lengthens out indefinitely while its height decreases. At places a long way down the effect of fluctuations in the supply are slight in amount but long in duration.

Given the height of a flood at A (Fig 147), the full effect of the flood will be felt at any place K only when the height at A is maintained for a sufficiently long period. If this period is prolonged indefinitely the rise at K will not be increased, except in so far as may be due to the cessation of absorption by the flooded soil, but if the period is shortened the rise at K may be greatly reduced. Empirical formult, intended to give the height of a flood at any place, in terms of the heights in some reach upstream of it, must include the time as a factor, or, what is probably a better plan, must include gauge readings at several places upstream, and not at one place only. This plan has been adopted on various rivers, the places selected being generally those where tributaries enter. Sometimes it is sufficient merely to add together the different readings and take a given proportion. If the channel is not uniform the form of the wave, even if it

If the channel is not uniform the form of the wave, even if it has once become fixed, changes At a reduction of slope the wave assumes a more clongated, and, at an increase of slope, a

more compact form. At an increase of suffice width, supposing the mean velocity to be unaltered the wave is checked because additional space has to be filled up. At a decrease of width the velocity of the wave increases.

When an additional supply is introduced or abstracted at a place where there is not a fall, the water surface upstream is herded up or drawn down, and the form which it eventually assumes may be found by the methods explained in chapter in (art 13) The volume of water eventually added to the stream upstream of the point of change can thus be found, but the time in which it is added cannot easily be found, because it is not known how much of the supply passes downstream The commonest case of the land is that of the tide at the mouth of a river When the tide begins to rise the water in the river is headed up and its velocity reduced. As the rise of the tide becomes more rapid the discharge of the river is insufficient to keep the channel filled up so as to I sep pace with the rise of the tide the water in the mouth of the river becomes first still and level, and then tales a slope away from the sea and flows landwards At a place some way inland the water surface forms a hollow and water flows in from both directions. This may obviously continue for some time after the tide has turned and high water then occurs later at the inland place than at the mouth of the river, a fact which is sometimes unnecessarily ascribed to 'momentum' A sudden and high flood in the Indus once caused a backward flow up the Cabul River where it ioms the Indus

If in a long reach of a river the flood water way is reduced (siy by embrakments which prevent flood spill, or by training walls which cause the channel inside them to sit up) a flood of any kind will, in most of that reach, rise higher and travel more quielly than before. The same effect will be produced but to a less degree at places further downstream. When the rise is followed by a fall the wave will not flatten out to the same extent as before. In the case of a permanent rise, except in so far as there will have been less absorption than before in the flooded are imputers will be as lefere.

5 Remarks—Sometimes a wave motion is seen in a stream when the supply seems to be quite uniform. The cause may be at some abrupt change where air, becoming imprisoned, escapes at intervals. (Cf. in tail e conditions at were chap it arts 10 and 13). It is believed that in a falling stream the surface is

slightly concave across, and in a rising stream convex, but the curvature is extremely small

The action of an unsteady stream on its channel is, no doubt, subject to the same laws as in a steady stream. At the front end of a rising wave the relation of I' to D is exceptionally high, and scour is likely to occur At the advancing end of a falling wave the reverse is the case, and hence a falling flood frequently causes In discussions on the training of estuaries the idea has often been put forward as a general law that it is wrong to diminish the flow of tidal water No doubt it is the tidal water which has made the estuary If only the upland water flowed through it the size would be far too great for the volume. The salt water may enter an estuary comparatively clear and return to sea siltladen But if training walls are made so as to reduce the volume of tidal water entering the estuary, the width to be kept open is also reduced. No such sweeping law as that above stated can be upheld The Thames embankments in London contracted the channel and to some extent interfered with the tidal flow, but the channel was scoured and improved

If a stream is temporarily obstructed by gates and the water headed up the sitt deposited, if any, is removed again when the gates are opened. The same is true of obstruction caused by the rise of tides. If a given volume of water is available for the flushing of a sewer, it can probably be utilised best by introducing it intermittently, suddenly, and in considerable volumes at various points in the course of the sewer, commencing from near the tail and proceeding upwards. If there are any falls or gates it is clearly best to introduce it just below a fall or below a closed gate

Ordinarily in a rising or filling stream the relative velocities at different points in a cross section are normal but where the fresh water of a river meets the sea the relations are apt to be much disturbed especially near the turns of the tide. The fresh water, being lighter, may rise on the salt water which may have a movement landwards while the fresh water above it is moving seawards. Such a landward current is obviously not the result of the surface slope and must be due to momentum and hence temporary.

#### CHAPTER X

#### DYNAMIC EFFECT OF FLOWING WATER

## SECTION I -GENERAL INFORMATION

1 Preliminary Remarks—Hitherto we have been concerned almost entirely with questions relating to velocities, discharges and water levels—In this chapter will be considered questions relating to the Dynamic Effects of Flowing Water—In all cases the effect of friction will be neglected

By dynamic pressure is meant the pressure produced by a stream of water when its velocity or its direction of motion is altered. This is, of course, entirely different from static pressure Let V, A, and Q be the velocity, sectional area, and its charge of a stream, and W the weight of one cubic foot of the liquid. The volume discharged per second is AV, and its momentum is  $WA\frac{V}{a}$ . The force which, acting for one second, will produce on

destroy this momentum is  $F = WA \frac{V^2}{g}$  On this principle the

pressures developed in various practical cases can be ascertained Before proceeding to them it will be convenient to give two theorems regarding currents, though these do not strictly full under the herding of this chapter, and might have been given in chapter in if they had been required sooner

2 Radiating and Circular Currents—Suppose water to be supplied by the pipe AB ( $\Gamma_{10}$ , 149), and then to flow out radially between two parallel horizontal surfaces CD and F, whose distance apart is d. Of radia  $P_1$ ,  $P_2$ , let  $I_1$  be the greater, and let the velocities be  $I^*$ ,  $I^*$ , and the pre-sures  $I_1$ ,  $P_2$ . Since the discharges past all vertical cylindrical sections are equal therefore  $I_1$ ,  $I_2$ . Also since by Bernouelli's theorem the hydrostatic head

 $H = \frac{P_1}{\mu'} + \frac{P_1^*}{\pi J} = \frac{P_2^*}{\mu'} + \frac{P_2^*}{2J} = \frac{P_3^*}{\mu'} + \frac{P_3^*}{2J} = \frac{P_3^*}{2J}$ 

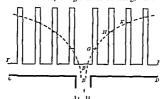
13

Therefore

$$\begin{split} P_1 &= H - \frac{I_1^{-1}}{2I} \\ P_2 &= H - \frac{I_1^{-1}}{I_1} - \frac{I_1^{-1}}{I_1^{-1}} \end{split}$$

And

or the heights in pressure columns increase from the centre out wards and tend to reach, though never reaching, the value H



the water flows mwards and passes away by the pipe the law is the same A curve through the points G, H, K, etc., is known as Barlow's curve

In a vessel (Fig. 150) which, with its contents, is revolving about a vertical axis with angular velocity a, the forces acting on a particle A whose velocity

is u are its weight wor AC, acting vertically, and a horizontal centrifugal force  $w = \frac{u^2}{gx}$  or  $w = \frac{a^2}{a} r$  or AL The water surface takes a

form normal to the resultant 1D of the above, that is, the angle  $DA\ell$  is  $\tan^{-1}\frac{a^2}{g}x$  . Hence  $\frac{dy}{dx}=\frac{a^2}{g}x$ 

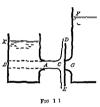
Integrating,  $y = \frac{a^2}{a} x^4$ , or the curve L I is a parabola with apex

at E Since  $u=\alpha x$ , therefore  $y=\frac{u^2}{2a}$ , or the elevation of any point above E is the head due to its velocity of revolution. The theoretical velocity of efflux from an orifice at F or L is that due to a head AF or GB

A similar condition occurs in a mass of water driven round by radiating puddles In either case the condition is termed a 'forced vortex' Questions connected with the pressure in a ridiating current or in a forced vortex enter, though not to a very important degree, into the theories of certain hydraulic machines centrifugal pump the pressures in the pump wheel follow the law of the radiating current, while those in the whirling chamber out side the wheel depend on the law of the forced vortex

## SECTION II - REACTION AND IMPACT

3 Reaction -Let 1 jet issue without contraction from an ornfice A (Fig 151) in the side of a tanl The force I causing



the flow is the pressure on B This force is called the reaction of the jet It tends to move the tanl in the direction AL It is equal to WA or to 2WAH where H is the head due to V If the trnk is supposed to move with velocity v in the direc tion AL, the absolute velocity of the issuing jet is V-1, but the quantity issuing is still AV Hence the momentum of the discharge per

second is WA V(V-v)

The principle of reaction has been utilised in driving a ship, water being pumped into the ship and driven out again stern wards The energy of the water just after leaving the ship is  $WAV \stackrel{(V-i)^2}{\longrightarrow}$ 

The work done on the ship is

$$FV = W \cdot I \cdot \frac{V(V - \iota)}{g}$$
 (58)

The total work done on the water is the sum of the above or  $y = \frac{y^{-1} - y^2}{2x}$  (~9)

$$|| 1|^{2} \frac{1}{2} \qquad (49)$$

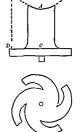
The efficiency of the machine is the ratio of (55) to (59) or 1 +1 The nearer tapproaches I the near r the efficience is to 10 lut the less the returd work done on the ship. If I = t the off in t 19 10, but the work done is mil. In the H ite it h I wis 2, so that the efficience was

The principal of reaction has alit in applied in driving a

'Reaction Wheel or 'Barker's Mill' (Fig. 152) The preceding formule and remarks apply to this case, v being the velocity of

the rotating orifices If AC is the head in the shaft the head over the orifice D is BD, AB being an imaginary water surface found by the principles of article 2 If AC=H the velocity of efflux at D is  $\sqrt{2aH+v^{1}}$ 

4 Impact -- When a jet of water (Fig 153) meets a solid surface which is at rest, it spreads out over the surface There is not, strictly speaking, any shock, but there is loss of head owing to abrupt change If the surface is horizontal and a jet strikes it vertically, it spreads out equally in all directions In other cases the amount and directions of spreading depend on the circumstances In all cases, without exception, the velocity of the jet relatively to the surface is the same after impact as before The flow after impact is along the surface which, being smooth, cannot alter the velocity of the water, but only force it to change its direction. The pressure



between the fluid and the surface in any direction is equal to the change of momentum in that direction of so much fluid as reaches the surface in one second Let a jet At (Fig. 151) meet a fixed

plane surface at right angles The momentum in the direction AC is wholly destroyed and the pressure on the plane is  $W t \frac{V^2}{t}$ , or the sume as the pressure

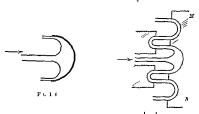
(reaction) on I or twice the pressure due to the hydrostatic head which produces ! Thus the pressure on DE will balance the pressure due to the head FG where FG is twice AB In the case shown in Fig 97 (p 135) the two heads are equal In that case the head HG has to be produced, the discharge rising through GH In the present case the head FG has merely to be muntuned

If the plane is moving with velocity r in the same direction as the jet the discharge meeting the plane per second is A(V-r) and

the pressure is  $W_{\mathcal{A}} \frac{(I-\iota)}{g}$  . The work done on the plane per second is  $WA^{(V-t)}_{g}$ . The total energy of the water before impact is  $WAV^{V^2}_{-q}$ . The efficiency is  $\frac{2(V-t)^{y}}{V}$ . This is a maximum mum when P=31 and the efficiency is then \$

If for the vine there is substituted a series of vanes as in the case of a jet directed against a series of radial vanes of a large wheel the discharge reaching the vanes per second is AV and the whole pressure is WAV(V-i) The work done per second is  $WdI \frac{(V-i)i}{n}$  and the efficiency is  $\frac{2I(V-i)i}{V^3}$  or  $2i\frac{I-i}{I}$ . It is a maximum when  $i = \frac{V}{2}$  and is then  $\frac{1}{2}$ 

If the vane is cup-shaped (Fig. 154) so that the water leaving the vine is reversed in direction, the velocity of the water leaving the vane has relatively to the vane a velocity I'-i in a backward



direction and an absolute velocity i-l+i or -i-lchange of momentum per second is  $\mathcal{U} = t^{(I-t)} \{I - (2r-I')\}$  or  $2H = \frac{(I-t)}{t}$ , and the pressure on the cup is double that on the plane considered above. The work done on the cup is  $2H \ t^{(I-z)^2} t$ . The efficiency is when I'=2r, and is then I In th nted by D<sub>E</sub> the pressure on the solid MN is t due to a si cup

If there is a series of cups the discharge per second reaching them is AV the whole pressure is  $WA\frac{I}{g}(V-(2r-I))$ ; or  $2WA\frac{I}{g}(V-q)$ . The efficience is  $\frac{4I}{I}\frac{(V-r)^n}{r}$ . It is a maximum when V=2r, and is then 1.0.

The preceding cases illustrate the great principle to be adopted in the design of water motors such as turbines and Poncelet wheels, namely, that the water shall leave the machines deprived, as far as possible, of its absolute velocity. If it has on departure any velocity it carries away work with it. In the last case it had no velocity and the efficiency is 10.

Another principle is that the water shall impinge on the vane so as to create as little disturbance as possille—that is, as nearly as possille tangentially to the vane—and thus minimise loss of energy by shock. When the jet strikes tangentially it has no tendency to spread out laterally, but shdes along the vane. In practice an exact tangential direction is impracticable, but the vanes are provided with raised edges which prevent lateral spread and cause the water to be deflected entirely in one plane

A third principle is that all passages for water shall as far as possible, be free from abrupt changes in section or direction, so that loss of head from shock shall be worlded

Let AA (Fig. 156) be a surface or vane moving in the direction

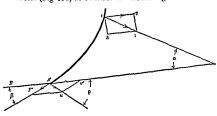
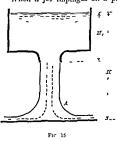


Fig 156

and with the velocity t, represented by At, and let AV represent the direction and velocity V of a jet impinging on the vane. Let

a be the angle between the two lines The line vV represents the velocity V of the jet relatively to the vane at A. Let it be assumed that the jet is deviated entirely in planes parallel to the figure. The jet leaves the vane at A with the velocity V, represented by the line AE. Draw Av equal and pirallel to Av. Then Av represents the absolute velocity of the water leaving the vane. Let the angle vA = 0 and BA = 0. If the quantity of water reaching the vane per second is u, the original and final momenta of the water resolved in a direction pirallel v.

to Av are  $\frac{w}{g}V\cos a$  and  $\frac{w}{g}V\cos \theta$  The change of momentum or pressure in the direction Av is  $\frac{w}{g}(V\cos a - V\cos \theta)$  or  $\frac{w}{g}(V\cos a - v + V\cos \theta)$ . These are general expressions cover ing all cases, and the preceding ones can be derived from them? When a jet impinges on a plane, as in Fig. 157, the issuing



is about \$\sigma\_q H\$ The outer streams at \$A\$ press on the inner by reason of centrifugal force, and the intensity of pressure increases towards the centre of the jet. It cannot exceed the amount due to \$\frac{T}{2J}\$ or \$H\_t\$ because otherwise the direction of flow would be reversed. Experiments made by Beresford \$2\$ with jets \$475\$.

velocity of the jet is theo retically  $\sqrt{2gH_{11}}$ , but on reach ing the plane the velocity V

meh to 195 meh m diameter falling on a briss plate show

\* Professional I apers on Indian I nomering No coexxii

<sup>1</sup> Some machines which illustrate the principles of dynamic pressure have been referred to above. There are many much ness such as water meters, modules, rams, presses, pumps, water wheels and water pressurengines which though water passes through them illustrate in a principle of hydraules, the questions involved in their design being engineering and dynamical. In fact, the principles involved in the above form the rejarding varies are dynamical, and are given here to brigo over a kap between by draulies and another accuracy. The same remark applies to parts of its succeeding article.

that at the axis of the jet, the pressure is very nearly that due to If and the pressure becomes negligible at a distance from the axis equal to alse ut twice the diameter of the jet pressure is thus distributed over an area of about four times that of the section of the jet. The pressures were measured by means of a water-column communicating with a small hole in the plate whose position could be altered

5 Miscellaneous Cases -Wien water flows round a lend in a channel the dinamic pressure produced on the channel is the same as if the channel was a curved rane. At lends in large pipes anchors are sometimes required to hold the pipe

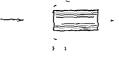
When a mass of water flowing in a 1 pe is alruptly brought to rest by the closure of a gate r value the pressure produced in  $f = \frac{v - u \cdot m}{L \cdot 2rm + WT}$ where I is the length I the p pe affected by the pulest on man! If the moduli of elast city for water and f r the material of the p pe in pounds per square in h T the ti charse f the pipe in inches r the ral us of the p pe in feet an I e the velocity of the water in feet per second f being in poun la per a juare incloser an l'above il e static pressure 1

When a thin plate (Fig. 155) is moved normally through still water with velocity I, a mass of water in front of the plate is put in motion and those portions of it which flow off at the sides of the plate cannot turn sharp round and fill up the space lehind the plate Instead of doing this they penetrate into the rest of



the water and so communicate forward momentum to it while other portions of still water have to be set in motion to fill up the space behind. Thus there is produced a resistance which is independent of friction or viscosity Practically it is found that

the resistance is KW 1 where A is 1 7 to 18 the lest results giving



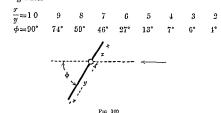
13 to 16 The resistance is less than that caused by the impinging on a fixed I lane of a jet

of the same section as the area of the plate with a velocity V

If for the plate there is substituted a cylinder (Fig. 159) whose length is not more than about three diameters, the resistance is less than in the case of the plate. It is further reduced if the downstream end of the cylinder is pointed.

In the above cases, if the plane or cylinder is fixed and the water moving, the pressures are the same

The following statement shows the approximate results of some experiments made by Higen to show the position assumed by a rectangular plane surface when proted (Fig. 160) and placed in flowing water —



rig is

When a thin sharpened plate or a spindle shaped or ship shaped both is moved endways through still water the resistance is almost wholly frictional and is nearly as  $\Gamma$ , but if the body is only partly submer\_cd waves are produced, and when  $\Gamma$  exceeds a certain limit (which lears a relation to the size of the body) the wave resistance increases after than  $\Gamma^2$ . If the body, though sharp at both ends, tapers more rapidly at one end than at the other, it probably causes least resistance when the blunter end is forward.

In experiments made by Froude by towing boards through still water, it was found that the power of the velocity to which the friction is proportional varies for different surfaces, being sometimes less than 2 and some times more. Also that for long boards f (chap ii art 9) is much less than for short ones, the reason being that the forward pirt of a long board communicates motion to the water, and the succeeding jortion thus experiences less revisance.

<sup>1</sup> For results of some recent experiments on cylinders with square and pointed ends see Min Proc. Inst. C.E., vol. exvii

# APPENDIX A

### CALCULATION OF m AND n

(Chap 11, arts. 5 and 8)

# THE following is a specimen of the method of calculating -

(1)	(2)	(3)	(4)	(5)	(6)	(1)	(8)	(9)
Height of Weir	Head	(op-	И* <u>П²</u> (≠Н)²	# (25- (25-	N or 1+241° (+1)-	] = V2 H2	is cr col - 4 c L 4	
Metres I 135		4254	00255	43.0	1-0056	10056	2 18	1 45
75	Do	4316	00518		1-0130	-0130	2 30	1-67
50	Ю	4359	-0100		1-655	655	225	1 52

Height of Weir

Head observed

M as

Three assumed sets of values for : and for each the

corresponding value of n

(1)	(2)	(3)	(4)		(5)		(6)	
Feet 3 72 2 46 1 64 1 15 79	Peet 49 Do Do Do Do	4284 4316 4359 4424 4522	4250 Do Do 4273 4303	1 45 1 67 1 52 1 29 89	#4270 Do Do 4283 4313	97 1 36 1 37 1 19 86	11 4284 Do Do 4297 4327	1 1 14 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Mean	Do			1 36	_	1 12		86
3 72 2 46 1 64 1 15 79	1 31 Do Do Do Do	4286 4430 4595 4794 5034	418a 4207 4245 4305 4395	1 28 1 42 1 20 1 04 86	4200 4221 4280 4320 4410	1 09 1 30 1 15 1 02 85	4286 4308 4346 4406 4500	85 96 87 70
Mean	Do			1 16		1 05		C7
3 31 <sup>1</sup> 2 46	1 44 Do	4310 4452	4167 4178	1 32 1 61	4200 4233	1 02 1 28	4214 4275	1 07
Mean	Do			1 47		1 15		1 04
3 31 2	1 80	4334	4100	1 51	4190	98	4211	89

2 Let gth of weir reduced to 1 64 feet

It will be noticed that slight changes in m cause great changes in n Obviously m cannot rise to the values shown in column 6, as it would then equal M for the highest weirs If reduced much below the value of column 4 it would make n very high values of m and n which seem most suitable are those of column 5, the mean value of n being 1 1

### APPENDIX B

NOTE REGARDING VALUE OF C IN VARIABLE FLOW

(Chap ii arts 10 and 12)

It may be said that no proof has been given that C is the same as in uniform flow. The case is somewhat analogous to the fourth proposition in Euclids book i. Regarding this it has been remarked that it would be sufficient to state that the two triangles are equal because there is no reason why they should be different Consider a portion of a uniform stream 200 feet long with H=50 feet, D=5 feet and V=2.5 feet per second. Now let W be 52 feet at one end and 48 feet at the other, so that  $V_1$  and V are, respectively, 2.4 and 2.6 feet per second. There is no reason why any appreciable alteration should occur either in the total loss of head from the resistance of the border, or in the velocity curves of the central section, or the average of the velocity curves of the whole length considered. Consequently there is no reason why C should be altered

#### APPENDIX C

VALUE OF A IN THE LAVI AT SIDENAL

(Chap vi art 13)

The river is straight for five miles upstrain of the discharge site and one mile downstream a reach unique, perhaps, unong the rivers of the world but its great length can hardly be the cause of the low value of N The silt is caused by a dum a mile below the discharge site. In floods the dam is removed and the silt then scours out. Thus the bed is probably roughest for the greatest depths of water. In spite of this, N is very much the same for all the depths from 6 feet to 10 feet, and C somewhere about 200, whereas Bazin s highest figure is 152



